

## **PSG COLLEGE OF ARTS & SCIENCE (AUTONOMOUS)**

**BSc DEGREE EXAMINATION DECEMBER 2025**  
**(Fifth Semester)**

## Branch – STATISTICS

## **OPERATIONS RESEARCH**

Time: Three Hours

Maximum: 75 Marks

**SECTION-A (10 Marks)**

**Answer ALL questions**

**ALL** questions carry **EQUAL** marks.

$$(10 \times 1 = 10)$$

**Cont...**

5	9	The main objective of network analysis is to a) Minimize total cost b) Minimize total project time c) Ensure project completion on time and within budget d) Increase project complexity	K1	CO5
	10	PERT differs from CPM because PERT a) Considers time-cost trade-off b) Uses probabilistic time estimates c) Is used for repetitive works d) Ignores uncertainty	K2	CO5

**SECTION - B (35 Marks)**

Answer ALL questions

ALL questions carry EQUAL Marks

 $(5 \times 7 = 35)$ 

Module No.	Question No.	Question	K Level	CO																											
1	11.a.	A small factory makes three items: Study Tables, Chairs and Stools. Profit per unit is ₹1200 for a Table, ₹450 for a Chair and ₹200 for a Stool. Each Table requires 6 hours of carpentry and 3 hours of polishing; each Chair requires 3 hours of carpentry and 2 hours of polishing; each Stool requires 1 hour of carpentry and 1 hour of polishing. The factory has at most 300 carpentry hours and 160 polishing hours per week. Market demand limits production to at most 30 Tables per week. Formulate an LPP to maximize weekly profit.	K2	CO1																											
	11.b.	(OR) Explain about the graphical method of solving LPP.																													
2	12.a.	Define: i) Transportation problem ii) Feasible Solution iii) Degeneracy	K3	CO2																											
	12.b.	(OR) <table border="1"> <tr> <th>From \ To</th> <th>D1</th> <th>D2</th> <th>D3</th> <th>D4</th> <th>Supply</th> </tr> <tr> <td>S1</td> <td>8</td> <td>6</td> <td>10</td> <td>9</td> <td>120</td> </tr> <tr> <td>S2</td> <td>9</td> <td>12</td> <td>13</td> <td>7</td> <td>200</td> </tr> <tr> <td>S3</td> <td>14</td> <td>9</td> <td>16</td> <td>5</td> <td>160</td> </tr> <tr> <td>Demand</td> <td>100</td> <td>150</td> <td>120</td> <td>110</td> <td></td> </tr> </table> <p>Solve the above transportation problem by VAM method.</p>			From \ To	D1	D2	D3	D4	Supply	S1	8	6	10	9	120	S2	9	12	13	7	200	S3	14	9	16	5	160	Demand	100	150
From \ To	D1	D2	D3	D4	Supply																										
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Demand	100	150	120	110																											
3	13.a.	Explain the sequential problem of $n$ jobs 3 machines.	K3	CO3																											
	13.b.	(OR) Solve the following assignment problem by Hungarian method. <table border="1"> <tr> <td></td> <td>J1</td> <td>J2</td> <td>J3</td> <td>J4</td> <td></td> </tr> <tr> <td>W1</td> <td>82</td> <td>83</td> <td>69</td> <td>92</td> <td></td> </tr> <tr> <td>W2</td> <td>77</td> <td>37</td> <td>49</td> <td>92</td> <td></td> </tr> <tr> <td>W3</td> <td>11</td> <td>69</td> <td>5</td> <td>86</td> <td></td> </tr> <tr> <td>W4</td> <td>8</td> <td>9</td> <td>98</td> <td>23</td> <td></td> </tr> </table>				J1	J2	J3	J4		W1	82	83	69	92		W2	77	37	49	92		W3	11	69	5	86		W4	8	9
	J1	J2	J3	J4																											
W1	82	83	69	92																											
W2	77	37	49	92																											
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W4	8	9	98	23																											
4	14.a.	Payoff matrix (A's payoffs): <table border="1"> <tr> <td></td> <td>Column 1</td> <td>Column 2</td> </tr> <tr> <td>Row 1</td> <td>4</td> <td>2</td> </tr> <tr> <td>Row 2</td> <td>1</td> <td>3</td> </tr> </table> <p>Find optimal mixed strategies and the value.</p>		Column 1	Column 2	Row 1	4	2	Row 2	1	3	K2	CO4																		
	Column 1	Column 2																													
Row 1	4	2																													
Row 2	1	3																													
14.b.	(OR) Describe dominance property and modified dominance property.																														

Cont...

	15.a.	Explain the phases of project management.							
		(OR)							
5	15.b.	A project has the following time schedule:							
		Activity	1-2	1-3	1-4	2-5	3-6	3-7	
		Time in Weeks	2	2	1	4	8	5	
		Activity	4-6	5-8	6-9	7-8	8-9		
		Time in Weeks	3	1	5	4	3		
		Construct PERT network and compute							
		i) Total float for each activity							
		ii) Critical path and its duration.							

**SECTION -C (30 Marks)**

Answer ANY THREE questions

ALL questions carry EQUAL Marks

 $(3 \times 10 = 30)$ 

Module No.	Question No.	Question	K Level	CO																									
1	16	Solve by big-M method: Maximise $Z=3X_1 + 2X_2$ subject to $X_1 + X_2 \leq 4$ , $X_1 + 2X_2 \geq 2$ , and $X_1, X_2 \geq 0$ .	K3	CO1																									
2	17	A manufacturer has 3 warehouses (W1, W2, W3) with a stock of 30, 25, and 35 units respectively. These are to be supplied to 4 retail shops (R1, R2, R3, R4) with requirements of 20, 25, 15, and 30 units respectively. The transportation costs are as follows:  <table border="1" style="display: inline-table; vertical-align: middle;"><tr><td></td><td>R1</td><td>R2</td><td>R3</td><td>R4</td></tr><tr><td>W1</td><td>6</td><td>4</td><td>8</td><td>13</td></tr><tr><td>W2</td><td>4</td><td>5</td><td>6</td><td>8</td></tr><tr><td>W3</td><td>8</td><td>10</td><td>6</td><td>7</td></tr></table> Determine the optimal cost using the MODI method.		R1	R2	R3	R4	W1	6	4	8	13	W2	4	5	6	8	W3	8	10	6	7	K3	CO2					
	R1	R2	R3	R4																									
W1	6	4	8	13																									
W2	4	5	6	8																									
W3	8	10	6	7																									
3	18	Write the algorithm for $n$ jobs and $m$ machines in a sequencing problem.	K2	CO3																									
4	19	Solve the following $2 \times 4$ game by graphic method. <table border="1" style="display: inline-table; vertical-align: middle;"><tr><td></td><td>B<sub>1</sub></td><td>B<sub>2</sub></td><td>B<sub>3</sub></td><td>B<sub>4</sub></td></tr><tr><td>A<sub>1</sub></td><td>3</td><td>3</td><td>4</td><td>0</td></tr><tr><td>A<sub>2</sub></td><td>5</td><td>4</td><td>3</td><td>7</td></tr></table>		B <sub>1</sub>	B <sub>2</sub>	B <sub>3</sub>	B <sub>4</sub>	A <sub>1</sub>	3	3	4	0	A <sub>2</sub>	5	4	3	7	K4	CO4										
	B <sub>1</sub>	B <sub>2</sub>	B <sub>3</sub>	B <sub>4</sub>																									
A <sub>1</sub>	3	3	4	0																									
A <sub>2</sub>	5	4	3	7																									
5	20	A project has the following activities and time estimates (in weeks):  <table border="1" style="display: inline-table; vertical-align: middle;"><tr><th>Activity</th><th>Predecessor</th><th><math>t_o</math></th><th><math>t_m</math></th><th><math>t_p</math></th></tr><tr><td>A</td><td>-</td><td>1</td><td>2</td><td>3</td></tr><tr><td>B</td><td>A</td><td>2</td><td>3</td><td>8</td></tr><tr><td>C</td><td>A</td><td>3</td><td>4</td><td>5</td></tr><tr><td>D</td><td>B, C</td><td>4</td><td>6</td><td>10</td></tr></table> (a) Construct the PERT network. (b) Compute the expected project duration and variance. (c) What is the probability that the project will be completed in 12 weeks?	Activity	Predecessor	$t_o$	$t_m$	$t_p$	A	-	1	2	3	B	A	2	3	8	C	A	3	4	5	D	B, C	4	6	10	K4	CO5
Activity	Predecessor	$t_o$	$t_m$	$t_p$																									
A	-	1	2	3																									
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C	A	3	4	5																									
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