

PSG COLLEGE OF ARTS & SCIENCE
(AUTONOMOUS)

BSc DEGREE EXAMINATION MAY 2024
(Second Semester)

Branch - STATISTICS

NUMERICAL METHODS

Time: Three Hours

Maximum: 75 Marks

SECTION-A (10 Marks)

Answer ALL questions

ALL questions carry EQUAL marks

$(10 \times 1 = 10)$

Module No.	Question No.	Question	K Level	CO
1	1	Mention $3x - \cos x - 1 = 0$ is a a) Algebraic equation b) Transcendental equation c) both (a) and (b) d) done	K1	CO1
	2	When $x = \varphi(x)$, the iteration process converges quickly if, a) $ \varphi(x) = 1$ b) $ \varphi(x) < 1$ c) $ \varphi(x) > 1$ d) $ \varphi(x) = 0$	K2	CO1
2	3	State the differences of constant function $\Delta(c) =$ a) 0 b) < 0 c) > 0 d) 1	K1	CO2
	4	Find the relation between the difference operators E and Δ a) $E > 1 + \Delta$ b) $E < 1 + \Delta$ c) $E = 1 + \Delta$ d) $E = 1 - \Delta$	K2	CO1
3	5	When the arguments x_1, x_2, \dots, x_n are not equally spaced then, we can use a) Gauss method b) Newton's forward method c) Newton's backward method d) Lagrange's method	K1	CO2
	6	Gauss backward interpolation formula useful when a) $0 < n < 1$ b) $-1 < n < 1$ c) $-1 < n < 0$ d) $-2 < n < 0$	K2	CO2
4	7	Indicate in numerical integration, the accuracy of the result can be improved by ----- the interval 'h'. a) increasing b) decreasing c) increasing or decreasing d) none	K1	CO3
	8	Mention Truncation error arises in a) numerical integration b) numerical differentiation c) numerical interpolation d) numerical extrapolation	K2	CO1
5	9	In an Euler's method, which of the following is called local error? a) $O(h^4)$ b) $O(h^3)$ c) $O(h^2)$ d) $O(h)$	K1	CO3
	10	To use Milne's predictor-corrector formula, we need atleast ----- values prior to the required value. a) 1 b) 2 c) 3 d) 4	K2	CO2

Cont ...

SECTION - B (35 Marks)

Answer ALL questions

ALL questions carry EQUAL Marks $(5 \times 7 = 35)$

Module No.	Question No.	Question	K Level	CO												
1	11.a.	Find a real root of the equation $x^3+x^2-1=0$ by iteration method. (OR)	K2	CO2												
	11.b.	Explain Newton-Raphson method.														
	12.a.	Show that $E\nabla = \nabla E = \Delta$ (OR)														
2	12.b.	Find $f(0.2)$ by suitable formula.	K3	CO4												
		<table border="1" style="margin-left: auto; margin-right: auto;"> <tr><td>x</td><td>0</td><td>1</td><td>2</td><td>3</td><td>4</td><td>5</td><td>6</td></tr> <tr><td>f(x)</td><td>176</td><td>185</td><td>194</td><td>203</td><td>212</td><td>220</td><td>229</td></tr> </table>			x	0	1	2	3	4	5	6	f(x)	176	185	194
x	0	1	2	3	4	5	6									
f(x)	176	185	194	203	212	220	229									
3	13.a.	State central differences for interpolation. (OR)	K2	CO3												
	13.b.	Using Bessel's formula, find $f(25)$ given $f(20)=2854$, $f(24)=3162$, $f(28)=3544$ and $f(32)=3992$.														
	14.a.	Explain Trapezoidal rule. (OR)														
4	14.b.	Calculate $\int_0^1 e^{-x^2} dx$ by dividing the range of integration in to 4 equal parts using Simpson's $\frac{1}{3}$ rule.	K3	CO2												
	15.a.	Using Taylor series method to compute $y(0.1)$ correct to 4 decimal places if $y(x)$ satisfies $y' = x+y$, $y(0) = 1$ (OR)														
5	15.b.	Explain the procedure for Euler's method for solving differential equation.	K3	CO5												

SECTION -C (30 Marks)

Answer ANY THREE questions

ALL questions carry EQUAL Marks $(3 \times 10 = 30)$

Module No.	Question No.	Question	K Level	CO														
1	16	Enumerate the root of $xe^x = 3$ by Regula -Falsi method correct to three decimal places.	K1	CO1														
2	17	Enumerate the missing values in the following data. <table border="1" style="margin-left: auto; margin-right: auto;"> <tr><td>x</td><td>0</td><td>5</td><td>10</td><td>15</td><td>20</td><td>25</td></tr> <tr><td>y</td><td>6</td><td>10</td><td>-</td><td>17</td><td>-</td><td>31</td></tr> </table>	x	0	5	10	15	20	25	y	6	10	-	17	-	31	K1	CO4
x	0	5	10	15	20	25												
y	6	10	-	17	-	31												
3	18	Enumerate the value of x when $y= 85$, using Lagranges's formula from the following table. <table border="1" style="margin-left: auto; margin-right: auto;"> <tr><td>x</td><td>2</td><td>5</td><td>8</td><td>14</td></tr> <tr><td>y</td><td>94.8</td><td>87.9</td><td>81.3</td><td>68.7</td></tr> </table>	x	2	5	8	14	y	94.8	87.9	81.3	68.7	K3	CO2				
x	2	5	8	14														
y	94.8	87.9	81.3	68.7														
4	19	Highlight Newton's Forward and Backward formula to compute the derivatives.	K1	CO3														
5	20	By applying the fourth order Runge-Kutta method Enumerate $y(0.2)$ from $y' = y-x$, $y(0) = 2$ taking $h=0.1$	K3	CO5														