

PSG COLLEGE OF ARTS & SCIENCE
(AUTONOMOUS)

BSc DEGREE EXAMINATION DECEMBER 2019
(Third Semester)

Branch-STATISTICS

PROBABILITY AND DISTRIBUTION-II

Time: Three Hours

Maximum: 75 Marks

SECTION-A (10 Marks)

Answer ALL questions

ALL questions carry EQUAL marks (10x1 = 10)

The characteristic function of the binomial distribution for the binomial variate $X \sim b(n, p)$ is :

- (i) $(q+pe^{it})^n$ (ii) $(p+qe^{-it})^n$
(iii) $(P+qe^{it})^n$ (iv) $(q+pe^{it})^n$

A Poisson random variable has $\mu=2$, the value of its mean is

- (i) X (ii) $\frac{\mu}{\sigma}$
(iii) μ (iv) σ

If a distribution has moment generating function $M_x(t) = (2 - e^t)^{-\lambda}$, then the distribution is

- (i) geometric distribution (ii) Hyper geometric distribution
(iii) binomial distribution (iv) Negative binomial distribution

The distribution having the m.g.f. $\frac{1}{(3 - 2e^t)^k}$ can be defined as

- (i) Negative binomial distribution (ii) Geometric distribution
(iii) Exponential distribution (iv) None of the above

The distribution function of a continuous uniform distribution of a variable X lying in the interval (a, b) is

- (i) $\frac{x-a}{b-a}$ (ii) $\frac{X-a}{b-a}$
(iii) $\frac{b-a}{X-a}$ (iv) $\frac{X-b}{b-a}$

The range of exponential distribution is

- (i) $0 < x < \infty$ (ii) $X < 0$
(iii) $\infty < x < \infty$ (iv) $0 < x < 1$

The characteristic function of gamma distribution is

- (i) $(1-it)^{-\lambda}$ (ii) $(1-it)^{-\lambda}$
(iii) $(1-it)^{\lambda}$ (iv) None of these

The harmonic mean of Beta distribution of second kind

- (i) $\frac{B}{v-1}$ (ii) $\frac{\hat{B}-1}{v-1}$
(iii) $B-1$ (iv) $\frac{B}{v}$

9 If the sample size $n=2$, the Student's t-distribution reduces to

- (i) $n-1$ (ii) n

- 10 The skewness in a chi-square distribution will be zero if
- | | |
|---------------------|------------|
| (i) n^{co} | (ii) $n=0$ |
| (iii) $n=1$ | (iv) $n<0$ |

SECTION - B (35 Marks)Answer **ALL** Questions**ALL** Questions Carry **EQUAL** Marks (5 x 7 = 35)

- 11 a Ten coins are tossed simultaneously. Find the probability of getting (i) at least seven heads (ii) exactly seven heads and (iii) at the most seven heads.
OR
b Obtain the mean and variance of Poisson distribution.
- 12 a A machine is known to produce 3% defective items. What is the probability that at least 5 items are to be examined in order to get 2 defective items?
OR
b Define the following:
(i) Geometric distribution and (ii) Hyper geometric distribution
- 13 a State the important properties of Normal distribution.
OR
b Show that the exponential distribution "Lacks of memory".
- 14 a Determine the mean and variance of Gamma distribution.
OR
b Find the constant of Beta distribution for second kind.
- 15 a State and prove Additive property of Chi-Square distribution.
OR
b Bring out the applications of t-distribution.

SECTION - C (30 Marks)Answer any **THREE** Questions**ALL** Questions Carry **EQUAL** Marks (3 x 10 = 30)

- 16 Find the mean and variance of Binomial distribution using MGF.
- 17 Prove that the recurrence relation for the moments of Poisson distribution.
- 18 Obtain the inflexion point for the Normal distribution follows $N(0,1)$.
- 19 Derive the mean and variance of Beta distribution of first kind.
- 20 Derive the student's t-distribution and mention its applications.

Z-Z-Z

END