

**PSG COLLEGE OF ARTS & SCIENCE  
(AUTONOMOUS)**

**BSc DEGREE EXAMINATION DECEMBER 2025  
(Second Semester)**

Branch - STATISTICS

**NUMERICAL METHODS**

Time: Three Hours

Maximum: 75 Marks

**SECTION-A (10 Marks)**

Answer ALL questions

ALL questions carry EQUAL marks (10 × 1 = 10)

Module No.	Question No.	Question	K Level	CO
1	1	The order of convergence of the Newton-Raphson method is _____ a) Linear                                      b) Quadratic c) Cubic                                        d) Exponential	K1	CO1
	2	The main advantage of Horner's method in numerical computation is _____ a) Reduces number of multiplications and additions b) Increases degree of polynomial c) Avoids derivatives d) Provides exact roots	K2	CO1
2	3	The relation between the operators E and $\Delta$ is _____ a) $\Delta = E - 1$ b) $\Delta = E + 1$ c) $\Delta = E^2 - 1$ d) $\Delta = E^{-1} - 1$	K1	CO2
	4	Which interpolation formula is best if values of x are not equally spaced? a) Newton's forward formula b) Newton's backward formula c) Newton's divided difference formula d) None of the above	K2	CO2
3	5	Everett's formula is commonly used for _____ a) Odd number of data points b) Even number of data points c) Single missing values only d) Unequal intervals	K1	CO3
	6	In central difference interpolation, the step size h must be _____ a) Unequal                                      b) Constant c) Decreasing                                      d) Increasing	K2	CO3
4	7	The second derivative of a function can be approximated using _____ a) Forward difference only b) Central difference formula c) Simpson's rule d) Trapezoidal rule	K1	CO4
	8	The error in Trapezoidal rule is proportional to _____ a) $h^2$ b) $h^4$ c) $h^3$ d) h	K2	CO4
5	9	Runge-Kutta 2nd order method is also called _____ a) Heun's method                                      b) Milne's method c) Euler-Cauchy method      d) Adams-Bashforth method	K1	CO5
	10	Milne's method uses previous points to _____ a) Reduce truncation error      b) Compute step size c) Solve algebraic equations      d) Interpolate the solution	K2	CO5

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**SECTION - B (35 Marks)**

Answer ALL questions

ALL questions carry EQUAL Marks (5 × 7 = 35)

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Module No.	Question No.	Question	K Level	CO												
1	11.a.	Explain the procedure of Newton Raphson Method.	K2	CO1												
	(OR)															
	11.b.	Solve the equation $x^3+x-1=0$ using the Iteration Method. Rearrange the equation suitably and find the root correct to 4 decimal places. Start with an initial guess $x_0=0.5$ .														
2	12.a.	Construct the properties of forward difference operator.	K3	CO2												
	(OR)															
	12.b.	Solve the $f(0.15)$ using Newton backward difference table from the data. <table><tr><td>X</td><td>0.1</td><td>0.2</td><td>0.3</td><td>0.4</td><td>0.5</td></tr><tr><td>F(X)</td><td>0.09983</td><td>0.19867</td><td>0.29552</td><td>0.38942</td><td>0.47943</td></tr></table>			X	0.1	0.2	0.3	0.4	0.5	F(X)	0.09983	0.19867	0.29552	0.38942	0.47943
X	0.1	0.2	0.3	0.4	0.5											
F(X)	0.09983	0.19867	0.29552	0.38942	0.47943											
3	13.a.	Using Newton's forward interpolation formula, find the polynomial $f(x)$ satisfying the following data. Hence evaluate $y$ at $x = 1985$ <table><tr><td>X</td><td>1981</td><td>1901</td><td>1911</td><td>1921</td><td>1931</td></tr><tr><td>F(X)</td><td>46</td><td>66</td><td>81</td><td>93</td><td>101</td></tr></table>	X	1981	1901	1911	1921	1931	F(X)	46	66	81	93	101	K3	CO3
	X	1981	1901	1911	1921	1931										
	F(X)	46	66	81	93	101										
(OR)																
13.b.	Explain the Lagrange Interpolation formula for unequal.															
4	14.a.	Apply Newton's forward differentiation method to find solution <table><tr><td>X</td><td>0.1</td><td>0.2</td><td>0.3</td><td>0.4</td><td>0.5</td></tr><tr><td>F(X)</td><td>1</td><td>0.9975</td><td>0.99</td><td>0.9776</td><td>0.860</td></tr></table>	X	0.1	0.2	0.3	0.4	0.5	F(X)	1	0.9975	0.99	0.9776	0.860	K3	CO4
	X	0.1	0.2	0.3	0.4	0.5										
	F(X)	1	0.9975	0.99	0.9776	0.860										
(OR)																
14.b.	Explain the Trapeziodal rule.															
5	15.a.	Explain the Euler's method with example.	K2	CO5												
	(OR)															
	15.b.	Use Milne's Predictor-Corrector method with step size $h=0.1$ to estimate $y_4$ for $\frac{dy}{dx} = x + y$ , following data. <table><tr><td>x</td><td>0.0</td><td>0.1</td><td>0.2</td><td>0.3</td></tr><tr><td>y</td><td>1.0</td><td>1.11</td><td>1.26</td><td>1.43</td></tr></table> Interpret $y$ at $x=0.4$			x	0.0	0.1	0.2	0.3	y	1.0	1.11	1.26	1.43		
x	0.0	0.1	0.2	0.3												
y	1.0	1.11	1.26	1.43												

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**SECTION -C (30 Marks)**

Answer ANY THREE questions

ALL questions carry EQUAL Marks (3 × 10 = 30)

ALL questions carry EQUAL Marks (5 x 10 = 50)

Module No.	Question No.	Question	K Level	CO												
1	16	Identify the root of an equation $f(x)=x^3-x-1$ using False Position method.	K3	CO1												
2	17	Explain briefly the forward difference operator and its properties.	K2	CO2												
3	18	Apply the Lagrange's interpolation formula and calculate the profit in the 2000 year from the following data <table border="1" style="margin-left: auto; margin-right: auto;"> <tr> <td>Year</td> <td>1997</td> <td>1999</td> <td>2001</td> <td>2002</td> </tr> <tr> <td>Profit in Lakhs</td> <td>43</td> <td>65</td> <td>159</td> <td>248</td> </tr> </table>	Year	1997	1999	2001	2002	Profit in Lakhs	43	65	159	248	K3	CO3		
Year	1997	1999	2001	2002												
Profit in Lakhs	43	65	159	248												
4	19	Apply Simpson's $3/8^{\text{th}}$ rule from the following data. <table border="1" style="margin-left: auto; margin-right: auto;"> <tr> <td>X</td> <td>1.4</td> <td>1.6</td> <td>1.8</td> <td>2</td> <td>2.2</td> </tr> <tr> <td>F(X)</td> <td>4.0552</td> <td>4.953</td> <td>6.0436</td> <td>7.3891</td> <td>9.025</td> </tr> </table>	X	1.4	1.6	1.8	2	2.2	F(X)	4.0552	4.953	6.0436	7.3891	9.025	K3	CO4
X	1.4	1.6	1.8	2	2.2											
F(X)	4.0552	4.953	6.0436	7.3891	9.025											
5	20	Explain the 4th order Runge-Kutta method with step size $h=0.1$ to find approximate values of $y$ at $x=0.1$ and $x=0.2$ for the differential equation $\frac{dy}{dx} = x + y$ with initial condition $y(0)=1$ .	K2	CO5												

Z-Z-Z END

