

PSG COLLEGE OF ARTS & SCIENCE
(AUTONOMOUS)

BSc DEGREE EXAMINATION MAY 2022
(Fourth Semester)

Branch - MATHEMATICS

MECHANICS-II(DYNAMICS)

Time: Three Hours

Maximum: 75 Marks

SECTION-A (10 Marks)

Answer ALL questions
ALL questions carry EQUAL marks (10 x 1 = 10)

- 1 When the velocity \vec{v} in terms of its components in two _____ directions.
(i) Parallel (ii) equal
(iii) Perpendicular (iv) not equal
- 2 If \vec{v}_1 and \vec{v}_2 are of equal magnitude, say v then _____.
(i) $2v \cos \frac{\alpha}{2}$ (ii) $2v \cos \frac{\alpha}{2}$
(iii) $2v^2 \cos \frac{\alpha}{2}$ (iv) $2v^2 \cos \frac{\alpha}{2}$
- 3 If m is the mass of the particle and \vec{v} its velocity then $m\vec{v}$ is called the _____.
(i) Linear momentum (ii) Linear
(iii) motions (iv) force
- 4 _____ is a force which comes into play when an elastic body is the deformed by application of forces.
(i) Tension (ii) Hooke's law
(iii) Reaction (iv) Poundal
- 5 State the Hooke's law _____.
(i) $T = \lambda \frac{x-a}{a}$ (ii) $T = \lambda \frac{x+a}{a}$
(iii) $T = \lambda \frac{x-b}{b}$ (iv) $T = \lambda \frac{x+b}{b}$
- 6 _____ is the joule of work done by 1 newton in moving the particle through 1 metre.
(i) Joule (ii) work
(iii) metre (iv) dyre
- 7 When $m\vec{v}$ is a constant vector, that is the linear momentum is conserved. Thus we obtain this called _____.
(i) Principle of conservation momentum (ii) momentum
(iii) work (iv) Joule
- 8 When the explosive charge in a gun forms a large _____.
(i) amount of gas (ii) moment
(iii) Particle (iv) amount

Cont...

- 9 The maximum distance through which the particle moves on either side of mean position is called
- (i) Amplitude (ii) Range
(iii) Vibration (iv) Epoch
- 10 The number of oscillations per second is called _____.
- (i) frequency (ii) phase and epoch
(iii) motions (iv) amplitude

SECTION - B (25 Marks)

Answer ALL questions

ALL questions carry EQUAL Marks

(5 x 5 = 25)

- 11 a If a point moves in a straight line with uniform acceleration and covers successive equal distance in times t_1, t_2, t_3 then show that
- $$\frac{1}{t_1} + \frac{2}{t_2} + \frac{3}{t_3} = \frac{3}{t_1 + t_2 + t_3}$$

OR

- b Calculate A train moving at 30m/ sec reduces to speed to 10m/sec in a distance 240m . At what distance will the train come to stop. If the brake power increased $12\frac{1}{2}$ % show that the train will stop in a total distance of 240 m.

- 12 a Explain Newton's second law motion.

OR

- b Describe the magnitude and direction of the resultant force \vec{F}_1 and \vec{F}_2 .

- 13 a Show that when a particle is subject to the action of conservative forces, the increase in k.E in an interval is equal to the work done in that interval.

OR

- b Prove that A body is projected along a rough inclined plane straight up with Kinetic energy E show that the work done friction before the body comes to rest

$$\frac{E\mu\cos^2}{\sin^2 + \mu\cos^2}$$

- 14 a Explain Newton's experimental law.

OR

- b When two smooth spheres collide directly to find the impulse to each sphere and the change in the total Kinetic energy of the spheres .

- 15 a Show that the resultant motion of two simple harmonic motions of the same period along perpendicular line is an ellipse.

OR

- b Calculate a particle is moving with S.H.M moving from mean position to one extreme position at three consecutive seconds x_1, x_2, x_3 showing its period is

$$2\pi / \cos^{-1} \left\{ \frac{(x_1 + x_3) / 2x_2}{2} \right\}$$

SECTION - C (40 Marks)

Answer ALL questions

ALL questions carry EQUAL Marks

(5 x 8 = 40)

- 16 a Describe the speed of a train increases at a constant rate from v , and then remains constant for an interval and decreases to constant rate β . If s is the total distances

prove index total time T is $T = \frac{s}{v} + \frac{v}{2s} \left(\frac{1}{\alpha} + \frac{1}{\beta} \right)$.

OR

- b Prove that train moves in straight line with uniform acceleration and describe distance a and b is successive intervals of duration t_1 & t_2 . Show that

$$\frac{2(bt_1 - at_2)}{t_1 t_2 (t_1 + t_2)}$$

- 17 a Derive plane of motion a particle interms of radial and transverse components.

OR

- b Discuss the magnitude of the resultant of two given forces P , Q is R . If G is doubled, then R is doubled. If Q is reversed then also R is doubled show that

$$P:Q:R = \sqrt{2}:\sqrt{3}:\sqrt{2}$$

- 18 a Discuss the car of mass 1 tonne attains a maximum speed of 45 km p.h when freely running down as in cline of 1 in 10. what power must engine develop to take incline of 1 in 20 with the same speed both cases the resistance of the same.

OR

- b Explain the principle of conservation of energy.

- 19 a Prove that when two spheres of equal masses m collide directly the velocities of the sphere are interchanged if $e=1$.

OR

- b Explain oblique impact of a smooth sphere on a plane.

- 20 a A particle moves along a circle with uniform speed then show that the motion of projection of a fixed diameter is simple harmonic.

OR

- b Explain two bodies of masses m and m' are attached to the lower end of an elastic string whose upper end is fixed and hang at rest m' falls of show that the distances of m from the upper end and of the string at time t is

$$a + b + c \cos \sqrt{\frac{g}{b}} t.$$

Z-Z-Z

END