PSG COLLEGE OF ARTS & SCIENCE

(AUTONOMOUS)

BSc DEGREE EXAMINATION DECEMBER 2017

(Fourth Semester)

Branch - STATISTICS

BASIC SAMPLING THEORY

Time: Three Hours

Maximum: 75 Marks

SECTION-A (20 Marks)

Answer **ALL** questions

ALL questions carry **EQUAL** marks $(10 \times 2 = 20)$

1 In which situations sampling in inevitable?

- 2 Distinguish between questionnaire and schedule.
- 3 State the demerits of simple random sampling.
- What do you mean by sampling with replacement?
- 5 Define sample frame and finite population correction.
- 6 State any two merits of stratified random sampling.
- 7 Express standard error of sample mean in terms of S^2 .
- 8 In which situations systematic sampling is preferred over the other sampling procedures.
- 9 Give the formula for mean and variance of systematic sample.
- Write the merits of cluster sampling.

SECTION - B (25 Marks)

Answer ALL Questions

ALL Questions Carry **EQUAL** Marks $(5 \times 5 = 25)$

11 a Distinguish between completed enumeration and sampling study.

OK

- b Write a short note on the important of random sample.
- 12 a Discuss the method of selecting a simple random sample.

OR

- b Show that $\frac{N-n}{N}s^2$ is biased for $var\begin{pmatrix} -x \\ x \end{pmatrix}$ in case of simple random sampling without replacement.
- 13 a Prove that var $\begin{pmatrix} \\ y_{st} \end{pmatrix} = \frac{1}{N^2} \sum_{n=1}^{l} \frac{N_h (N_h n_h)}{n_h}$. S_h^2 in stratified random sampling.

OR

- b prove that under proportional allocation $var \begin{pmatrix} \\ y_{st} \end{pmatrix} = \frac{1-f}{n} \sum_{h=1}^{L} W_h . S_h^2$.
- 14 a Obtain the variance of sample mean under systematic sample.

OK

- b What are the advantages and disadvantages of systematic sample?
- What are the main differences between cluster sampling and stratified sampling?
 - b Distinguish between ratio and regression estimators.

14STU12 cont...

SECTION - C (30 Marks)

Answer any **THREE** Questions **ALL** Questions Carry **EQUAL** Marks (3 x 10 = 30)

- Discuss briefly about the two types of errors in sampling.
- Derive the expression for $V\left(\frac{1}{y_n}\right)$ in simple random sampling with and without replacement and compare the results.
- Prove that $V\left(\overline{Y_n}\right) \le V\left(\overline{Y_{sys}}\right) \le V\left(\overline{Y_{ran}}\right)$, when population in linear trend.
- Obtain the relative precision on stratified random sampling and simple random sampling.
- A simple random sample of n clusters, each containing M elements, is drawn from the N clusters in the population. Then prove that, the variance of sample mean per element $\stackrel{=}{y}$ is $var\left(\stackrel{=}{y}\right) = \left(\frac{1-f}{nM}\right)s^2\left[1+(M-1)\rho\right]$.

Z-Z-Z

END