

Branch MATHEMATICS

FLUID DYNAMICS

Time: Three Hours

Maximum: 75 Marks

Answer ALL questions
ALL questions carry EQUAL marks (5 x 15 = 75)

- 1 a Give an account of (i) Density, weight and Specific Volume
(ii) Specific heat fluid properties. (15)
OR
b Derive the fluid motion by Lagrangian method. (8)
c Describe the vorticity in orthogonal curvilinear coordinates. (7)
- 2 a Verify the following invariants for two dimensional stress components
 $(G_x - a_y \cdot y')^2 + 4a^y = (a_{xx} + a_{yy})^2 + 4a_{xy}$ (5)
b Derive the relationship between stress and Strain. (10)
OR
c Derive the energy equation at conservation of energy. (15)
- 3 a State and prove Kelvin's theorem at constancy of circulation. (8)
b Give an examples of irrotational and rotational flows. (7)
OR
c Derive the integration of equation of motion in Bernoulli's equation. (7)
d Derive the Laplace equation of velocity potential in spherical coordinates. (8)
- 4 a Derive the velocity distribution of Couette flow of two parallel plates.
Also solve the following.
(i) Average and maximum velocity distribution
(ii) Shearing Stress of Couette flow of two parallel plates (15)
OR
b State and prove Reynolds law of dynamical similarity. (7)
c Solve the shearing stress of flow⁷ between two concentric rotating cylinders. (8)
- 5 a State the properties of Navier - Stokes equation. (7)
b Derive the momentum integral equation of the boundary layer by momentum law. (8)
OR
c Solve the Prandtl boundary layer equation along a flat plate in account of the Blasius solution. (15)