

PSG COLLEGE OF ARTS & SCIENCE
(AUTONOMOUS)

MSc(SS) DEGREE EXAMINATION DECEMBER 2023
(Third Semester)

Branch – **SOFTWARE SYSTEMS (Five Year Integrated)**

TRANSFORMATION TECHNIQUES

Time: Three Hours

Maximum: 50 Marks

SECTION-A (5 Marks)

Answer **ALL** questions

ALL questions carry **EQUAL** marks

(5 x 1 = 5)

1. The Laplace transform of 2^t is _____.
 (i) $\frac{1}{s-\log 2}$ (ii) $\frac{1}{s-2}$ (iii) $\frac{1}{2s}$ (iv) $\frac{1}{s}$
2. Inverse Laplace transform of $\frac{1}{s^5}$ is _____.
 (i) $\frac{t^5}{24}$ (ii) $\frac{t^4}{12}$ (iii) $\frac{t^4}{24}$ (iv) t^3
3. $f(k) = 1, k \in N$ is a _____ sequence.
 (i) Kronecker delta (ii) Unit step (iii) Unit ramp (iv) ramp
4. If $F(w)$ is the Fourier transform of $f(t)$ then $F[f(t - \alpha)] =$ _____.
 (i) $e^{j\alpha w} F(w)$ (ii) $e^{\alpha w} F(w)$ (iii) $F(w)$ (iv) $e^{-j\alpha w} F(w)$
5. The discrete fourier transform $F(k)$ is periodic with period N then _____.
 (i) $F(kN) = F(k)$ (ii) $F(k + N) = F(k)$
 (iii) $F(k + N) = kF(k)$ (iv) $F(k + N) = f(k^2)$

SECTION - B (15 Marks)

Answer **ALL** questions

ALL questions carry **EQUAL** Marks

(5 x 3 = 15)

6. (a) Find Laplace transform of (i) $t \sin t$ (ii) $e^{-3t} \sinh 4t$
 (OR)
 (b) Find Laplace transform of (i) $\frac{1}{3} \sin 3t - 4 \cos(\frac{t}{2})$ (ii) $\sinh 2t + 3 \cosh 2t$
7. (a) Find the inverse Laplace transform of $\frac{6s-5}{(s+5)(s+3)}$.
 (OR)
 (b) Find the inverse Laplace transform of $\frac{2s+1}{s^2-2s+2}$.
8. (a) Find the z transform of the sequence defined by $f[k] = k, k \in N$.
 (OR)
 (b) Find the z transform of $e^{-2k} \cos k$.
9. (a) Find the Fourier transform of the function $f(t) = u(t)e^{-t}$, where $u(t)$ is the unit step function.

(OR)

- (b) Find the Fourier transform of $f(t) = \begin{cases} 1 - \frac{t}{2} & 0 \leq t \leq 2 \\ 1 + \frac{t}{2} & -2 \leq t \leq 0 \\ 0 & \text{otherwise} \end{cases}$

Cont...

10. (a) Find the inverse discrete fourier transform of the sequence $F[k]$, for $k = 0, 1, 2, 3$ given by $F[k] = -4, 1, 0, 1$.
(OR)
- (b) Calculate the circular convolution, $h[n] = f * g$, of the two periodic sequences $f[n] = 9, -1, 3$ and $g[n] = 7, 2, -4$.

SECTION -C (30 Marks)

Answer ALL questions

ALL questions carry EQUAL Marks (5 × 6 = 30)

11. (a) State Final value theorem. Verify Final value theorem for $f(t) = e^{-t} \sin t$.
(OR)
- (b) Find Laplace transform of $3y'' - y' + 2y = 0$ given that $y(0) = 3, y'(0) = 1$.
12. (a) (i) Find $f * g$ when $f = 1, g = t$
(ii) Use the convolution theorem to determine the inverse Laplace transform of $\frac{1}{s^2(s+1)}$.
(OR)
- (b) Using Laplace transform solve $x'' - 5x' + 6x = 6t - 4$ given that $x(0) = 1, x'(0) = 2$
13. (a) The continuous signal $f(t) = \cos\left(\frac{\pi t}{2}\right)$ is sampled at 1 second intervals starting from $t = 0$.
(i) Find the Laplace transform of the sampled signal $f^*(t)$.
(ii) Show that $F^*(s)$ has an infinity of poles.
(iii) Find the z transform of the sampled signal and show that this is just two poles.
(OR)
- (b) Find the sequence whose z transform is
(i) $F(z) = \frac{2z^2 - z}{(z-5)(z+4)}$. (ii) $F(z) = \frac{z+3}{z-2}$
14. (a) Show that the Fourier transform of $f(t) = \begin{cases} 3 & -2 \leq t \leq 2 \\ 0 & \text{elsewhere} \end{cases}$ is given by
 $F(\omega) = \frac{6 \sin 2\omega}{\omega}$. Use the first shift theorem to find the Fourier transform of $e^{-jt} f(t)$. Also verify the first shift theorem by obtaining the Fourier transform of $e^{-jt} f(t)$ directly.
(OR)
- (b) Calculate the convolution $f * g$ when $f(t) = u(t)e^{-t}$ and $g(t) = u(t)e^{-2t}$, where $u(t)$ is the unit step function. Also verify the convolution theorem for these functions.
15. (a) Find the d.c.t., $F[k]$ of the sequence $f[n] = 2, 4, 6$. Also apply the inverse d.c.t. to $F[k]$ and show that the original sequence, $f[n]$, is obtained.
(OR)
- (b) Use the (Circular) convolution theorem to find $f * g$ when $f[n] = 5, 4$ and $g[n] = -1, 3$.