

PSG COLLEGE OF ARTS & SCIENCE
(AUTONOMOUS)
MSc DEGREE EXAMINATION MAY 2025
(Second Semester)
Branch - **STATISTICS**

DISTRIBUTION THEORY

Time: Three Hours

Maximum: 75 Marks

SECTION-A (10 Marks)
Answer ALL questions
ALL questions carry EQUAL marks (10 × 1 = 10)

| Module No. | Question No. | Question | K Level | CO |
|------------|--------------|---|---------|-----|
| 1 | 1 | A censored data point is a) A missing data point b) A completely observed value c) A data point known only up to a limit d) An outlier | K1 | CO1 |
| | 2 | The sum of independent Poisson-distributed random variables follows a a) Normal distribution b) Binomial distribution c) Poisson distribution d) Uniform distribution | K2 | CO1 |
| 2 | 3 | The F-distribution is commonly used in a) Hypothesis testing for means b) ANOVA and variance comparisons c) Linear regression d) Confidence interval estimation | K1 | CO2 |
| | 4 | The sample correlation coefficient 'r' ranges between a) 0 and 1 b) -1 and 1 c) $-\infty$ and ∞ d) 0 and ∞ | K1 | CO2 |
| 3 | 5 | A multivariate normal distribution is characterized by a) Mean vector and covariance matrix b) Mean and variance only c) Median and mode d) Probability mass function | K1 | CO3 |
| | 6 | Recall the usage of Mahalanobis distance. a) Measuring distances in correlated data b) Computing Euclidean distance c) Standardizing normal variables d) Testing equality of means | K2 | CO3 |
| 4 | 7 | The Wishart distribution is associated with a) Covariance matrices b) Regression coefficients c) Mean vectors d) Correlation matrices | K1 | CO4 |
| | 8 | The Hotelling's T^2 statistic is an extension of a) The t-test b) The F-test c) The chi-square test d) The Kolmogorov-Smirnov test | K2 | CO4 |
| 5 | 9 | Fisher's discriminant function maximizes a) The separation between groups b) The within-group variance c) The correlation coefficient d) The sample mean | K1 | CO5 |
| | 10 | Identify the significance of Principal Component Analysis. a) Reducing dimensionality b) Testing independence c) Regression analysis d) Time series forecasting | K2 | CO5 |

Cont...

SECTION - B (35 Marks)

Answer ALL questions
ALL questions carry EQUAL Marks

(5 × 7 = 35)

| Module No. | Question No. | Question | K Level | CO |
|------------|--------------|--|---------|-----|
| 1 | 11.a. | Derive the distribution function of Binomial distribution. | K2 | CO1 |
| | (OR) | | | |
| | 11.b. | If X and Y are independent Poisson variates with means λ_1 and λ_2 respectively, find $P(X + Y = K)$. | | |
| 2 | 12.a. | Describe Order Statistics with an example. | K3 | CO2 |
| | (OR) | | | |
| | 12.b. | Write short notes on partial correlation coefficient and regression coefficient. Illustrate. | | |
| 3 | 13.a. | State the properties of Multivariate Normal Density Function. | K3 | CO3 |
| | (OR) | | | |
| | 13.b. | Derive the Characteristics function of Multivariate Normal Distribution. | | |
| 4 | 14.a. | Describe Wishart matrix and its distribution. | K3 | CO4 |
| | (OR) | | | |
| | 14.b. | Explain Mahalanobis distance and its significance. | | |
| 5 | 15.a. | Narrate in detail about Factor Analysis – Illustrate. | K3 | CO5 |
| | (OR) | | | |
| | 15.b. | Summarize Canonical Correlation. | | |

SECTION - C (30 Marks)

Answer ANY THREE questions
ALL questions carry EQUAL Marks

(3 × 10 = 30)

| Module No. | Question No. | Question | K Level | CO |
|------------|--------------|---|---------|-----|
| 1 | 16 | Derive the probability mass function of Binomial distribution truncated at $x = 0, 1$. | K4 | CO1 |
| 2 | 17 | Explain the concept of χ^2 distribution and describe its applications. | K3 | CO2 |
| 3 | 18 | Estimate the mean vector and the covariance matrix of a multivariate normal distribution. | K4 | CO3 |
| 4 | 19 | Derive the distribution of Hotelling's T^2 statistic. | K3 | CO4 |
| 5 | 20 | Write the procedure of finding first and second principal components. | K4 | CO5 |

Z-Z-Z

END