

PSG COLLEGE OF ARTS & SCIENCE  
(AUTONOMOUS)

BSc DEGREE EXAMINATION MAY 2024  
(Fifth Semester)

Branch – PHYSICS

MATHEMATICAL PHYSICS

Time: Three Hours

Maximum: 50 Marks

SECTION-A (5 Marks)

Answer ALL questions  
ALL questions carry EQUAL marks (5 x 1 = 5)

- 1  $0^{\text{th}}$  rank tensor is called .....  
(i) scalar (ii) vector  
(iii) matrix (iv) None of the above
- 2 Find an equation in spherical coordinates from a rectangular equation  $x^2 + y^2 = z^2$   
(i) 0 (ii) -1  
(iii) 1 (iv) Infinity
- 3 If the order of the matrix is  $m \times n$ , then how many elements will there be in the matrix?  
(i)  $mn$  (ii)  $m^2n^2$   
(iii)  $mn^2$  (iv)  $2mn$
- 4 If the Laplace transform of function  $f(t)$  is given by  $S / (S^2 - 4)$  then the  $f(t)$  is  
(i)  $\sin(2t)$  (ii)  $\cosh(2t)$   
(iii)  $\sinh(2t)$  (iv)  $\cos(2t)$
- 5 If  $u = x^2 - y^2$ , then the conjugate harmonic function is  
(i)  $2xy$  (ii)  $x + y$   
(iii)  $4xy$  (iv)  $x - y$

SECTION - B (15 Marks)

Answer ALL Questions  
ALL Questions Carry EQUAL Marks (5 x 3 = 15)

- 6 a Define tensor  
OR  
b State Gauss divergence theorem.
- 7 a Prove that  $\text{div curl } A = 0$   
OR  
b Explain about orthogonal curvilinear coordinate.
- 8 a Compare unitary transformation and orthogonal transformation.  
OR  
b Explain the characteristics equation of a matrix.
- 9 a Define Fourier series.  
OR  
b Find Laplace transform of  $(t^n)$ ,  $n > -1$
- 10 a Define continuity and differentiability.  
OR  
b Write conditions for Harmonic functions.

**SECTION -C (30 Marks)**

Answer ALL questions

ALL questions carry EQUAL Marks

(5 x 6 = 30)

- 11 a Find a unit vector perpendicular to the surface  $x^2 + y^2 - z^2 = 11$ , at the point (4,2,3)  
OR  
b Derive the Christobel's 3 – index symbol.
- 12 a Discuss Differential operators in terms of orthogonal curvilinear co-ordinates.  
OR  
b Discuss Differential operators in terms of spherical polar curvilinear co-ordinates.
- 13 a Explain similarity transformation with an example.  
OR  
b Explain power of matrix with suitable examples.
- 14 a Discuss the Properties of Fourier's transform.  
OR  
b Derive Laplace transform of integral.
- 15 a Write the Cauchy – Riemann equations.  
OR  
b Determine the analytic function  $f(z) = u + iv$  where  $V = 6xy - 5x + 3$  express the result as a function of Z.

Z-Z-Z

END