PSG COLLEGE OF ARTS & SCIENCE (AUTONOMOUS)

BSc DEGREE EXAMINATION MAY 2024

(Second Semester)

Branch - STATISTICS

PROBABILITY THEORY / PROBABILITY & DISTRIBUTIONS - I

Time: Three Hours

Maximum: 75 Marks

SECTION-A (10 Marks)

Answer ALL questions

ALL questions carry EQUAL marks

 $(10 \times 1 = 10)$

All Questions are Multiple Choice

| Module No. | Question No. | Question | K Level | СО |
|---------------|-----------------|--|------------|-----|
| 1 | 1 | If two event the conditional probability of A given A is equal to a) 0 b)1 c)Infinite d) inter determinate | K1 | CO1 |
| | 2 | If B A the probability P(A/B) is equal to a) 0 b)1 c) P(A)/P(B) d) P(B)/P(A) | K2 | CO1 |
| 2 | 3 | Two random variable X and Y are said to be independent if a) E(XY)=0 b) E(XY)=1 c) E(XY)=E(X)E(Y) d) All of these | K1 | CO2 |
| | 4 | If X is a random variable the E(t ^x) is a) CGF b) MGF c) PGF d) X th moment | K2 | CO2 |
| 3 | 5 | The heights of father and their sons form bivariable variables which are a) Continuous b) Discrete c) Both a and b d) None of these | K1 | CO3 |
| | 6 | Bivariate normal distribution is named as a) Bravais distribution b) Laplace-gauss distribution c) Gaussian distribution d) All the above | K2 | CO3 |
| 4 | 7 | If X is a random variable the E(e ^{xti}) is a) CGF b) MGF c) PGF d) X th moment | K1 | CO4 |
| | 8 | If X is a random variable the E(e ^{xt}) is a) CGF b) MGF c) PGF d) X th moment | K2 | CO4 |
| 5 | 9 | If X is a random variable with its mean \overline{X} the expression $E(X-\overline{X})^2$ represents a) Variance b) covariance c) second central moment d) both a and c | K1 | CO5 |
| | 10 | If X is a r.v, which can take only non negative values then a) $E(X^2) = [E(X)]^2$ b) $E(X^2) \ge [E(X)]^2$ c) $E(X^2) \le [E(X)]^2$ d) $E(X^2) \ne [E(X)]^2$ | K2 | CO5 |

SECTION - B (35 Marks)

Answer ALL questions

ALL questions carry EQUAL Marks $(5 \times 7 = 35)$

| Module No. | Question No. | Question | K Level | СО |
|---------------|-----------------|---|------------|-----|
| 1 | 11.a. | Define i)Random experiment ii) Algebra of events. | K2 | CO1 |
| | | (OR) | | |
| | 11.b. | Show that the multiplication theorem on probability. | | |
| 2 | 12.a. | Prove that $V(aX+b) = a^2$ | К3 | CO2 |
| | | (OR) | | |
| | 12.b. | Examine Random variable and its types. | | C |
| 3 | 13.a. | Inspect the assumptions of Bivariate Distribution. | К3 | CO3 |
| | (OR) | | | |
| | 13.b. | Organize the properties of joint distribution function. | | |
| 4 | 14.a. | Mention the properties of moment generating function. | K5 | CO4 |
| | | (OR) | | |
| | 14.b. | State and prove the weak law of large numbers. | | |
| 5 | 15.a. | Estimate the distribution of the difference of two random variable. | K5 | CO5 |
| | | (OR) | | - |
| | 15.b. | Derive the distribution of the quotient of two random variable. | | |

SECTION - C (30 Marks)

Answer ANY THREE questions

ALL questions carry EQUAL Marks $(3 \times 10 = 30)$

| Module No. | Question No. | Question | K Level | со |
|---------------|-----------------|--|------------|-----|
| 1 | 16 | A letter is known to have come either from TATANAGAR or from CALCUTTA. On the envelop just two consecutive letters TA are visible. What is the probability that the letter came from CALCUTTA? | К3 | CO1 |
| 2 | 17 | Prove that the properties of Expectation of random variables. | K5 | CO2 |
| 3 | 18 | Derive the marginal density function of bivariate distribution. | K4 | CO3 |
| 4 | 19 | State and prove the chebychev's Inequality. | K5 | CO4 |
| 5 | 20 | If X and Y are independent continuous random variable, then the pdf of $U = X + Y$ is given by $h(u) = \int_{-\infty}^{\infty} f(v)f(u - v)dv.$ | K4 | CO5 |