

PSG COLLEGE OF ARTS & SCIENCE
(AUTONOMOUS)

BCom DEGREE EXAMINATION MAY 2026
(Second Semester)

Branch – COMMERCE (BUSINESS ANALYTICS)

OPTIMIZATION TECHNIQUES FOR BUSINESS ANALYTICS

Time: Three Hours

Maximum: 75 Marks

SECTION-A (10 Marks)

Answer ALL questions

ALL questions carry EQUAL marks (10 × 1 = 10)

Module No.	Question No.	Question	K Level	CO
1	1	A factory produces two products A and B. Profit per unit of is Rs.5 and B is Rs. 3 which of the following function represents the objective function i) Maximize $Z = 5A + 3B$ ii) Minimize $Z = 5A - 3B$ iii) Maximize $Z = A + B$ iv) Minimize $Z = 5 + 3$	K1	CO1
	2	Slack variable is added to i) $\geq$ constraint ii) $\leq$ constraint iii) = constraint iv) Objective function	K2	CO1
2	3	A transportation problem aims at i) Maximizing profit ii) Minimizing transportation cost iii) Maximizing production iv) Allocating jobs	K1	CO2
	4	Assignment problem is a special case of i) LPP ii) Transportation problem iii) Sequencing problem iv) Game theory	K2	CO2
3	5	A zero-sum game means i) Total gain equals total loss ii) No loss situation iii) Random outcome iv) All players win	K2	CO3
	6	Saddle point exists when i) Maximin = Minimax ii) Maximin $\neq$ Minimax iii) No solution iv) Mixed strategy	K1	CO3
4	7	Critical path is i) Longest Path ii) Shortest Path iii) Medium Path iv) Optional Path	K1	CO4
	8	Expected time in PERT is i) $(a+m+b)/3$ ii) $(a+4m+b)/6$ iii) $(a+b)/2$ iv) m only	K2	CO4
5	9	Sequencing objective is to i) Maximize idle time ii) Minimize total elapsed time iii) Increase jobs iv) Reduce machines	K2	CO5
	10	Idle time is i) Working Time ii) Waiting Time ii) Completion Time iv) Total Time	K2	CO5

Cont...

SECTION - B (35 Marks)Answer **ALL** questions**ALL** questions carry **EQUAL** Marks

(5 × 7 = 35)

Module No.	Question No.	Question	K Level	CO																						
1	11.a.	Formulate the mathematical model of LPP and convert the following into standard form and solve graphically: Max $Z = 5x + 3y$ $3x + 2y \leq 18$ $x + y \leq 8$	K2	CO1																						
	(OR)																									
	11.b.	Explain the steps involved in formulating an LPP.																								
2	12.a.	Solve the following transportation problem <table border="1"><tr><td></td><td>D1</td><td>D2</td><td>D3</td><td>Supply</td></tr><tr><td>S1</td><td>6</td><td>4</td><td>1</td><td>50</td></tr><tr><td>S2</td><td>3</td><td>8</td><td>7</td><td>40</td></tr><tr><td>Demand</td><td>30</td><td>30</td><td>30</td><td></td></tr></table>		D1	D2	D3	Supply	S1	6	4	1	50	S2	3	8	7	40	Demand	30	30	30		K3	CO2		
		D1	D2	D3	Supply																					
	S1	6	4	1	50																					
S2	3	8	7	40																						
Demand	30	30	30																							
(OR)																										
12.b.	Solve the following maximization assignment problem. <table border="1"><tr><td></td><td>S1</td><td>S2</td><td>S3</td><td>S4</td></tr><tr><td>A</td><td>62</td><td>75</td><td>80</td><td>93</td></tr><tr><td>B</td><td>75</td><td>80</td><td>82</td><td>85</td></tr><tr><td>C</td><td>80</td><td>75</td><td>81</td><td>98</td></tr><tr><td>D</td><td>78</td><td>82</td><td>84</td><td>80</td></tr></table>		S1	S2	S3	S4	A	62	75	80	93	B	75	80	82	85	C	80	75	81	98	D	78	82	84	80
	S1	S2	S3	S4																						
A	62	75	80	93																						
B	75	80	82	85																						
C	80	75	81	98																						
D	78	82	84	80																						
3	13.a.	Solve the following 2×4 game using graphical method and find optimal mixed strategies: <table border="1"><tr><td></td><td>B1</td><td>B2</td><td>B3</td><td>B4</td></tr><tr><td>G1</td><td>2</td><td>4</td><td>6</td><td>8</td></tr><tr><td>G2</td><td>7</td><td>5</td><td>3</td><td>1</td></tr></table>		B1	B2	B3	B4	G1	2	4	6	8	G2	7	5	3	1	K3	CO3							
		B1	B2	B3	B4																					
	G1	2	4	6	8																					
G2	7	5	3	1																						
(OR)																										
13.b.	Reduce the following game matrix using dominance rule and then solve the reduced game. <table border="1"><tr><td></td><td>X1</td><td>X2</td><td>X3</td></tr><tr><td>Y1</td><td>1</td><td>7</td><td>2</td></tr><tr><td>Y2</td><td>6</td><td>2</td><td>7</td></tr><tr><td>Y3</td><td>5</td><td>1</td><td>6</td></tr></table>		X1	X2	X3	Y1	1	7	2	Y2	6	2	7	Y3	5	1	6									
	X1	X2	X3																							
Y1	1	7	2																							
Y2	6	2	7																							
Y3	5	1	6																							
4	14.a.	A project consists of the following activities: <table border="1"><tr><th>Activity</th><th>Predecessor</th><th>Duration (Days)</th></tr><tr><td>V</td><td>—</td><td>4</td></tr><tr><td>U</td><td>V</td><td>6</td></tr><tr><td>W</td><td>V</td><td>5</td></tr><tr><td>X</td><td>W</td><td>3</td></tr><tr><td>Y</td><td>X</td><td>4</td></tr><tr><td>Z</td><td>X,Y</td><td>2</td></tr></table> Draw the network diagram and identify Critical Path	Activity	Predecessor	Duration (Days)	V	—	4	U	V	6	W	V	5	X	W	3	Y	X	4	Z	X,Y	2	K3	CO4	
	Activity	Predecessor	Duration (Days)																							
	V	—	4																							
U	V	6																								
W	V	5																								
X	W	3																								
Y	X	4																								
Z	X,Y	2																								
(OR)																										

4	14.b.	Using the following data:																			
		<table><tr><th>Activity</th><th>a</th><th>m</th><th>b</th></tr><tr><td>A</td><td>1</td><td>2</td><td>3</td></tr><tr><td>B</td><td>2</td><td>4</td><td>6</td></tr><tr><td>C</td><td>3</td><td>5</td><td>9</td></tr></table>	Activity	a	m	b	A	1	2	3	B	2	4	6	C	3	5	9			
Activity	a	m	b																		
A	1	2	3																		
B	2	4	6																		
C	3	5	9																		
		Calculate expected duration and variance.																			
5	15.a.	Five jobs are to be processed on two machines MX and MY in the order MX → MY. Processing times (in hours) are:																			
		<table><tr><th>Job</th><th>MX</th><th>MY</th></tr><tr><td>J1</td><td>4</td><td>7</td></tr><tr><td>J2</td><td>6</td><td>3</td></tr><tr><td>J3</td><td>5</td><td>8</td></tr><tr><td>J4</td><td>2</td><td>6</td></tr><tr><td>J5</td><td>9</td><td>5</td></tr></table>	Job	MX	MY	J1	4	7	J2	6	3	J3	5	8	J4	2	6	J5	9	5	
	Job	MX	MY																		
	J1	4	7																		
J2	6	3																			
J3	5	8																			
J4	2	6																			
J5	9	5																			
		Determine Optimal sequence using Johnson's Rule.																			
(OR)																					
15.b.		Five jobs must be processed on two machines in the order MA → MB.																			
		<table><tr><th>Job</th><th>MA</th><th>MB</th></tr><tr><td>J1</td><td>3</td><td>8</td></tr><tr><td>J2</td><td>12</td><td>6</td></tr><tr><td>J3</td><td>5</td><td>4</td></tr><tr><td>J4</td><td>2</td><td>7</td></tr><tr><td>J5</td><td>9</td><td>3</td></tr></table>	Job	MA	MB	J1	3	8	J2	12	6	J3	5	4	J4	2	7	J5	9	3	
Job	MA	MB																			
J1	3	8																			
J2	12	6																			
J3	5	4																			
J4	2	7																			
J5	9	3																			
		Determine optimal sequence and Idle time of machines.																			

SECTION -C (30 Marks)

Answer ANY THREE questions

ALL questions carry EQUAL Marks (3 × 10 = 30)

Module No.	Question No.	Question	K Level	CO																									
1	16	Solve the following LPP using the graphical method and find the optimum solution: Maximize $Z = 4x + 6y$ Subject to Constraint $x + y \leq 8$ $2x + y \leq 10$ $x + 3y \leq 15$ $x, y \geq 0$	K2	CO1																									
2	17	Solve the following transportation problem using MODI's Method <table><tr><td></td><td>D1</td><td>D2</td><td>D3</td><td>Supply</td></tr><tr><td>S1</td><td>8</td><td>6</td><td>10</td><td>70</td></tr><tr><td>S2</td><td>9</td><td>7</td><td>4</td><td>50</td></tr><tr><td>S3</td><td>3</td><td>4</td><td>2</td><td>30</td></tr><tr><td>Demand</td><td>40</td><td>60</td><td>50</td><td></td></tr></table>		D1	D2	D3	Supply	S1	8	6	10	70	S2	9	7	4	50	S3	3	4	2	30	Demand	40	60	50		K3	CO2
	D1	D2	D3	Supply																									
S1	8	6	10	70																									
S2	9	7	4	50																									
S3	3	4	2	30																									
Demand	40	60	50																										
3	18	Solve the following 2×3 game graphically and determine the value of the game. <table><tr><td></td><td>B1</td><td>B2</td><td>B3</td></tr><tr><td>A1</td><td>1</td><td>4</td><td>2</td></tr><tr><td>A2</td><td>3</td><td>2</td><td>5</td></tr></table>		B1	B2	B3	A1	1	4	2	A2	3	2	5	K2	CO3													
	B1	B2	B3																										
A1	1	4	2																										
A2	3	2	5																										

Cont...

4	19	Draw the network and determine: Critical Path ii)Project Duration	i)	K3	CO4																												
		<table><tr><th>Activity</th><th>Predecessor</th><th>Duration</th></tr><tr><td>A</td><td>—</td><td>2</td></tr><tr><td>B</td><td>—</td><td>4</td></tr><tr><td>C</td><td>A</td><td>3</td></tr><tr><td>D</td><td>A</td><td>5</td></tr><tr><td>E</td><td>B</td><td>6</td></tr><tr><td>F</td><td>C, D</td><td>4</td></tr><tr><td>G</td><td>E</td><td>3</td></tr><tr><td>H</td><td>F, G</td><td>5</td></tr></table>				Activity	Predecessor	Duration	A	—	2	B	—	4	C	A	3	D	A	5	E	B	6	F	C, D	4	G	E	3	H	F, G	5	
		Activity				Predecessor	Duration																										
		A				—	2																										
		B				—	4																										
		C				A	3																										
		D				A	5																										
		E				B	6																										
		F				C, D	4																										
G	E	3																															
H	F, G	5																															
5	20	A workshop has 6 jobs to process on three machines. Processing times are:		K3	CO5																												
		<table><tr><th>Job</th><th>Machine 1</th><th>Machine 2</th><th>Machine 3</th></tr><tr><td>J1</td><td>5</td><td>3</td><td>6</td></tr><tr><td>J2</td><td>6</td><td>4</td><td>5</td></tr><tr><td>J3</td><td>4</td><td>5</td><td>7</td></tr><tr><td>J4</td><td>7</td><td>6</td><td>4</td></tr><tr><td>J5</td><td>3</td><td>4</td><td>6</td></tr><tr><td>J6</td><td>5</td><td>7</td><td>5</td></tr></table>				Job	Machine 1	Machine 2	Machine 3	J1	5	3	6	J2	6	4	5	J3	4	5	7	J4	7	6	4	J5	3	4	6	J6	5	7	5
		Job				Machine 1	Machine 2	Machine 3																									
		J1				5	3	6																									
		J2				6	4	5																									
		J3				4	5	7																									
		J4				7	6	4																									
J5	3	4	6																														
J6	5	7	5																														
Find optimal schedule and minimum elapsed time.																																	

Z-Z-Z

END