

PSG COLLEGE OF ARTS & SCIENCE
(AUTONOMOUS)
BSc DEGREE EXAMINATION DECEMBER 2019
(First Semester)

Branch – CHEMISTRY

MATHEMATICS – I

Time: Three Hours

Maximum: 75 Marks

SECTION-A (10 Marks)

Answer ALL questions

ALL questions carry EQUAL marks

(10 x 1 = 10)

- 1 If the roots are $1 + \sqrt{2}, 3$, then the equation with rational coefficient is _____.
 (i) $x^3 - 5x^2 + 5x + 3 = 0$ (ii) $x^2 + 5x + 3 = 0$
 (iii) $5x^2 - 5x - 3 = 0$ (iv) $x^3 - x^2 - x - 3 = 0$
- 2 Sum of the roots of $x^3 - 7x + 6 = 0$ is
 (i) 0 (ii) -7 (iii) 6 (iv) 7
- 3 The locus of center of curvature is called as _____.
 (i) Involute (ii) evolute (iii) envelope (iv) circle of curvature
- 4 The curvature of a straight line is _____.
 (i) 3 (ii) 2 (iii) 1 (iv) 0
- 5 If $f(x)$ is an odd function of x , then $\int_{-a}^a f(x) dx$ is _____.
 (i) 0 (ii) a (iii) $-a$ (iv) $2a$
- 6 $\int xe^x dx$ is _____.
 (i) e^x (ii) $x - 1$ (iii) $e^x(x - 1)$ (iv) $\frac{e^x}{x - 1}$
- 7 $\int_0^{\frac{\pi}{2}} \int_0^{\cos \theta} dr d\theta$ is _____.
 (i) 1 (ii) -1 (iii) $\frac{\pi}{2}$ (iv) $-\frac{\pi}{2}$
- 8 $\int_0^1 \int_0^1 \int_0^1 dx dy dz =$ _____.
 (i) 1 (ii) 0 (iii) -1 (iv) 2
- 9 $\theta + \frac{\theta^3}{3} + \frac{2\theta^5}{15} + \dots$ is _____.
 (i) $\sin \theta$ (ii) $\cos \theta$ (iii) $\tan \theta$ (iv) $\sec \theta$
- 10 $\cosh^2 x - \sinh^2 x =$ _____.
 (i) $\cosh 2x$ (ii) $\sinh 2x$ (iii) 1 (iv) -1

SECTION - B (25 Marks)

Answer ALL questions

ALL questions carry EQUAL Marks

(5 x 5 = 25)

- 11 a Solve the equation $2x^3 - 11x^2 + 10x + 8 = 0$ given that one of the root is double to another of its roots.

OR

- b Transform the equation $x^4 - 8x^3 - x^2 + 68x + 60 = 0$ into one which does not

12 a Show that the radius of curvature at any point of the curve $y = c \cosh \frac{x}{e}$ is $\frac{y^2}{c}$.

OR

b Find the curvature of the curve $xy = c^2 t (c, c)$.

13 a Prove that $\int_0^{\frac{\pi}{4}} \log(1 + \tan \theta) d\theta = \frac{\pi}{8} \log 2$.

OR

b Obtain the reduction formula for $\int \tan^n x dx$.

14 a Evaluate $\int_1^{2x} \int_1^{xy^2} dy dx$.

OR

b $\int_0^1 \int_0^{1-x} \int_0^y x dx dy dz$.

15 a Express $\cos 8\theta$ in terms of $\cos \theta$.

OR

b If $\sin(A+iB) = x+iy$, then prove that

$$(i) \frac{x^2}{\sin^2 A} - \frac{y^2}{\cos^2 A} = 1 \quad (ii) \frac{x^2}{\cosh^2 B} - \frac{y^2}{\sinh^2 B} = 1$$

SECTION -C (40 Marks)

Answer ALL questions

ALL questions carry EQUAL Marks

(5 x 8 = 40)

16 a If α, β, γ are the roots of $x^3 + px^2 + qx + r = 0$, then form the equation whose roots are

$$(i) \alpha + \beta, \beta + \gamma, \gamma + \alpha \quad (ii) \frac{1}{\alpha^2}, \frac{1}{\beta^2}, \frac{1}{\gamma^2}$$

OR

b Solve the following equation $3x^6 + x^5 - 27x^4 + 27x^2 - x - 3 = 0$.

17 a Find the centre of curvature of $x = a(t + \sin t)$ $y = a(1 - \cos t)$.

OR

b Show that the evolute of the curve $x = a(\cos \theta + \theta \sin \theta)$ $y = a(\sin \theta - \theta \cos \theta)$ is a circle.

18 a If $m > 0$ and $n > 0$, then prove that $\int_0^1 x^m (1-x)^n dx = \frac{m!n!}{(m+n-1)!}$

OR

b Evaluate $\int x^4 e^x dx$.

19 a Find the volume bounded by the cylinder $x^2 + y^2 = 4$ the planes $y + z = 4$ & $z = 0$.

OR

b Evaluate $\iiint xyz dx dy dz$ taken through the positive octant of the sphere $x^2 + y^2 + z^2 = a^2$.

20 a If $\frac{\tan \theta}{\theta} = \frac{2524}{2523}$, show that θ is approximately equal to $1^{\circ} 58'$.

OR

b If $\cosh u = \sec \theta$, then show that $u = \log \tan \left(\frac{\pi}{4} + \frac{\theta}{2} \right)$.