

**PSG COLLEGE OF ARTS & SCIENCE
(AUTONOMOUS)**

**BSc DEGREE EXAMINATION MAY 2022
(Second Semester)**

Branch – MATHEMATICS

ANALYTICAL GEOMETRY

Time: Three Hours

Maximum: 50 Marks

SECTION-A (5 Marks)

Answer ALL questions

ALL questions carry EQUAL marks

One question from each unit (with four choices) (5 x 1 = 5)

1 The directrix of the conic $\frac{l}{r} = 1 + e \cos(\theta - \alpha)$ corresponding to the focus

$$(i) \frac{l}{r} = 1 + e \cos(\theta + \alpha)$$

$$(ii) \frac{l}{r} = e \cos(\theta - \alpha)$$

$$(iii) \frac{l}{r} = 1 - e \cos(\theta - \alpha)$$

$$(iv) \frac{l}{r} = 1 + e \cos(\theta - \alpha)$$

2 A straight line may be determined as the _____ of two planes.

(i) Union

(ii) sum

(iii) intersection

(iv) complement

3 When $u^2 + v^2 + w^2 - d$ is negative, the locus is an _____

(i) imaginary sphere

(ii) real sphere

(iii) solid sphere

(iv) tangent sphere

4 A right circular cone, the fixed point is called a _____

(i) Line

(ii) Angle

(iii) Axis

(iv) Vertex

5 Any plane which intersects the cylinder whose equation is of second degree is a

(i) Conic

(ii) Cylinder

(iii) Sphere

(iv) Circle

SECTION - B (15 Marks)

Answer ALL Questions

ALL Questions Carry EQUAL Marks

One question from each unit with either or type (5 x 3 = 15)

6 a Trace the curve $\frac{12}{r} = 4 + \sqrt{3}(\cos \theta + 3 \sin \theta)$

OR

b Derive the asymptotes of the conic $\frac{l}{r} = 1 + e \cos \theta$

7 a Find the image of the point (1, -2, 3) in the plane $2x - 3y + 2z + 3 = 0$

OR

b Find the shortest distance between the lines

$$\frac{x-3}{-1} = \frac{y-4}{2} = \frac{z+2}{1} = \frac{x-1}{1} = \frac{y+7}{3} = \frac{z+2}{2}$$

8 a Find the co-ordinates of the centre and radius of the sphere

$$2x^2 + 2y^2 + 2z^2 - 2x + 4y + 2z - 15 = 0$$

OR

Cont...

- b Find the equation of the sphere having the circle
 $x^2 + y^2 + z^2 - 2x + 4y - 6z + 7 = 0, 2x - y + 2z = 5$ for a great circle.
- 9 a Show that the plane $2x - y - 2z = 16$ touches the sphere
 $x^2 + y^2 + z^2 - 4x + 2y + 2z - 3 = 0$ and find the point of contact.
OR
b Show that the equation of a right circular cone whose vertex is O, axis OZ and semi-vertical angle α is $x^2 + y^2 = z^2 \tan^2 \alpha$
- 10 a Derive the equation of the cylinder whose generators are parallel to the line
 $\frac{x}{l} = \frac{y}{m} = \frac{z}{n}$ and whose guiding curve is $f(x, y, z) = 0, ax + by + cz + d = 0$
OR
b Find the equation of the cylinder whose generators are parallel to the z-axis and the guiding curve is $ax^2 + by^2 = cz, lx + my + nz = p$

SECTION -C (30 Marks)

Answer ALL questions

ALL questions carry EQUAL Marks

One question from each unit with either or type (5 x 6 = 30)

- 11 a Trace the curve $\frac{10}{r} = 3\cos\theta + 4\sin\theta + 5$
OR
b A chord PQ of a conic subtends an angle of 2β of constant magnitude at the pole. Find the locus of the intersection of the tangents at P and Q.
- 12 a Find the symmetrical form of the equations of the line of intersection of the planes $x + 5y - z - 7 = 0, 2x - 5y + 3z + 1 = 0$
OR
b Prove that the lines $\frac{x+1}{-3} = \frac{y+10}{8} = \frac{z-1}{2} = \frac{x+3}{-4} = \frac{y+1}{7} = \frac{z-4}{1}$ are coplanar.
Find also their point of intersection and the plane through them.
- 13 a Find the equation to the sphere through the four points (2,3,1), (5,-1,2), (4,3,-1) and (2,5,3)
OR
b Find the equation of the sphere which touches $x^2 + y^2 + z^2 - 6x + 2z + 1 = 0$ at the point (2,-2,1) and passes through the origin.
- 14 a Derive the condition for the equation
 $F(x, y, z) = ax^2 + by^2 + cz^2 + 2fyz + 2gzx + 2hxy + 2ux + 2vy + 2wz + d = 0$
to represent a cone.
OR
b Find the conditions of the tangent planes to the cone $9x^2 - 4y^2 + 16z^2 = 0$
which contains the line $\frac{x}{32} = \frac{y}{72} = \frac{z}{27}$
- 15 a Derive the equation of the right circular cylinder with axis $\frac{x-\alpha}{l} = \frac{y-\beta}{m} = \frac{z-\gamma}{n}$ and radius of the guiding circle λ .
b Find the equation of a right circular cylinder of radius 3 with axis
 $\frac{x+2}{3} = \frac{y-4}{6} = \frac{z-1}{2}$