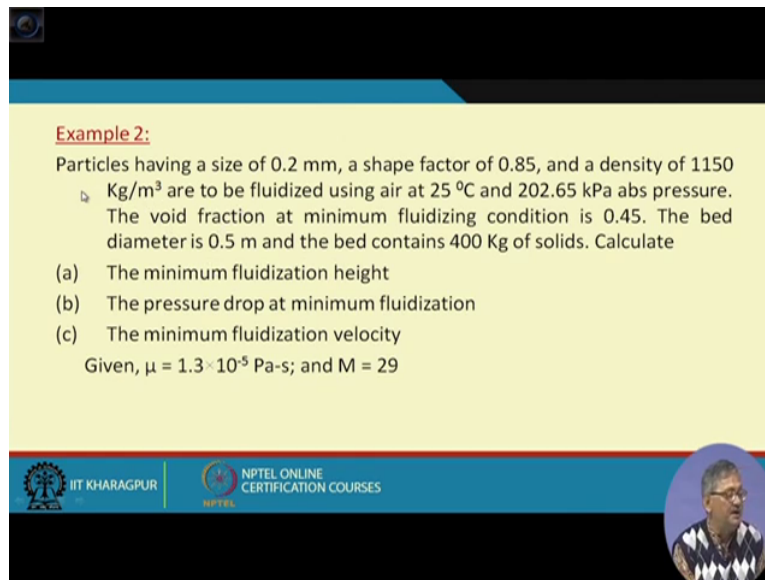


Momentum Transfer in Process Engineering
Professor Tridib Kumar Goswami
Department of Agriculture and Food Engineering
Indian Institute of Technology Kharagpur
Module 11
Lecture No 55
Problem of Fluidized bed Condition Part 2

So we have done one problem on fluidised bed and perhaps at the end because of the time constraint we asked you that you please try and hopefully you have tried, there was a quadratic equation in terms of say $A N Re^2 + B N Re - C$ that is equal to 0 by using that $(-B \pm \sqrt{B^2 + 4AC}) / 2A$ formula you can find out the root of a quadratic equation and you can find out $N Re$ from there and that $-B$ with the coefficients $-B \pm \sqrt{B^2 + 4AC}$ by $2A$, using this formula can find out what is the value of that $N Re$, so that you have hopefully done, so let us now do another problem say let us do another problem yeah.

So this is like this, Air at 390 Kelvin flows through a packed bed of cylinders having a diameter of 0.0127 meters and length the same as diameter no this we have already done so hopefully this one.

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Example 2:
Particles having a size of 0.2 mm, a shape factor of 0.85, and a density of 1150 Kg/m^3 are to be fluidized using air at 25 °C and 202.65 kPa abs pressure. The void fraction at minimum fluidizing condition is 0.45. The bed diameter is 0.5 m and the bed contains 400 Kg of solids. Calculate

- The minimum fluidization height
- The pressure drop at minimum fluidization
- The minimum fluidization velocity

Given, $\mu = 1.3 \times 10^{-5}$ Pa-s; and $M = 29$

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This is particles having a size of 0.2 millimetre, a shape factor of 0.85 and density of 1150 kg per meter cube are to be fluidised using air at 25 degree centigrade and 202.65 kilopascal absolute pressure. The void fraction at minimum fluidising condition is 0.45, the bed diameter is 0.5 meter and the bed contains 400 KG of solids. Calculate the minimum fluidisation height, the pressure drop at the minimum fluidisation, the minimum fluidisation

velocity. Given, viscosity of the fluid is 1.3×10^{-5} Pascal seconds and molecular weight is 29.

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Soln

$D_p = 0.2 \text{ mm} = 0.2 \times 10^{-3} \text{ m}$, $\phi_s = 0.85$, $\rho_p = 1150 \text{ kg/m}^3$
 $T = 25^\circ\text{C} = 298 \text{ K}$, $P_{in} = 202.65 \text{ kPa}$, $\epsilon_{mf} = 0.45$, $D = 0.5 \text{ m}$
 $m = 400 \text{ kg solid}$, $\mu_{air} = 1.3 \times 10^{-5} \text{ Pa.s}$, $M_{air} = 29$

Assuming zero porosity
 Bed volume = $\frac{400}{1150} = 0.3478 \text{ m}^3$

① $L_0 = \frac{0.3478}{\frac{\pi}{4} (0.5)^2} = 1.77 \text{ m}$. $L_{mf} = \frac{L_0}{1 - \epsilon_{mf}} = \frac{1.77}{1 - 0.45} = 3.22 \text{ m}$

② $\Delta P = L_{mf} (1 - \epsilon_{mf}) (\rho_p - \rho_g)$ $\rho = \frac{PM}{RT} = \frac{202650 \times 29}{8314 \times 298} = 2.32 \text{ kg/m}^3$

So I repeat the problem, particle having a size of 0.2 millimetre, a shape factor of 0.85 , so let us write D_p the solution when we do, let us write this way that D_p is 0.2 millimetre = 0.2×10^{-3} meter, shape factor that is $\phi_s = 0.85$, density ρ_p particle is 1150 KG per meter cube are to be fluidised using air at temperature, so T is 25 degree centigrade = 298 Kelvin and pressure inlet 202.65 kilopascal. The void fraction at minimum fluidising condition so $\epsilon_{mf} = 0.45$, the bed diameter so $D = 0.5$ meter and it contains 400kg of solids, so $m = 400$ kg solid. And given $\mu_{air} = 1.3 \times 10^{-5}$ Pascal seconds and molecular weight of air = 29.

So as we have done earlier here also that assuming 0 porosity we can write that the bed volume that can be written = 400 kg by 1150 that is equal to 400 divided by 1150 = 0.3478 meter cube. So if L_0 is the length corresponding to no porosity then L_0 becomes equals to this volume 0.3478 divided by the cross-sectional area that is $\frac{\pi}{4} D^2$ $\frac{\pi}{4}$ into it was 0.5 meters, so 0.5 square, so this becomes equal to 0.3478 divided by $\frac{\pi}{4}$ into 4 divided by 0.5 square, 1.77 meter. So if it is so then L_{mf} we can write equals to L_0 by $1 - \epsilon_{mf}$, so this is equal to 1.77 by $1 - 0.45$. So we can write 1.77 divided by $1 - 0.45$ so that is $0.55 = 3.218$, so we roughly can write 3.22 meter.

So if L_0 is known, L_{mf} is known then first one is done that one is the L_{mf} 3.22. Second one is ΔP that we can write as $\Delta P = L_{mf} (1 - \epsilon_{mf}) (\rho_p - \rho_g)$.

Now the question of Rho so we can write $\rho = \frac{PM}{RT}$ and P is given as yeah inlet so 202.65Kpa or 650 pascal, remove that decimal into M is 29 by 8314 into 298. So this comes to be equal to 202650 into 29 into 29 divided by is equal to divided by 8314 into 298 = 2.37 kg per meter cube, so this hopefully you can see kg per meter cube okay.

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$T = 25^\circ\text{C} = 298\text{K}, P_{in} = 202.65\text{ kPa}, \epsilon_{mf} = 0.45, D = 0.5\text{ m}$
 $m = 400\text{ kg solid}, \mu_{air} = 1.5 \times 10^{-5}\text{ Pa.s}, \mu_{w} = 2.9$
 Assuming zero porosity
 $\text{Porous volume} = \frac{400}{1150} = 0.3478\text{ m}^3$
 $L_{mf} = \frac{0.3478}{\frac{\pi}{4}(0.5)^2} = 1.77\text{ m}, L_{mf} = \frac{L_0}{1 - \epsilon_{mf}} = \frac{1.77}{1 - 0.45} = 3.22\text{ m}$
 $\Delta P = L_{mf} (1 - \epsilon_{mf}) (P_0 - P) g$
 $= 3.22 (1 - 0.45) (1150 - 2.37) 9.82$
 $= 19958.66\text{ Pa} = 199.58\text{ kPa}$
 $P_{out} = 202.65 - 199.58 = 3.07\text{ kPa}$
 $\rho = \frac{PM}{RT} = \frac{202650 \times 29}{8314 \times 298} = 2.37\text{ kg/m}^3$
 $\rho_w = \frac{202.65 + 3.07}{2} = 102.86\text{ kPa}, \rho_w = \frac{PM}{RT} = \frac{102860 \times 29}{8314 \times 298} = 0.12\text{ kg/m}^3$
 $\frac{D_i^3 \rho}{\mu^2} (P_0 - P) g \left(\frac{\rho_s (\epsilon_{mf})^3}{(1 - \epsilon_{mf})^2} \right) = 221.85$
 $1.77 \times 1150 + 150 \times 1150 - 221.85 = 0$

Now if Rho is so much, L mf we have found out 3.22 1 – 0.45 Rho p is 1150, Rho is 2.37 and g is 9.82, so this comes out to be 3.22 into 1 – 0.45 into 1150 – 2.37 into 9.82 = 19958.68 pascal, so we can say 199.58 kilopascal Delta p. So P out = 202.65 – 199.58 = 3.07 kilo pascal. So it appears to be a huge pressure drop 20062.2 yeah, it appears to be a huge pressure drop. So P out is there so you have got then average of P in and P out, P average = 202.65 + 3.07, did we do any mistake here?

199.58 kilopascal so this pascal 199.58 Delta P L mf 3.22 1 – 0.451 into 1150 2.37 9.82 so it is somewhere 1150 this is 0.6, we recheck this let us it is appearing a little absurd, 3.22 into 1 – 0.45 into 1150 – 2.37 into 9.82 = 19958 they have got Delta P 2.37 okay 202650 okay then we got 3.07kpa P 1 okay P average is 202 this by 2 = 3.07 into 101.325 this + oh 3.07 kilopascal sorry 3.07 kilopascal so 30700 3.07 kilopascal means or we can simply write 3.07 + 202.65 is equal to this divided by 2 = 102.86. I do not know this is appearing to be a little less kilopascal, so Rho average = $\frac{PM}{RT} = \frac{102.860}{8314} \times 29$ divided by 8314 into T 298, so that becomes into 100 = 102860 into 29 = this divided by 8314 divided by 298, 0.12 okay 0.12 kg per meter cube, this is appearing to be low very low.

Okay, now we know that $D^3 \rho = \mu^2 \rho - \rho \Phi s \epsilon$ into g into $\Phi s \epsilon$ mf square or cube $\Phi s \epsilon$ mf cube divided by $1 - \epsilon$ mf square. And this value if we take this should come to be 221.85 this value should come 221.85 then we can say that $1.75 N Re^2 + 150 N Re - 221.85 = 0$.

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$$N_{Re} = \frac{-150 \pm \sqrt{(150)^2 + 4 \times 1.75 \times 221.85}}{2 \times 1.75}$$

$$= 1.45$$

$$V_{mf}' = \frac{N_{Re} \mu (1 - \epsilon_{mf})}{D_p \rho \phi_s} = \frac{1.45 \times 1.3 \times 10^{-5} (1 - 0.45)}{0.2 \times 10^{-3} \times 2.25 \times 0.85}$$

$$= 0.027 \text{ m/sec.}$$

So from this equation we can find out the $N Re$ as $N Re = -B \pm \sqrt{B^2 - 4AC}$ that is $-150 \pm \sqrt{150^2 - 4 \times 1.75 \times 221.85}$ by $2A$, 2 into 1.75 this becomes equal to okay $150^2 + 4$ into 1.75 into 221.85 is equal to so much square root of this is so much. So if we make it $-$ then it becomes this $-$ and this $-$ into $-$ whereas, if we take it plus then it is $1 -$ and $1 +$ then it becomes $+$ that is meaningful so let us take it $+$ so -150 is equal to this divided by 2 into 1.75 is this is equal to 1.45 , so $N Re$ is 1.45 .

Now from there if we see that V_{mf}' is equal to that $N Re \mu (1 - \epsilon_{mf}) / D_p \rho \phi_s$. So $N Re$ is 1.45 into μ is 1.3×10^{-5} it was, $1 - 1.45 \epsilon_{mf}$, D_p is 0.2×10^{-3} into ρ , ρ we got somewhere some wrong but it should be 2.27 around or 2.25 into ϕ_s given 0.85 . So if we do this and see how much it is coming, it is 1.45 into 1.3 into 10^{-5} so much into $1 - 0.45$ is equal to this divided by 0.2 divided by 10^{-3} divided by 2.25 divided by $0.85 = 0.027$ meter per second. So we have found out that velocity, so velocity is coming to be 0.027 meter per second. Here we have shown that the quadratic equation which we got earlier here it was $1.75 N Re^2 + 150 N Re - 221.85 = 0$.

So this on simply on finding out the root N Re we got so $A X^2 + B X - C$ is got say + C + is here -, so that if we apply $-B \pm \sqrt{B^2 - 4AC}$ so that became + by 2 A, which came to be 1.45. Now from there V_{mf} prime was N Re was $\frac{\mu (1 - \epsilon_{mf})}{D_p \rho \phi_s}$, so from there we got this number and ultimately $V_{mf} = 0.027$ meter per second. So this way we can find out and do the problems and you must to some practices so that this kind of minimum fluidisation velocity or what is the height of the bed under minimum fluidised condition or what is the pressure drop that is in majority cases that is required, so what is the pressure drop that you can find out from the different relations under fluidised bed condition.

Mind it that fluidisation is very helpful to increase the surface area for any extend of heat or mass or whatever that depends on what you are choosing as the what you are choosing as the unit operation okay, thank you.