

PSG COLLEGE OF ARTS & SCIENCE  
(AUTONOMOUS)

**BSc DEGREE EXAMINATION DECEMBER 2018**  
(Third Semester)

Branch- **MATHEMATICS**

**MECHANICS -1 (STATICS!)**

Time : Three Hours

Maximum : 75 Marks

**SECTION-A 120 Marks!**

Answer **ALL** questions

**ALL** questions carry **EQUAL** marks (10 x 2 = 20)

- 1 What is the resultant of two perpendicular forces?
- 2 State the polygon law of forces.
- 3 “The effect of two equal and unlike parallel forces cannot be replaced by a single force”. Why?
- 4 Define the moment of a force.
- 5 Define the moment of a couple.
- 6 State the equivalence of two couple.  
What are the necessary and sufficient conditions that a system of coplanar forces acting on a rigid body may be in equilibrium?
- 8 State the second form of the conditions of equilibrium of a system of coplanar forces.
- 9 Define the centre of gravity.
- 10 What is the centre of gravity of a thin plate?

**SECTION - B (25 Marks!)**

Answer **ALL** Questions

**ALL** Questions Carry **EQUAL** Marks (5 x 5 = 25)

- 11 a State and prove Lami's theorem.  
OR  
b State and prove an extended form of the parallelogram, law of forces.
- 12 a State and prove the generalized theorem of moments.  
OR  
b Find the conditions of equilibrium of three coplanar parallel forces.
- 13 a Find the resultant of a couple and force.  
OR  
b ABC is an equilateral triangle of side a: D, E, F dividing the sides BC, CA, AB respectively in the ratio 2:1. Three forces each equal to  $\frac{1}{2}Pa$  act at D, E, F perpendicularly to the sides and outward from the triangle. Prove that they are equivalent to a couple of moment  $\frac{1}{4}Pa$ .
- 14 a Forces 3,2,4,5 kg.wt act respectively along the side AB, BC, CD and DA of a square. Find the magnitude of their resultant and the points where its line of action meets AB and AD.  
OR  
b State and prove the third form of the conditions of equilibrium of a system of coplanar forces.
- 15 a Prove that the centre of gravity of a body is unique.  
OR  
b Find the C.G of a uniform solid hemisphere.

**SECTION - C (30 Marks)**

Answer any **THREE** Questions

**ALL** Questions Carry **EQUAL** Marks (3 x 10 = 30)

- 16 i) State the parallelogram law of forces and also find an analytical expression for the resultant of two forces, (ii) State and prove the theorem on resolved parts.
- 17 State and prove the Varignon's theorem of moments.
- 18 Prove that if two couples, whose moments are equal and opposite, act in the same plane upon a rigid body, they balance one another.
- 19 ABCDEF is regular hexagon: forces P,2P,3P,2P,5P,6P act along AB,BC,DC,ED,EF,AF respectively. Show that the six forces are equivalent to a