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## PSG COLLEGE OF ARTS & SCIENCE

(AUTONOMOUS)

## **MCom (IB) DEGREE EXAMINATION MAY 2022**

(Second Semester)

## Branch - INTERNATIONAL BUSINESS

# BUSINESS STATISTICS AND MATHEMATICAL OPTIMIZATION TECHNIQUES

|     | Time: Three Hours Maximum: 50 Marks  |
|-----|--|
|     | SECTION-A (5 Marks)  Answer ALL questions  ALL questions carry EQUAL marks (5 x 1 = 5)   |
| 1   | In a symmetrical distribution, the coefficient of skewness is  (i) negative  (ii) positive  (iii) zero  (iv) either positive or negative                                     |
| 2   | If the sum of the product of deviations of X and Y series from their means is zero then the coefficient of correlation is  (i) +1  (ii) 0  (iii) -1  (iv) none of these      |
| 3   | The mean difference between 9 paired observations is 15 and the standard 4 deviation of differences is 5. The value of t-statistic is  (i) 27  (ii) 9  (iii) 3  (iv) 15      |
| 4 · | An optimization model  (i) provides the best solution  (ii) provides decision within its limited context  (iii) helps in evaluating various alternatives  (iv) all the above |
| 5   | A saddle point exists when  (i) maximin value = maximax value  (ii) minimax value = minimum value  (iii) minimax value = minimum value  (iv) none of the above               |
|     | $\frac{\text{SECTION - B (15 Marks)}}{\text{Answer ALL Questions}}$ $\text{ALL Questions Carry EQUAL Marks} \qquad (5 \times 3 = 15)$  |
| 6.  | a Give the names of one dimensional diagrams.  OR  b The average of 7 numbers 7, 9, 12, x, 5, 4, 11 is 9. Find the missing number x  |
| 7   | a What is positive correlation? Give example.  OR  |
|     | b If the two lines of regression are: $x + 2y - 5 = 0$ and $2x + 3y - 8 = 0$ , calculate the mean values of x and y.   |
| 8   | a What is ANOVA?  OR   |
|     | b Write the test statistic for testing the significance of difference of means for   |

large samples.

9 a What is transportation problem?

OR

b Solve the following problems:

Machines

Jobs

| 120 | 100 | 80  |
|-----|-----|-----|
| 80  | 90  | 110 |
| 110 | 140 | 120 |

10 a What is two person's zero sum game?

OR

b Solve the following game:

| Player A       | Player B |       |       |  |  |
|----------------|----------|-------|-------|--|--|
|                | $B_1$    | $B_2$ | $B_3$ |  |  |
| Aı             | - 2      | 15    | - 2   |  |  |
| A <sub>2</sub> | - 5      | - 6   | - 4   |  |  |
| $A_3$          | -5       | 20    | - 8   |  |  |

### SECTION -C (30 Marks)

Answer ALL questions

ALL questions carry EQUAL Marks

 $(5 \times 6 = 30)$ 

11 a From the following data calculate the mean and mode.

| Wages          | 110 | 112 | 113 | 117 | 120 | 125 |
|----------------|-----|-----|-----|-----|-----|-----|
| No. of workers | 26  | 17  | 13  | 15  | 14  | 8   |

OR

b Find the coefficient of skewness from the following information: Difference of two quartiles = 8, mode = 11, sum of two quartiles = 22, mean = 8

Write the procedure for testing the significance of single mean for large samples

b Find the most likely production corresponding to a rainfall 40<sup>0</sup> from the following data:

 $\begin{array}{ccc} & \text{Rainfall} & \text{Production} \\ \text{Average} & 30^0 & 500 \text{ kg} \\ \text{Standard deviation} & 5^0 & 100 \text{ kg} \end{array}$ 

Coefficient of correlation = 0.5

13 a Two types of batteries A and B are tested for their length the life and the following results are obtained:

| Battery | sample size | mean (hrs) | variance (hrs) |
|---------|-------------|------------|----------------|
| A       | 10          | 500        | 110            |
| В       | 12          | 560        | 121            |

Is there any significant difference between the two sample means?

OR

The following table gives the classification of 100 workers according to sex and the nature of work. Test whether the nature of work is independent of the sex of the worker.

| OIRCI.  | Skilled | Unskilled |
|---------|---------|-----------|
| Males   | 40      | 20        |
| Females | 10      | 30        |

Obtain the initial basic feasible solution for the following transportation problem by Vogel's approximation method.

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|-------------|-------|--------|------------|------------|-----------|
|             | $D_1$ | $D_2$  | D3         | $D_4$      | Supply    |
| $S_1$       | 19    | 30     | 50         | 10         | 7         |
| $S_2$       | 70    | 30     | 40         | 60         | 9         |
| $S_3$       | 40    | 8      | 70         | 20         | 18        |
| Demand      | . 5   | 8      | 7          | 14         | 34        |

OR

b A department of a company has five employees with five jobs to be performed. The time (in hours) that makes to perform each job is given in the effectiveness matrix.

| Jobs | Employees |    |     |    |    |  |
|------|-----------|----|-----|----|----|--|
|      | I         | II | III | IV | V  |  |
| A    | 10        | 5  | 13  | 15 | 16 |  |
| В    | 3         | 9  | 18  | 13 | 6  |  |
| С    | 10        | 7  | 2   | 2  | 2  |  |
| D    | 7         | 11 | 9   | 2  | 12 |  |
| E    | 7         | 9  | 10  | 4  | 12 |  |

How should the jobs be allocated, one per employee, so as to minimize the total man hours?

15 a Explain the decision environment under uncertainty.

#### OR

b Solve the following game using dominance principle

| Player           | ,     | Player B |       |       |  |  |
|------------------|-------|----------|-------|-------|--|--|
| A                | $B_1$ | $B_2$    | $B_3$ | $B_4$ |  |  |
| $A_1$            | 3     | 2        | 4     | 0     |  |  |
| $A_2$            | 3     | 4        | 2     | 4     |  |  |
| $\overline{A_3}$ | 4     | 2        | 4     | 0     |  |  |
| A                | 0     | 4        | 0     | 8     |  |  |