

- Branch - STATISTICS

STATISTICAL INFERENCE -1

Time : Three Hours

Maximum : 75 Marks

SECTION-A (20 Marks)

Answer ALL questions

ALL questions carry EQUAL marks (10 x 2 = 20)

- 1 Define point estimation.
- 2 When do you say an estimator is efficient.
- 3 State asymptotic efficiency of an estimator.
- 4 What do you mean by sufficient statistic?
- 5 Give any two methods of estimation.
- 6 Define likelihood function.
- 7 Define standard error.
- 8 What is confidence co-efficient?
- 9 Define order statistics. *
- 10 When do you use non-parametric tests.

SECTION - B (25 Marks)

Answer ALL Questions

ALL Questions Carry EQUAL Marks (5 x 5 = 25)

- 11 a Prove that the sample mean from $N(p, a^2)$ is consistent for p .
OR
b Prove that minimum variance unbiased estimator is unique. *
- 12 a Let X_1, x_2, \dots, x_n , be a random sample from $N(p, CT^2)$, find the sufficient estimator for p .
OR
b State and prove Rao - Blackwell theorem.
- 13 a Explain briefly about method of moments.
OR
b Describe briefly about method of minimum variance.
- 14 a Obtain $100(1-\alpha)\%$ confidence interval for p when small samples are taken from $N(p, CT^2)$. *
OR
b Write a short note on Baye's estimation.
- 15 a Explain briefly about distribution of order statistic.
OR
b Write a short note on sign test.

SECTION - C (30 Marks)

Answer any THREE Questions

ALL Questions Carry EQUAL Marks (3 x 10 = 30)

- 16 State and prove Cramer - Rao inequality.*
- 17- Let $x_1, x_2, x_3, \dots, x_n$ are random sample from $f(x, \theta) = \exp \{-(x - \theta)\}$,
 $0 < x < \infty, -\infty < \theta < \infty$, obtain sufficient statistics for θ .
- 18 Show the sample mean \bar{x} in random sampling from $f(x, \theta) = \frac{1}{\Gamma(\theta)} e^{-x/\theta}$,
 $0 < x < \infty, 0 < \theta < \infty$, is an MLE of θ and has variance θ^2/n .
- 19 Find $100(1-\alpha)\%$ confidence interval for difference of two proportions. *
- 20 Explain the procedure to find goodness of fit by χ^2 - test