

**PSG COLLEGE OF ARTS & SCIENCE**  
(AUTONOMOUS)  
**BSc DEGREE EXAMINATION DECEMBER 2019**  
(Fifth Semester)

**Branch- STATISTICS**

**CORE ELECTIVE -1: OPERATIONS RESEARCH -1**

Time : Three Hours

Maximum : 75 Marks

**SECTION-A (20 Marks)**

Answer **ALL** questions

**ALL** questions carry **EQUAL** marks (10 x 2 = 20)

- 1 What is the scope of O.R?
- 2 State the mathematical formulation of LPP.
- 3 Define Slack Variables.
- 4 Define initial basic feasible solution of LPP.
- 5 What do you mean by duality in LPP?
- 6 State any two important results in duality.
- 7 Define feasible solution in transportation problem.
- 8 State the degeneracy in transportation problem.
- 9 Define unbalanced assignment problem with an example.
- 10 Define total elapsed time and idle time on machine with an example.

**SECTION - B (25 Marks)**

Answer **ALL** Questions

**ALL** Questions Carry **EQUAL** Marks (5 x 5 = 25)

- 11 a Discuss the characteristic of a good linear programming model.  
OR  
b Old hens can be bought at Rs.2 each and young ones at Rs.5 each. The old hens lay 3 eggs per week and the young ones lay 5 eggs per week, each egg being worth 30 paise. A hen cost Rs.1 per week to feed. A person has only Rs.80 to spend for hens. How many of each kind should he buy to give a profit of more than Rs.6 per week, assuming that he cannot house more than 20 hens. Formulate this as LPP.
- 12 a Explain the canonical and standard forms of LPP with suitable illustrations.  
OR  
b Solve the following LPP by simplex method.  
Maximize  $z=4x_1+10x_2$   
subject to the constraints  
 **$2x_1+x_2<50$**   
 **$2x_1+5x_2<100$**   
 **$2x_1+3x_2<90$**   
and  $x_1, x_2 > 0$
- 13 a Write down the dual of the following LPP.  
Maximize  $z=4x_1+3x_2$   
subject to the constraints  
 $-x_1, x_2 < -3$   
 **$-x_1+x_2 > -2$**   
 $x_1, x_2 > 0$   
OR  
b Write the mathematical model of the dual simplex method.

Cont...

Find the initial basic feasible solution for the following transportation problem by VAM.

Si	Distribution Centres				Availability
	D <sub>1</sub>	D <sub>2</sub>	D <sub>3</sub>	D <sub>4</sub>	
s <sub>1</sub>	11	13	17	14	250
s <sub>2</sub>	16	18	14	10	300
s <sub>3</sub>	21	24	13	10	400
Requirements	200	225	275	250	

OR

Write the methods of finding initial basic feasible solution in transportation problem and explain the procedure of any one method.

Solve the following Assignment Problem.

Person	Job				
	1	2	3	4	5
A	8	4	2	6	5
B	0	9	5	5	4
C	3	8	9	2	6
D	4	3	1	0	3
E	9	5	8	9	5

OR

Explain the Johnson's procedure of solving a sequencing problem of 'n' jobs on '3' machines.

### SECTION - C (30 Marks)

Answer any **THREE** Questions

**ALL** Questions Carry **EQUAL** Marks (3 x 10 = 30)

Solve the LPP graphically

Maximize  $z = 5x_1 + 3x_2$

subject to

$$4x_1 + 5x_2 < 1000$$

$$5x_1 + 2x_2 < 1000$$

$$3x_1 + 8x_2 < 1200$$

and  $x_1, x_2 > 0$

Use Big-M method to solve

Maximize  $z = 4x_1 + 3x_2$

subject to

$$2x_1 + x_2 > 10$$

$$-3x_1 + 2x_2 < 6$$

$$x_1 + x_2 > 6$$

and  $x_1, x_2 > 0$

Use dual Simplex method to solve the LPP.

Maximize  $z = -3x_1 - 2x_2$

subject to

$$x_1 + x_2 > 1$$

$$x_1 + x_2 < 7$$

$$x_1 + 2x_2 > 10$$

$$x_2 < 3$$

and  $x_1, x_2 > 0$

Describe the procedure of MODI method in transportation problem.

Find the sequence that minimizes the total elapsed time required to complete the following jobs on machines  $M_1, M_2$ , and  $M_3$  in the order  $M_1, M_2, M_3$ .

Task	A · B   c	D <sup>-</sup>	E <sup>-</sup>	F	G	H   I
1U.	9 5 4	0	6	8	7	5 4