

**rstj CULFLGE OF ARTS & SCIENCE**  
**(AUTONOMOUS)**  
**BSc DEGREE EXAMINATION MAY 2018**  
**(Sixth Semester)**

Branch - STATISTICS

**CORE ELECTIVE - II OPERATIONS RESEARCH - II**

Time : Three Hours

Maximum : 75 Marks

**SECTION-A (20 Marks!)**

Answer ALL questions

ALL questions carry EQUAL marks (10 x 2 = 20)

- 1 Define strategy for a player.
- 2 What is meant by saddle point?
- 3 State group replacement policy.
- 4 What happens to the items that deteriorate gradually for optimum replacement interval?
- 5 Define simulation.
- 6 State the classification of simulation models.
- 7 Define size of the queue.
- 8 What do you mean by Poisson queues?
- 9 Define dummy activity in network theory .
- 10 Given variance = 3, duration of project = 17 days what is the probability of meeting the due date of 19 weeks?

**SECTION - B (25 Marks!)**

Answer ALL Questions

ALL Questions Carry EQUAL Marks (5 x 5 = 25)

- 11 a For what value of X, the game with following payoff matrix is strictly determinable?

		Player B		
		B <sub>1</sub>	B <sub>2</sub>	B <sub>3</sub>
Player A	A <sub>1</sub>	X	6	2
	A <sub>2</sub>	-1	X	-7
	A <sub>3</sub>	-2	4	3

OR

- b Solve the game:

		Player B	
		B <sub>1</sub>	B <sub>2</sub>
Player A	A <sub>1</sub>	30	2
	A <sub>2</sub>	4	14
	A <sub>3</sub>	6	9

- 12 a The yearly cost of two machines A and B, when money value is neglected is shown in table below. Find their cost patterns if money value is 10% per year and hence find which machine is more economical.

Year	1	2	3
Machine A (Rs.)	1800	1200	1400
Machine B (Rs.)	2800	200	1400

OR

- b Explain group replacement policy.

- 13 a Explain Monte Carlo simulation.

OR

- b Explain generation of random numbers.

**Cont...**

- 14 a On an average, 6 customers reach a telephone booth every hour to make calls. Determine the probability that exactly 4 customers will reach in 30-minutes period, assuming that arrivals follow Poisson distribution.

OR

- b Customers arrive at the first class ticket counter of a theatre at the rate of 12 per hour. There is one clerk serving the customers at the rate of 30 per hour.

- i) What is the probability that there is no customer in the counter.  
ii) What is the probability that there are more than 2 customers in the counter?

- 15 a Explain the rules of construction of a network.

OR

- b Draw a network to represent the project.

Task : A < D, A < E, B < F, D < F, C < G, C < H, F < I, G < I

Task:	A	B	C	D	E	F	G		H I
Davs:-	8	10	8	10	16	17	17	14	9

### **SECTION - C (30 Marks!**

Answer any THREE Questions

ALL Questions Carry EQUAL Marks (3 x 10 = 30)

- 16 Solve the following game by using the principle of dominance.

		Player B					
		I	II	III	IV	V	VI
Player A	1	4	2	0	2	1	1
	4	4	3	1	3	2	2
	J	4	3	7	-5	1	2
	4	4	3	4	-1	2	2
	5	4	3	J	-2	2	2

- 17 The maintenance cost and resale value per year of a machine whose purchase price is Rs. 7,000 is given below:

Year:	1	2	3	4	5	6	7	<b>8</b>
Maintenance cost in Rs. :	900	1,200	1,600	2,100	2,800	3,700	4,700	5,900
Resale value in Rs. :	4,000	2,000	1,200	600	500	400	400	400

When should the machine be replace?

- 18 Generate a sequence of 5 two - digit random numbers by employing mixed congruential method given the recursive equation as

$$r_{i+1} = (2r_i + 53) \pmod{100} \text{ and } r_0 = 46.$$

- 19 A self service store employs one cashier at its counter. Nine customers on an average every 5 minutes while the cashier can serve 10 customers in 5 minutes. Assuming Poisson distribution for arrival rate and exponential distribution for service time, find

- (i) Average number of customers in the sy stem  
(ii) Average number of customers in the queue or average queue length  
(iii) Average time a customer spends in the system  
(iv) Average time a customer waits before being served.

- 20 A mother notes that when her teenage son uses the telephone, he takes no less then 10 minutes for a call and sometimes as much as one hour. Twenty-minutes calls are more frequent than calls of any other duration.

If son's phone call were an activity in a PERT project:

- (i) What would be the phone call's expected duration?  
(ii) What would be its variance ?  
(iii) In scheduling the project, how much time would be allocated for the phone call?