

PSG COLLEGE OF ARTS & SCIENCE
(AUTONOMOUS)
BSc DEGREE EXAMINATION MAY 201[^]
(Second Semester)

Branch - STATISTICS

NUMERICAL METHODS

Time : Three Hours

Maximum : 75 Marks

SECTION-A (20 Marks)

Answer ALL questions

ALL questions carry EQUAL marks (10x 2 = 20)

- 1 Show that $(1+A)(1-V) = 1$ with usual notations.
- 2 State the formula for Newton's forward interpolation formula for equal intervals.
- 3 Define inverse interpolation.
4. State Everett's formula.
- 5 State Weddle's rule.
- 6 State Euler Maclaurin's formula.
- 7 What is the order of convergence of iterative process?
- 8 Define transcendental equation.
- 9' State the Runge - Kutta method of 2nd order for solving an ODE.
- 10 State the use of predictor and corrector formula. '

SECTION - B (25 Marks!)

Answer ALL Questions

ALL Questions Carry EQUAL Marks (5 x 5 = 25)

- 11 a Find the missing term in the following:

X:	1	2	3	4	5	6	7
Y:	2	4	8	-	32	64	128

OR

- b Find the values of Y at x = 21 from the following table

X:	20	23	26	29
Y:	0.3420	0.3907	0.4384	0.4848

- 12 a Derive Bessel's formula.

OR

- b From the following table, using Stirling's formula estimate the value of tan 16

X:	0°	5°	10°	15°	20°	25°	30°
Y = tan x:	0.0	0.0875	0.1763	0.2679	0.3640	0.4663	0.5774

- 13 a Derive Simpson's 3/8 rule.

OR

- b $\int \frac{dx}{M+x^2}$. Using trapezoidal rule with h = 0.2. Hence obtain an approximate value of n.

- 14 a Solve for a positive root of $x - x = 1$ correct to four decimal by Bisection method.

OR

- b Solve the equation $x^3 + x^2 - 1$ for the positive root by iteration method.

15 a Solve $\frac{dy}{dx} = x + y$, given $y(1) = 0$ and get $y(1.1)$ and $y(1.2)$ by Taylor series method. ■ y.

; OR

b Using Euler's method, solve numerically the equation, $y' = x + y$, $y(0) = 1$, for $x = 0.0(0.2)(1.0)$ check your answer with the exact solution.

SECTION - C (30 Marks)

Answer any **THREE** Questions

ALL Questions Carry **EQUAL** Marks (3 x 10 = 30)

■ ■ 16 -

Given x:	654	658	659	661
log ₁₀ x:	2.8156	2.8182	2.8189	2.8202

Find the value of k for 656 .

17 Using Lagrange's inverse interpolation formula, find the value of x when $y = 13.6$ from the given table

X:	30	35	40	45	50
Y:	15.9	14.9	14.1	13.3	12.5

$\int \frac{f(x)}{g(x)} dx$ by (i) Trapezoidal rule (ii) Simpson's rule (both),

Q 1 + x ^

Weddle's rule. Also check up the results by actual integration.

19 Find the positive root of $x^3 = 2x + 5$ by Regula Falsi method.

20 Given $\frac{dy}{dx} = -(1+x^2)y^2$ and $y(0) = 1$, $y(0.1) = 1.06$, $y(0.2) = 1.12$, $y(0.3) = 1.21$. Evaluate $y(0.4)$ by Milne's predictor corrector method. ■ .

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END.