

PSG COLLEGE OF ARTS & SCIENCE  
(AUTONOMOUS)

MCA DEGREE EXAMINATION DECEMBER 2018  
(Second Semester)

Branch - COMPUTER APPLICATIONS

MATHEMATICAL STRUCTURES

Time: Three Hours

Maximum: 75 Marks

Answer ALL questions  
ALL questions carry EQUAL marks (5x15 = 75)

1 a If A, B and C are any three sets, prove that  $A \cup (B \cap C) = (A \cup B) \cap C$ . (5)

b Prove that by Venn diagram  $A \cap (B \cup C) = (A \cap B) \cup (A \cap C)$ . (5)

c If  $U = \{1,2, 3,4, 5,6,7, 8,9\}$

$A = \{1,3, 5\}$ ,  $B = \{2, 4, 6, 8\}$  and  $C = \{2, 5, 10\}$

Verify  $(A \cap B)^c = A^c \cap B^c$ . (5)

OR

d If  $A = \{1, 2, 3\}$ ,  $B = \{3, 4\}$  and  $C = \{4, 5, 6\}$

Find (i)  $A \times (B \cup C)$  (ii)  $A \times (B \cap C)$  (iii)  $(A \times B) \cap (B \times C)$  (8)

e If  $f : A \rightarrow B$  and  $g : B \rightarrow C$  are two 1-1 and onto functions, prove that

(i)  $g \circ f : A \rightarrow C$  is one to one onto and

(ii)  $g \circ f$  is invertible (7)

2 a Solve by Gauss elimination and Gauss Jordan method :

$X + 2y + z = 3$ ;  $2x + 3y + 3z = 10$ ;  $3x - y + 2z = 13$  (7+8)

OR

b Solve for x from  $\cos x - xe^x = 0$  by iteration method. (7)

c Solve for a positive root of  $x^3 - 4x + 1 = 0$  by Regula falsi method. (8)

Find the non-degenerate basic feasible solution for the T.P

(i) Northwest Corner Rule (5)

(ii) Least Cost method (5)

(iii) Vogel's approximation method (5)

		To Supply				
		10	20	5	7	10
		13	9	12	8	20
From		4	5	7	9	30
		14	7	i	0	40
		3	12	5	19	50
Demand		60	60	20	10	

OR

b Describe the Difference between TP and Assignment problem. (3)

Solve the traveling salesman problem

To

4 a State Ford and Fulkerson's rule, (2)

b Draw the network : (5)

Activity :	P	Q	R	S	T	U
Predecessor :	-	-	-	P, Q	P, R	0, R

c Calculate earliest start, earliest finish, latest start and latest finish of each activity of the project and determine the critical path. (8)

Activity :	1-2	1-3	1-5	2-3	2-4	3-4	3-5	3-6	4-6	5-6
Duration :	8	7	12	4	10	3	5	10	7	4

OR

d A project consists of the following activities and time estimates (day) : (12)

Activity :	1-2	1-3	1-4	2-5	2-6	3-6	4-7	5-7	6-7
to:	3	2	6	2	5	3	3	1	2
to:	15	14	30	8	17	15	27	7	8
tm:	6	5	12	5	11	6	9	4	5

(i) Draw the network.

(ii) What is the probability that the project will be completed in 27 days?

e Describe the basic difference between PERT & CPM. (13)

5 a Explain types of Grammars, (5)

b Explain operation on languages, (5)

c Explain Regular languages. (5)

OR

d Find the DFA equivalent to the NFA for which the state table is given (12)

	t	
S	a	B
S <sub>0</sub>	0	S <sub>0</sub> , S <sub>1</sub>
S <sub>1</sub>	Q	S <sub>2</sub>
S <sub>2</sub>	S <sub>0</sub> , S <sub>1</sub> , S <sub>2</sub>	0

e Define finite state automata. (3)