

**PSG COLLEGE OF ARTS & SCIENCE**  
(AUTONOMOUS)

**BSc DEGREE EXAMINATION MAY 2026**  
(Sixth Semester)

Branch – MATHEMATICS

**NUMERICAL METHODS WITH R PROGRAMMING**

Time: Three Hours

Maximum: 75 Marks

**SECTION-A (10 Marks)**

Answer ALL questions

ALL questions carry EQUAL marks

(10 × 1 = 10)

| Module No. | Question No. | Question                                                                                                                                                                                             | K Level | CO  |
|------------|--------------|------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|---------|-----|
| 1          | 1            | In Gauss Elimination method, the coefficient matrix is reduced to<br>(i) Diagonal form<br>(ii) Lower triangular form<br>(iii) Identity matrix<br>(iv) Upper triangular form                          | K1      | CO1 |
|            | 2            | The Gauss–Jacobi method is an example of _____.<br>(i) Direct method (ii) Iterative method<br>(iii) Exact method (iv) Graphical method                                                               | K2      | CO1 |
| 2          | 3            | Newton’s forward difference formula is mainly used when the required value is near to _____.<br>(i) End of the table (ii) Middle of the Table<br>(iii) Beginning of the table (iv) Ende of the Table | K1      | CO2 |
|            | 4            | Simpson’s one-third rule requires the number of subintervals to be _____.<br>(i) Odd (ii) Even (iii) Prime (iv) Zero                                                                                 | K2      | CO2 |
| 3          | 5            | The Taylor’s series method for solving ODEs requires _____.<br>(i) Only first derivative (ii) No derivative<br>(iii) Higher order derivatives (iv) Integration only                                  | K1      | CO3 |
|            | 6            | The Newton–Raphson method has _____.<br>(i) Linear convergence (ii) Quadratic convergence<br>(iii) No convergence (iv) Cubic convergence                                                             | K2      | CO3 |
| 4          | 7            | In R, the assignment operator is _____.<br>(i) = (ii) <- (iii) == (iv) :=                                                                                                                            | K1      | CO4 |
|            | 8            | A system of linear algebraic equations can be written in matrix form as _____.<br>(i) $AX = B$ (ii) $A + X = B$<br>(iii) $A - X = B$ (iv) $A/B = X$                                                  | K2      | CO4 |
| 5          | 9            | Which R function is used to perform numerical integration?<br>(i) diff() (ii) integrate()<br>(iii) deriv() (iv) quad()                                                                               | K1      | CO5 |
|            | 10           | The pracma package provides functions for _____.<br>(i) Only integration<br>(ii) Only differentiation<br>(iii) Numerical mathematics routines<br>(iv) Data frames                                    | K2      | CO5 |

Cont...

**SECTION - B (35 Marks)**Answer **ALL** questions**ALL** questions carry **EQUAL** Marks

(5 × 7 = 35)

| Module No. | Question No. | Question                                                                                                                      | K Level | CO  |
|------------|--------------|-------------------------------------------------------------------------------------------------------------------------------|---------|-----|
| 1          | 11.a.        | Describe the Gauss–Jordan Elimination Method and highlight the difference between Gauss Elimination and Gauss–Jordan methods. | K2      | CO1 |
|            |              | (OR)                                                                                                                          |         |     |
|            | 11.b.        | Explain the algorithm for the Gauss–Seidel method and compare it with Gauss–Jacobi method.                                    |         |     |
| 2          | 12.a.        | Derive Newton’s forward difference formula for the first derivative.                                                          | K1      | CO2 |
|            |              | (OR)                                                                                                                          |         |     |
|            | 12.b.        | State and derive the Trapezoidal rule for numerical integration.                                                              |         |     |
| 3          | 13.a.        | Using Taylor’s series method, find $y(0.1)$ correct to four decimal places, given $dy/dx = x+y, y(0)=1$ .                     | K3      | CO3 |
|            |              | (OR)                                                                                                                          |         |     |
|            | 13.b.        | Use the Bisection method to find a real root of $x^3 - x - 1 = 0$ correct to three decimal places.                            |         |     |
| 4          | 14.a.        | Explicate relational operators in R. Write an R program demonstrating Comparison of two numbers.                              | K4      | CO4 |
|            |              | (OR)                                                                                                                          |         |     |
|            | 14.b.        | Find the zeros of the polynomial $x^4 - 5x^2 + 4 = 0$ using an appropriate numerical method.                                  |         |     |
| 5          | 15.a.        | Describe the use of the numDeriv package for computing gradients and Hessians.                                                | K4      | CO5 |
|            |              | (OR)                                                                                                                          |         |     |
|            | 15.b.        | Discuss the integrate() function in R with syntax and example.                                                                |         |     |

**SECTION -C (30 Marks)**Answer **ANY THREE** questions**ALL** questions carry **EQUAL** Marks

(3 × 10 = 30)

| Module No. | Question No. | Question                                                                                                                                    | K Level | CO  |
|------------|--------------|---------------------------------------------------------------------------------------------------------------------------------------------|---------|-----|
| 1          | 16           | Solve the following system of equations using Gauss Elimination Method.<br>$2x + y - z = 82$<br>$-3x - y + 2z = -11$<br>$-2x + y + 2z = -3$ | K2      | CO1 |
| 2          | 17           | Evaluate $\int_0^6 (x^3 + 1) dx$ using Simpson’s One-Third Rule with $h = 1$ .                                                              | K2      | CO2 |
| 3          | 18           | Using the fourth-order Runge–Kutta method, compute $y(0.2)$ with step size $h = 0.1$ , given $dy/dx = x + y, y(0) = 1$ .                    | K3      | CO3 |
| 4          | 19           | Discuss the role of numerical methods in solving real-world problems. Explain how R tools assist in implementing numerical algorithms.      | K4      | CO4 |
| 5          | 20           | Write an R program to compute numerical differentiation of a function using base R and compare it with analytical derivative.               | K5      | CO5 |

Z-Z-Z

END