

PSG COLLEGE OF ARTS & SCIENCE  
(AUTONOMOUS)  
BSc DEGREE EXAMINATION DECEMBER 2018  
(First Semester)

Branch - MATHEMATICS

CLASSICAL ALGEBRA AND TRIGONOMETRY

Time : Three Hours

Maximum : 75 Marks

**SECTION-A (20 Marks)**

Answer ALL questions

ALL questions carry EQUAL marks (10 x 2 = 20)

- 1 Define a convergent sequence, say whether the sequence  $\left\{ \frac{1}{2n+2} \right\}$  is convergent or not
- 2 When do you say a series as a divergent series?
- 3 If  $\sum u_n$  and  $\sum v_n$  are two series of positive terms and if  $\frac{u_n}{v_n} < \frac{1}{k}$  and  $\frac{1}{k}$  is a constant when can  $\sum u_n$  be convergent.
- 4 Say whether the series  $1 - \frac{1}{2^2} + \frac{1}{3^2} - \frac{1}{4^2} + \dots$  is absolutely convergent or not.
- 5 State remainder theorem.
- 6 If  $a, p, q$  and the roots of the equation  $x^3 + px^2 + qx + r = 0$  find  $\frac{1}{a} + \frac{1}{p} + \frac{1}{q} + \frac{1}{r}$ .
- 7 If  $x = \cos t - W \sin t$  find  $\frac{dx}{dt} - V$ .
- 8 Prove that  $\sin 2x = 2 \sin x \cos x$ .
- 9 Write down the principal value of  $\log(x + iy)$ .
- 10 Write down the gregor's series of  $\tan^{-1} x$ .

**SECTION - B (25 Marks)**

Answer ALL Questions

ALL Questions Carry EQUAL Marks (5 x 5 = 25)

- 11 a Show that  $\left\{ \frac{1}{n+1} \right\}$  is a monotonic increasing sequence.  
OR  
b Discuss the convergence of the series  $\sum \frac{1}{n}$
- 12 a Test for convergence the series  $a + b + a^2 + b^2 + a^3 + b^3 + \dots$   
OR  
b Prove that an absolutely convergent series is convergent.
- 13 a Form a rational cubic equation which shall have for roots 1, 3-4-2.  
OR  
Show that if the roots of the equation  $x^3 + px^2 + qx + r = 0$  are in arithmetic progression then  $2p^3 - 9pq + 27r = 0$ .
- 14 a Evaluate  $\lim_{x \rightarrow 0} \frac{\tan 2x - 2 \tan x}{x}$ .  
OR  
b Expand  $\cosh^8 \theta$  in terms of hyperbolic cosines of  $\theta$ .

15 a Find the value of  $\log(4+3i)$

OR

b Sum  $n$  terms the series  $\sin a + \sin^2 2a + \sin^3 3a + \dots$

**SECTION - C (30 Marks)**

Answer any **THREE** Questions

**ALL** Questions Carry **EQUAL** Marks (3 x 10 = 30)

16 / Show that the series  $\sum_{r=0}^{\infty} r^k x^r$  is convergent when  $k$  is greater than unity and divergent when  $k$  is equal to or less than unity.

17 Discuss the convergency of the series

$$\frac{x}{1+x} + \frac{x^2}{1+2x^2} + \frac{x^3}{1+3x^3} + \frac{x^4}{1+4x^4} + \dots$$

for positive values of  $x$ .

18 Solve the equation  $6x^5 - x^4 - 43x^3 + 43x^2 + x - 6 = 0$ .

19 Expand  $\cos^5 \theta \sin^3 \theta$  in a series of sines of multiples of  $\theta$ .

20 Show that  $\log \tan(\theta + i\alpha) = i \tan^{-1}(\sinh x)$ .

Z-Z-Z

END