PSG COLLEGE OF ARTS & SCIENCE (AUTONOMOUS)

BSc DEGREE EXAMINATION MAY 2025

(Fifth Semester)

Branch - STATISTICS

OPERATIONS RESEARCH Maximum: 50 Marks Time: Three Hours SECTION-A (5 Marks) Answer ALL questions $(5 \times 1 = 5)$ ALL questions carry EQUAL marks The two - phase simplex method is another method to solve a given _ 1 involving some artificial variables (ii) Assignment problem (i) Transportation problem (iv) Linear programming problem (iii) Both (a) and (b) 2 In Least cost method the allocation is done by selecting (ii) Upper left hand Upper right hand (iii) Middle cell in the transportation table (iv) Cell with lowest cost In assignment problem if number of rows is greater than column then 3 Add dummy row (ii) Add dummy column (iv) Add column with cost 1 (iii) Add row with cost 1 In a game with a saddle point, maximum for player I equals....for Player II 4 (ii) Maximin (iii)Row minima (iv) Column maxima Minimax 5 The path of least float in a project is called...... (iii) Independent path (iv) Total path Free path (ii) Critical path SECTION - B (15 Marks) Answer ALL Questions **ALL** Questions Carry **EQUAL** Marks $(5 \times 3 = 15)$ 6. (a) Solve the following LPP using graphical method: Maximize $z = x_1 + 3x_2$ Subject to the constraints: $3x_1 + 6x_2 \le 8$ $5x_1 + 2x_2 \le 10$ and $x_1, x_2 \ge 0$. (OR) Write the dual of the following linear programming problem: Maximize $Z = 2x_1 + 3x_2 + x_3$ subject to the constriants: $4x_1 + 3x_2 + x_3 = 6$, $x_1 + 2x_2 + 5x_3 = 4$ and $x_1, x_2, x_3 \ge 0$ 7. (a) List out the methods of finding initial basic feasible solution. (OR) (b) Find the initial basic feasible solution using North West Corner rule. Τo Ē D G 17 250 11 13 14 18 14 10 300 16 21 24 13 10 400 225 200 275 250

| 8. | (a) | What is an assignment problem? |
|----|-----|--------------------------------|
|----|-----|--------------------------------|

(OR)

(b) Solve the following Assignment Problem:

| | 1 | 2 | 3 | 4 | 5 |
|--------|----|----|----|-----|----|
| Α | 85 | 75 | 65 | 125 | 75 |
| B C | 90 | 78 | 66 | 132 | 78 |
| С | 75 | 66 | 57 | 114 | 69 |
| D | 80 | 72 | 60 | 120 | 72 |
| E | 76 | 64 | 56 | 112 | 68 |

9. (a) Determine the range of value of p and q that will make the payoff element a22, a saddle point for the game whose payoff matrix is given below:

(b) Explain the term Pay off matrix in game theory

10. (a) What are the Basic Steps in PERT /CPM

(OR)

(b) Describe the rules of construction of network diagram.

SECTION -C (30 Marks)

Answer ALL questions

ALL questions carry EQUAL Marks

 $(5 \times 6 = 30)$

11. (a) Solve the following LPP using Simplex method: Maximize $z = 5x_1+3x_2$

Subject to the constraints:

 $\begin{array}{l}
 x_1 + x_2 \le 2 \\
 5x_1 + 2x_2 \le 10
\end{array}$

 $3x_1 + 8x_2 \le 12$

and $x_1, x_2 \ge 0$.

(OR)

(b) Solve the following LPP using big-M method: Maximize $z = x_1 + 3x_2$

Subject to the constraints:

 $3x_1 + 6x_2 \le 8$

 $5x_1 + 2x_2 \le 10$

and $x_1, x_2 \ge 0$.

12. (a) Solve the following transportation problem:

| | | | 10 | | |
|-------------|----|---|----|----|--------------|
| | | Α | В | C | Availability |
| | I | 6 | 8 | 4 | 14 |
| From | II | 4 | 9 | 8 | 12 |
| | Ш | 1 | 2 | 6 | 5 |
| Requirement | | 6 | 10 | 15 | 31 |
| - | | l | | | (OR) |

(b) Use Vogel's Approximation method to obtain an initial basic feasible solution of the transportation problem.

| | D ₁ | D_2 | D_3 | D_4 | Supply |
|----------------|----------------|-------|-------|-------|--------|
| S_1 | 20 | 25 | 28 | 31 | 200 |
| S ₂ | 32 | 28 | 32 | 41 | 180 |
| S ₃ | 18 | 35 | 24 | 32 | 110 |
| Demand | 150 | 40 | 180 | 170 | |

13. (a) Write down the Hungarian Algorithm to solve an Assignment problem.

(OR)

(b) Five jobs are offered with expected profit for each machines to the jobs that will result in a maximum profit.

| | _ | Job | | | |
|---------|----|-----|-----|-----|----|
| Machine | Α | В | C | D | E |
| 1 | 62 | 78 | 50 | 111 | 82 |
| 2 | 71 | 84 | 61 | 73 | 59 |
| 3 | 87 | 92 | 111 | 71 | 81 |
| Λ | AΩ | 61 | 97 | 77 | 80 |

14. (a) Solve the following game:

| | | G | Playe | Player B | | |
|----------|-----|------------|-------|----------|------|--|
| | | 1 | II | Ш | ΙV | |
| | I | 「 3 | 2 | 4 | 0 7 | |
| | II | 3 | 4 | 2 | 4 | |
| Player A | III | 4 | 2 | 4 | 0 | |
| - | IV | ١٥ | 4 | 0 | ر 8 | |
| | | | | | (OR) | |

(b) Explain the types of strategy.

15.(a) A project schedule has the following characteristics:

| Activity | 1-2 | 1-3 | 2-4 | 3-4 | 3-5 | 4-9 | 5-6 | 5-7 | 6-8 | 7-8 | 8-10 | 9-10 |
|----------|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|------|------|
| Time | 4 | 1 | 1 | 1 | 6 | 5 | 4 | 8 | 1 | 2 | 5 | 7 |
| (OR) | | | | | | | | | | | | |

(b) Constructthenetworkdiagramforaprojectwiththefollowingactivities:

| Event-Event | Activity | PredecessorActivity |
|-------------|----------|---------------------|
| 1-2 | A | - |
| 1-3 | В | <u> </u> |
| 1-4 | C | |
| 2-5 | D | A |
| 3-6 | E | В |
| 4-6 | F | C. |
| 5-6 | G | D |

Z-Z-Z