

PSG COLLEGE OF ARTS & SCIENCE
(AUTONOMOUS)

BSc / BCA DEGREE EXAMINATION MAY 2024
(Second Semester)

Common to Branches – INFORMATION TECHNOLOGY &
COMPUTER APPLICATION

MATHEMATICAL FOUNDATIONS OF COMPUTING

Time: Three Hours

Maximum: 75 Marks

SECTION-A (10 Marks)

Answer ALL questions

ALL questions carry EQUAL marks

(10 × 1 = 10)

Module No.	Question No.	Question	K Level	CO
1	1	The rank of two matrices are same only if they are _____ matrices. a) row c) equivalent	K1	CO1
		b) square d) non zero		
2	2	Which matrix satisfies its own characteristic equation? a) row c) column	K2	CO1
		b) square d) singular		
2	3	Which of the following are the roots of $\frac{d^2y}{dx^2} + 5\frac{dy}{dx} + 4y = 0$? a) 1 and 4 c) -1 and 4	K2	CO2
		b) -1 and -4 d) 1 and -4		
3	4	Identify the roots of the equation whose solution is $y = Ae^{m_1x} + Be^{m_2x}$ a) real and distinct c) imaginary	K1	CO2
		b) real and equal d) constant		
3	5	What is the PDE of $z = (x + a)(y + b)$ by eliminating a and b? a) $z = (x + p)(y + q)$ c) $z = (x + q)(y + p)$	K2	CO3
		b) $z = (x - p)(y - q)$ d) $z = pq$		
4	6	Identify the Lagrange's linear equation. a) $P + Q = R$ c) $Pp - Qq = R$	K1	CO3
		b) $P - Q = R$ d) $Pp + Qq = R$		
4	7	In Gauss-Jordan elimination method, the given matrix is reduced to _____ matrix. a) upper triangular c) diagonal	K2	CO4
		b) lower triangular d) identity		
5	8	Interpret the convergence, when the coefficient matrix A is diagonally dominant in $AX = B$? a) converges slowly c) does not converge	K1	CO4
		b) converges quickly d) converges always		
5	9	The process of computing _____ is called numerical differentiation. a) derivative b) derivative of a constant c) derivative for some particular value d) integral	K1	CO5
	10	Compute the order of error in Trapezoidal rule. a) h^2 b) h^3 c) h^{-1} d) h^{-2}		

Cont...

SECTION - B (35 Marks)

Answer ALL questions

ALL questions carry EQUAL Marks

(5 × 7 = 35)

Module No.	Question No.	Question	K Level	CO												
1	11.a.	Identify the rank of $\begin{bmatrix} -2 & -1 & -1 \\ 12 & 8 & 6 \\ 10 & 5 & 6 \end{bmatrix}$.	K2	CO1												
		(OR)														
	11.b.	Calculate A^4 , when $A = \begin{bmatrix} -1 & 3 \\ -1 & 4 \end{bmatrix}$.														
2	12.a.	Solve $\frac{d^3y}{dx^3} - 3\frac{dy}{dx} + 2y = 0$.	K3	CO2												
		(OR)														
	12.b.	Solve $(D^2 + 5D + 6)y = e^x$.														
3	13.a.	Solve $\frac{\partial^2 z}{\partial x \partial y} = 0$.	K3	CO3												
		(OR)														
	13.b.	Solve $p^2 + q^2 = npq$.														
4	14.a.	Apply Gaussian elimination method to solve the following system of equations. $x + y + z = 9$ $2x - 3y + 4z = 13$ $3x + 4y + 5z = 40$	K3	CO4												
		(OR)														
	14.b.	Apply Gauss Jordan method to solve the following system of equations. $x + y = 2$ $2x + 3y = 5$														
5	15.a.	Evaluate $\frac{dy}{dx}$ and $\frac{d^2y}{dx^2}$ at $x = 51$ from the following data <table style="margin-left: 20px;"> <tr> <td>x</td> <td>50</td> <td>60</td> <td>70</td> <td>80</td> <td>90</td> </tr> <tr> <td>y</td> <td>19.96</td> <td>36.65</td> <td>58.81</td> <td>77.21</td> <td>94.61</td> </tr> </table>	x	50	60	70	80	90	y	19.96	36.65	58.81	77.21	94.61	K4	CO5
	x	50	60	70	80	90										
y	19.96	36.65	58.81	77.21	94.61											
	(OR)															
	15.b.	Evaluate $\int_0^5 \frac{dx}{4x+5}$ by Trapezoidal rule using 11 coordinates.														

SECTION - C (30 Marks)

Answer ANY THREE questions

ALL questions carry EQUAL Marks

(3 × 10 = 30)

Module No.	Question No.	Question	K Level	CO												
1	16	Diagonalize the matrix $\begin{bmatrix} 2 & 2 & 0 \\ 2 & 1 & 1 \\ -7 & 2 & -3 \end{bmatrix}$.	K4	CO1												
2	17	Solve $(D^2 - 3D + 2)y = \sin 3x$.	K3	CO2												
3	18	Solve $x^2 \frac{\partial z}{\partial x} + y^2 \frac{\partial z}{\partial y} = (x + y)z$.	K3	CO3												
4	19	Apply Gauss Seidel iteration method to solve the following system of equations. $6x + 15y + 2z = 72$ $x + y + 5z = 110$ $27x + 6y - z = 85$	K3	CO4												
5	20	The population of a certain town is given below. <table style="margin-left: 20px;"> <tr> <td>Year</td> <td>1931</td> <td>1941</td> <td>1951</td> <td>1961</td> <td>1971</td> </tr> <tr> <td>Population</td> <td>40.62</td> <td>60.80</td> <td>79.95</td> <td>103.56</td> <td>132.65</td> </tr> </table> Evaluate the rate of growth of the population in 1961.	Year	1931	1941	1951	1961	1971	Population	40.62	60.80	79.95	103.56	132.65	K4	CO5
Year	1931	1941	1951	1961	1971											
Population	40.62	60.80	79.95	103.56	132.65											