

PSG COLLEGE OF ARTS & SCIENCE
(AUTONOMOUS)

BSc DEGREE EXAMINATION MAY 2025
(Second Semester)

Branch - CHEMISTRY

MATHEMATICS – II FOR CHEMISTRY

Time: Three Hours

Maximum: 75 Marks

SECTION-A (10 Marks)

Answer ALL questions

ALL questions carry EQUAL marks

(10 × 1 = 10)

| Module No. | Question No. | Question | K Level | CO |
|------------|--------------|--|---------|-----|
| 1 | 1 | The Matrix $A = \begin{bmatrix} 2 & -1 & 3 \\ -1 & 4 & 1 \\ 3 & 1 & 5 \end{bmatrix}$ is called as a) Symmetric b) identity c) diagonal d) singular | K1 | CO1 |
| | 2 | Every _____ matrix satisfies its own characteristic equation. a) Symmetric b) identity c) diagonal d) square | K2 | CO1 |
| 2 | 3 | If $x = \cos\theta + i \sin\theta$, What is the value of $\left(x - \frac{1}{x}\right)^n$? a) $(2)^n \cos n\theta$ b) $(2i)^n \sin n\theta$ c) $(2)^n \cos^n \theta$ d) $(2i)^n \sin^n \theta$ | K1 | CO2 |
| | 4 | $7C_1 \cos^{7-1}\theta \sin\theta - 7C_3 \cos^{7-3}\theta \sin^3\theta + 7C_5 \cos^{7-5}\theta \sin^5\theta - 7C_7 \cos^{7-7}\theta \sin^7\theta \dots = \dots$ a) $\cos 7\theta$ b) $\sin 7\theta$ c) $\cos^7 \theta$ d) $\sin^7 \theta$ | K2 | CO2 |
| 3 | 5 | Find the complete solutions of $z = px + qy + p^2q^2$ a) $z = ax + by + a^2b^2$ b) $z = ax + by$ c) $z = ax + ab$ d) $z = by + ab$ | K1 | CO3 |
| | 6 | The form $z = px + qy + f(p,q)$ is called as _____. a) Clairaut's b) Cayley c) De morgans d) Lagranges | K2 | CO3 |
| 4 | 7 | $L(\sin 2t) = \dots$. a) $\frac{2}{s^2+2^2}$ b) $\frac{1}{s-2}$ c) $\frac{1}{s+2}$ d) $\frac{s}{s^2+2^2}$ | K1 | CO4 |
| | 8 | $L^{-1} \left[\frac{1}{s+3} \right] = \dots$. a) e^{-3t} b) e^{3t} c) e^{-t} d) e^t | K2 | CO4 |
| 5 | 9 | In Fourier series, the value of a_n is _____ in $(0, 2\pi)$ a) $\frac{1}{\pi} \int_0^{2\pi} f(x) dx$ b) $\frac{1}{\pi} \int_0^{2\pi} f(x) \sin nx dx$ c) $\frac{1}{\pi} \int_0^{2\pi} f(x) \cos nx dx$ d) $\frac{1}{\pi} \int_0^{\pi} f(x) \cos nx dx$ | K1 | CO5 |
| | 10 | In Fourier series $f(x)$ is even function in the interval $(-\pi, \pi)$ then $b_n = ?$ a) π b) $-\pi$ c) 0 d) 1 | K2 | CO5 |

Cont...

SECTION - B (35 Marks)

Answer ALL questions

ALL questions carry EQUAL Marks

 $(5 \times 7 = 35)$

| Module No. | Question No. | Question | K Level | CO |
|------------|--------------|---|---------|-----|
| 1 | 11.a. | Using Cayley Hamiltonian theorem find the inverse of the matrix $\begin{bmatrix} 7 & 2 & -2 \\ -6 & -1 & 2 \\ 6 & 2 & -1 \end{bmatrix}$ (OR) | K1 | CO1 |
| | 11.b. | Find the eigen values of $A = \begin{bmatrix} 2 & -2 & 3 \\ 1 & 1 & 1 \\ 1 & 3 & -1 \end{bmatrix}$ | K4 | CO1 |
| 2 | 12.a. | Express $\cos 5\theta$ in terms $\cos \theta$. (OR) | K1 | CO2 |
| | 12.b. | Show that $\sin^8 \theta = \frac{1}{2^7} [\cos 8\theta - 8\cos 6\theta + 28\cos 4\theta - 56\cos 2\theta + 35]$ | K6 | CO2 |
| 3 | 13.a. | Form the P.D.E. by eliminating the arbitrary function from $z = f(x^2 + y^2)$. (OR) | K3 | CO3 |
| | 13.b. | Solve $p^2 + q^2 = npq$. | K5 | CO3 |
| 4 | 14.a. | Find $L(\sin^2 t)$. (OR) | K1 | CO4 |
| | 14.b. | Find $L^{-1} \left[\frac{s-3}{s^2+4s+13} \right]$. | K2 | CO4 |
| 5 | 15.a. | Find half range cosine series for $f(x) = x^2$ in $(0, \pi)$. (OR) | K1 | CO5 |
| | 15.b. | Find the Fourier series for $f(x) = x $ in $(-\pi, \pi)$ | K1 | CO5 |

SECTION - C (30 Marks)

Answer ANY THREE questions

ALL questions carry EQUAL Marks

 $(3 \times 10 = 30)$

| Module No. | Question No. | Question | K Level | CO |
|------------|--------------|--|---------|-----|
| 1 | 16 | Find the eigen value and eigen vectors of the matrix $A = \begin{bmatrix} 2 & 2 & 1 \\ 1 & 3 & 1 \\ 1 & 2 & 2 \end{bmatrix}$ | K2 | CO1 |
| 2 | 17 | Show that $\frac{\sin 6\theta}{\sin \theta} = 32\cos^5 \theta - 32\cos^3 \theta + 6\cos 6\theta$. | K3 | CO2 |
| 3 | 18 | Solve $p^2 + q^2 = z^2(x + y)$. | K4 | CO3 |
| 4 | 19 | Find : (i) $L(\sin^2 2t)$ (ii) $L(e^{-at} \cos bt)$. | K5 | CO4 |
| 5 | 20 | Find the Fourier series for $f(x) = \frac{1}{2}(\pi - x)$ in $(0, 2\pi)$. | K5 | CO5 |