

**MATHEMATICAL METHODS - II**

Time : Three Hours

Maximum : 75 Marks

**SECTION-A (20 Marks)**

Answer ALL questions

ALL questions carry EQUAL marks (10 x 2 = 20)

- 1 What is marginal revenue?
- 2 State the second order condition for minimization and maximization.
- 3 If  $z = 2x^3y^2$ , find  $\partial z / \partial x$  &  $\partial z / \partial y$ .
- 4 If  $z = 3x^3y$ , find  $\partial^2 z / \partial x^2$ .
- 5 What is integration?
- 6 What is producer's surplus?
- 7 What is meant by Linear programming ?
- 8 State the meaning of saddle point.
- 9 State any two assumptions of input output analysis.
- 10 State any two limitations of input output analysis.

**SECTION - B (25 Marks)**

Answer ALL Questions

ALL Questions Carry EQUAL Marks (5 x 5 = 25)

- 11 a If  $y = \sqrt{4x^4 + 25x^3} - x + 50$  find  $dy/dx$ .  
OR  
b If total cost of a firm is  $C = 15x^3 - 8e^x + 5\log x$ , then find average cost and marginal cost.
- 12 a If  $u = 3x^2 + 5xy^2 - 2y$ , prove that  $\partial^2 u / \partial x \partial y = \partial^2 u / \partial y \partial x$ .  
OR  
b If the production function of a firm is  $Q = 8LK - L^2 - K^2$ , show that  $L \cdot \partial Q / \partial L + K \cdot \partial Q / \partial K = 2Q$ .
- 13 a Evaluate :  $\int 1/x + 3x^2 + e^x dx$ .  
OR  
b If the demand function  $p = 45 - 2x - x^2$  and the demand  $x_0$  is 4, what will be the consumer's surplus.
- 14 a Explain the assumptions of Linear programming.  
OR  
b Write a short note on simplex method.
- 15 a List out the importance of input output analysis.  
OR  
b Explain the assumptions and limitations of input output analysis.

**SECTION - C (30 Marks)**Answer any **THREE** Questions**ALL** Questions Carry **EQUAL** Marks (3 x 10 = 30)

- 16 Given the demand function  $x^2 = 12 - p$  and cost function  $C = -\frac{4}{3}x^3 + 4x^2 + 10$ , where  $p$  denotes price,  $x$  number of units of output and  $c$  is the total cost. Find the output when profit is maximum.
- 17 In a duopoly market, demand and cost functions are given as  $p = 150 - 0.4Q_1 + 0.4Q_2$ ,  $C_1 = 8Q_1$ ;  $C_2 = 0.4Q_2^2$ . Find output  $Q_1$ ,  $Q_2$  and Profit of both the seller.
- 18 Marginal cost of a firm is  $100 - 10x + 0.1x^2$ , Where  $x$  is the output. What is the total cost function and average cost function if the fixed cost is Rs.500. Also find the output when marginal cost is minimum.
- 19 Explain the uses of linear programming.
- 20 There are two industries A and B in an economy. The following table gives the supply and demand position of these industries in million Rupees.

Industry	A	B	Final Demand	Total Output
A	30	20	20	70
B	40	60	30	130

Determine the total output if the final demand changes to 24 for industry A and 36 for B.

Z-Z-Z

END