

Branch- STATISTICS
MATRICES

Time: Three Hours

Maximum: 75 Marks

SECTION-A (20 Marks)

Answer ALL questions

ALL questions carry EQUAL marks (10x2 = 20)

Give the examples for diagonal matrix and scalar matrix.

What is meant by unitary matrix?

Define determinant of a square matrix.

4 Find the cofactor of $\begin{vmatrix} 3 & 2 \\ 5 & 0 \end{vmatrix}$

Find the rank of $A = \begin{vmatrix} 3 & 6 \\ 4 & 8 \end{vmatrix}$

6 • What is the application of rank of a matrix?

7 Define characteristic polynomial.

8 What is characteristic vector?

9 Define basic of a vector.

10 Define quadratic form.

SECTION - B (25 Marks)

Answer ALL Questions

ALL Questions Carry EQUAL Marks (5 x 5 = 25)

11 a Show that the matrix $\begin{vmatrix} \cos\theta & \sin\theta \\ -\sin\theta & \cos\theta \end{vmatrix}$ is orthogonal.

OR

Define (i) Hermitian matrix with example (ii) Skew - Hermitian matrix with example. »

12 a Find the adjoint of $\begin{vmatrix} 1 & 2 \\ 5 & 3 \\ 2 & 1 \end{vmatrix}$

OR

b State the properties of determinant.

13 a Verify whether the given system of equation is consistent.

$$2x + 5y + 7z = 52$$

$$x + y + z = 9$$

$$2x + y - z = 0.$$

• OR

b Explain homogenous and non-homogenous with examples.

14 a Derive the expression for the inverse of a non-singular matrix.

OR

b State certain relationship between characteristic roots and vectors.

- 15 a Write down the quadratic forms corresponding to the following symmetric matrices. .

$$\begin{pmatrix} 1 & 2 & 3 \\ 0 & 2 & 0 & 3 \\ 3 & 3 & 1 \end{pmatrix} \quad \text{(ii) dig } (X_1, X_2, \dots, X_n)$$

OR

- b Write down the matrix of each of the following quadratic forms,

(i) $x^2 - 18x_1x_2 + 5x_2^2$ (ii) $x^2 + 2x_1x_2 - 5x_3^2 - x_1x_2 - 3x_3x_1$

SECTION - C (30 Marks)

Answer any THREE Questions

ALL Questions Carry EQUAL Marks (3 x 10 = 30)

- 16 i) Define equal and equivalent matrices.

ii) Show that the matrix $A = \begin{bmatrix} -5 & -8 & 0 \\ 3 & 5 & 0 \\ 1 & 2 & -2 \end{bmatrix}$ is involutory.

- 17 Find the inverse of the matrix $A = \begin{pmatrix} 1 & 0 & -1 \\ 3 & 4 & 5 \\ 0 & -6 & -7 \end{pmatrix}$

- 18 • Find the rank of the matrix $\begin{vmatrix} 1 & 2 & 3 & -1 \\ 2 & 4 & 6 & -2 \\ 3 & 6 & 9 & -3 \end{vmatrix}$

- 19 Determine the characteristic roots of a matrix $A = \begin{pmatrix} 0 & 1 & 2 \\ 1 & 0 & -1 \\ 2 & -1 & 0 \end{pmatrix}$

20 Define:

- (i) Positive definite
- (ii) Negative definite
- (iii) Positive semi-definite
- (iv) Negative semi-definite
- (v) Indefinite.

Z-Z-Z

END