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SECTION - B (35 Marks)Answer ALL questions
ALL questions carry EQUAL Marks

(5 × 7 = 35)

Module No.	Question No.	Question	K Level	CO
	11.a	Show that the matrix $\frac{1}{3} \begin{bmatrix} 2 & 2 & 1 \\ -2 & 1 & 2 \\ 1 & -2 & 2 \end{bmatrix}$ is orthogonal.	K3	CO1
		(OR)		
	11.b	Find the Characteristic equation of the matrix $\begin{bmatrix} 2 & -1 & 1 \\ -1 & 2 & -1 \\ 1 & -1 & 2 \end{bmatrix}$ and hence obtain its inverse.		
2	12.a	Prove that $\cos 8\theta = 1 - 32 \sin^2 \theta + 160 \sin^4 \theta - 256 \sin^6 \theta + 128 \sin^8 \theta$.	K4	CO2
		(OR)		
	12.b	Prove that $\cos^5 \theta \sin^4 \theta = \frac{1}{2^8} [\cos 9\theta + \cos 7\theta - 4 \cos 5\theta - 4 \cos 3\theta + 6 \cos \theta]$.		
3	13.a	(i) Derive the reduction formula for $\int \cot^n x \, dx$ (n being a positive integer) (ii) Evaluate $\int \cos^5 x \, dx$ using reduction formula.	K4	CO4
		(OR)		
	13.b	Evaluate $\int x^5 e^{2x} \, dx$.		
4	14.a	Evaluate $\int \int_R (x^2 + y^2) \, dx \, dy$ where R is the region in the positive quadrant for which $x + y \leq 1$.	K3	CO2
		(OR)		
	14.b	Evaluate $\int \int \int_V (x + y + z) \, dx \, dy \, dz$, where the region V is bounded by $x + y + z = a$ ($a > 0$), $x = 0$, $y = 0$, $z = 0$.		
5	15.a	Solve by Gauss-elimination procedure, the equations $3.15x - 1.96y + 3.85z = 12.95$; $2.13x + 5.12y - 2.89z = -8.61$; $5.92x + 3.05y + 2.15z = 6.88$.	K5	CO5
		(OR)		
	15.b	Solve the following equations by Gauss-Jordan method: $2x - 3y + z = -1$; $x + 4y + 5z = 25$; $3x - 4y + z = 2$.		

SECTION - C (30 Marks)Answer ANY THREE questions
ALL questions carry EQUAL Marks

(3 × 10 = 30)

Question No.	Question	K Level	CO
16	Find the eigenvalues and eigenvectors of $\begin{bmatrix} 2 & 2 & 0 \\ 2 & 1 & 1 \\ -7 & 2 & -3 \end{bmatrix}$.	K4	CO1
17	(i) Evaluate $\lim_{\theta \rightarrow 0} \frac{\tan \theta - \sin \theta}{\theta^3}$ (ii) Separate into real and imaginary parts of $\tan(x + iy)$.	K5	CO1
18	Evaluate $\int_0^{\frac{\pi}{2}} \log(\sin x) \, dx$.	K4	CO4
19	Change the order of integration and hence evaluate it $\int_0^{4a} \int_{\frac{x^2}{4a}}^{2\sqrt{ax}} xy \, dy \, dx$.	K4	CO4
20	Solve by Gauss-seidal method of iteration the equations $27x + 6y - z = 85$; $6x + 15y + 2z = 72$; $x + y + 54z = 110$.	K5	CO5