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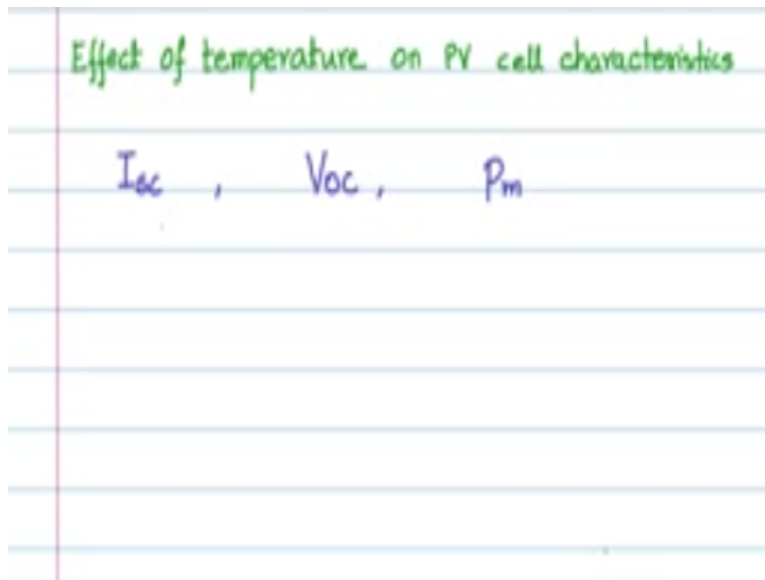
**Design of Photovoltaic Systems**

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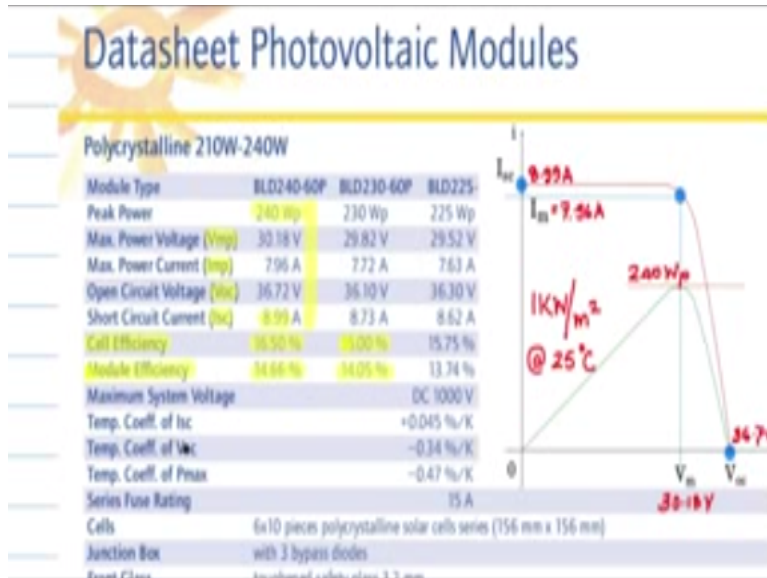
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In this clip let us look at the effect of temperature on the PV cell characteristics there are 3 important parameters one is  $I_{sc}$  the short circuit current and then you have the  $V_{oc}$  open circuit voltage and you have  $P_m$  the max power of the Pv cell or the peak power of the Pv cell now how does these 3 important parameters vary with temperature let us now have a look at the data sheet and see what are the number and what are the values they give.

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Here in this data sheet you see here there are 3 parameters temperature, coefficient of Isc short circuit current temperature coefficient of Voc temperature coefficient of P max these are the 3 parameters that we would be discussing now see the temperature coefficient Yac is + 0. 045 %/ degree Kelvin and the temperature coefficient of Voc is – 0.34%/ degree k which means that as the temperature increases Voc will decrease same way P max this is understandable because the temperature coefficient of Isc is positive temperature coefficient of Voc is negative the temperature coefficient of power which a product of current and voltage will also be negative.

And that is given as – 0.47%/ degree K, so let us study bit on how these temperature coefficients come about and what is there relationship with respect to temperature.

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## Effect of temperature on PV cell characteristics

$I_{sc}$  ,  $V_{oc}$  ,  $P_m$

### Effect of temperature on $I_{sc}$

$I_{sc} \approx I_p \rightarrow \text{photocurrent} \propto \text{Insolation (kW/m}^2\text{)}$

$I_{sc} \uparrow$  as  $T \uparrow$  0.1% per  $^{\circ}\text{K}$ .

With regard to  $I_{sc}$  we know that we have seen in an earlier clip that  $I_{sc}$  is approximately equal to the photo current  $I_p$  which is the photocurrent and the photocurrent is directly proportional to the insolation, which is nothing but the power /  $\text{m}^2$  of the incident solar radiation. So if you see this from this relationship, with an increase in temperature, what will happen to  $I_{sc}$  with an increase in temperature? The photocurrent will increase.

Why should the photocurrent increase? The band gap energy reduces as the band gap energy was 1.16 electron volts and it will come down, and this will allow more wavelengths of electrons to jump into the conduction band. Any way, there are more free electrons, and as a result, more photocurrent and therefore a higher value of  $I_{sc}$ , short circuit current. So in summary, for the short circuit current, the short circuit current  $I_{sc}$  increases as temperature increases. And this is a very small value; it is around 0.1% /  $^{\circ}\text{K}$  or /  $^{\circ}\text{C}$  / silicon.

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### Effect of temperature on Voc

$$V_{oc} = nV_T \ln\left(\frac{I_p + I_0}{I_0}\right)$$

$$V_{oc} = nV_T \ln\left(\frac{I_p}{I_0}\right)$$

$$I_0 \propto T^m e^{-\frac{V_{G0}}{nV_T}}$$

$$\frac{dV_{oc}}{dT} = \frac{V_{oc} - (V_{G0} + mnV_T)}{T}$$

$m = 1.5$   
 $n = 2$   
 $V_T = 0.026 \text{ V @ } 300^\circ\text{K}$   
 $T = 300^\circ\text{K}$   
 $V_{oc} = 0.6 \text{ V}$

$-2.1 \text{ mV}/^\circ\text{K}$

We pick of to the effect of temperature on Voc the open circuit voltage we seen the relationship of Voc with the photocurrent which is given like this and we have seen this equation earlier in another video clip so it is given as this relationship where this is  $nV_T$  n is to for silicon  $V_T$  is the voltage equivalent of temperature logarithm of  $I_p$  the photo current  $I_0$  is the reverse saturation current by  $I_0$  if you take  $I_0$  very small compare to the photocurrent then we can say Voc is =  $nV_T$  logarithm of  $I_p$  of /  $I_0$  the reviser saturation current.

So apparently if you look at this equation it is not directly evident that Voc will decrease if temperature increases however you should note that  $V_T$  is a function of temperature where as  $T/11600$   $I_0$  is also a function of temperature it is an exponential function of temperature so considering  $I_0$  and  $V_T$  effect together you will see that Voc is inversely proportional to temperature the reverse saturation current  $I_0$  is proportional to temperature to the power of m  $e^{V_{G0}}$  recall  $V_{G0}$  was the numerically voltage equivalent of the band gab energy by an  $V_T$  So you see the dependence of  $I_0$  on temperature and substituting this and then trying to find  $dV_{oc}/dT$  we get  $dV_{oc}/dT$  as  $V_{oc} - V_{G0} + mnV_T$  hole over T so you see that for a given temperature we can calculate the rate Voc will change with temperature now if we take values typical values for silicon let us say for silicon  $m = 1.5$   $n = 2$ ,  $V_T = 0.026 \text{ mv}$  or  $26 \text{ v @ } 300^\circ\text{ k}$  how take temperature as  $300^\circ\text{ k}$  and you will and Voc as  $0.6 \text{ v}$  or a certain cutting voltage.

And you will see that if you apply all these to the above formula you will get approximately –  $2.1 \text{ mV}/^\circ\text{ K}$  what it means that for every cell an junction P variation of the open circuit voltage Voc with temperature is –  $2.1\text{mV}/^\circ\text{ K}$   $1^\circ\text{ C}$  rising temperature will make Voc to fall by  $2.1\text{mV}$

how did we get this equation I will quickly run through the derivation you can use the pass mode and try to study how the relationship is with effect of temperature of Voc came about.

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$$= m \ln(kT) + \left( \frac{-V_{G0}}{nV_T} \right)$$

$$\ln(I_p) = m \ln(kT) + m \ln(kT) - \left( \frac{V_{G0}}{nV_{T000}} \right)$$

Differentiating w.r.t T,  $\frac{d(\ln I_p)}{dT} = \frac{m}{T} + \frac{V_{G0}}{nTV_T} \quad \text{--- } \textcircled{1}$

$$V_{oc} = nV_T \ln\left(\frac{I_p + I_0}{I_0}\right) \approx nV_T \ln\left(\frac{I_p}{I_0}\right) \quad \text{as } I_p \gg I_0$$

$$\frac{V_{oc}}{nV_T} = \ln\left(\frac{I_p}{I_0}\right) = \ln(I_p) - \ln(I_0)$$

Differentiating w.r.t T

$$\frac{d}{dT} \left( \frac{V_{oc}}{nV_T} \right) = \frac{d(\ln I_p)}{dT} - \frac{d(\ln I_0)}{dT}$$

So here I have the derivation for  $dV_{oc} / dT$  the derivation is simple but I am not going to explain every step I will just run through it you can use the pause mode on the video clip and read it at your convinces the reverse saturation current  $V$  so was five was given by  $I_0 = K T^m e^{-V_{G0}/nV_T}$  where  $G_0$  is the numerically voltage equivalent of the van gab energy  $m$  is 1.5 for silicon  $n$  is 2 for silicon and  $V_T$  the temperature equivalent to the voltage.

Now for this equation take  $dL$  logarithm and you will see that it falls into this kind of a relationship and logarithm of  $I_0$  is given like this then this equation you differentiate with respect to temperature  $T$  so differentiating with respect to temperature you will land up with  $m / T + V_{G0}/ nTV_T$  so keep this equation a side next come to the  $V_{oc}$  relationship we say that  $V_{oc}$  is =  $nV_T$  logarithm of  $I_p + I_0/I_0$  and if we take  $I_p$  greater than much greater than  $I_0$  you will see that it is equal to  $nV_T$  log of  $I_T/ I_0$  and this the relationship that falls as the next step.

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$$V_{oc} = n V_T \ln\left(\frac{I_p + I_0}{I_0}\right) = n V_T \ln\left(\frac{I_p}{I_0}\right) \quad \text{as } I_p \ll I_0$$

$$\frac{V_{oc}}{n V_T} = \ln\left(\frac{I_p}{I_0}\right) = \ln(I_p) - \ln(I_0)$$

Differentiating w.r.t T

$$\frac{d}{dT} \left( \frac{V_{oc}}{n V_T} \right) = \frac{d}{dT} \{ \ln(I_p) \} - \frac{d}{dT} \{ \ln(I_0) \}$$

$$\bullet \quad -\frac{V_{oc}}{n V_T} + \frac{1}{n V_T} \frac{dV_{oc}}{dT} = -\left( \frac{m}{T} + \frac{V_{oc}}{n V_T} \right) \quad \text{from } \textcircled{1}$$

$$\text{Simplifying, } \frac{dV_{oc}}{dT} = \frac{V_{oc}}{T} - \left( \frac{m n V_T}{T} + \frac{V_{oc}}{T} \right)$$

Now differentiate that differentiating this equation with respect to temperature you get  $d/dT$   $V_{oc} / n V_T$   $dT / \log$  of  $I_T - d/dT$   $\log$  of  $I_0$  now  $d/dT$   $\log$  of  $I_0$  we have all ready derived here so we can directly substitute this value here  $d/dT$  of  $\log$  of  $I_T$  is 0 assuming that the variation is good negligible come compare to variation and  $I_0$ , so as you are having numerator as you are having 2 terms  $V_{oc}$  dependent on temperature and  $V_T$  dependent on temperature splitting it up single product rule. You get this relationship and then simplifying.

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$$\frac{d}{dT} \left( \frac{V_{oc}}{nV_T} \right) = \frac{1}{nV_T} \frac{dV_{oc}}{dT} = - \left( \frac{m}{T} + \frac{V_{G0}}{nV_T} \right) \text{ from } \textcircled{1}$$

Simplifying,  $\frac{dV_{oc}}{dT} = \frac{V_{oc}}{T} - \left( \frac{m n V_T}{T} + \frac{V_{G0}}{T} \right)$

$$\frac{dV_{oc}}{dT} = \frac{V_{oc} - (V_{G0} + m n V_T)}{T}$$

for Si  $m=1.5$ ,  $n=2$   $V_{G0} = 1.16$ ,  $V_{oc} = 0.6$

$$\frac{dV_{oc}}{dT} = \frac{0.6 - (1.16 + 3V_T)}{T} = \frac{-0.56 - 3V_T}{T}$$

at  $T = 300^\circ\text{K}$   $\frac{dV_{oc}}{dT} = -2.12 \text{ mV}/^\circ\text{K}$

You will see that  $dV_{oc} / dT = V_{oc} - V_{G0} + mn V_T / T$  and this is what I had mentioned earlier the see weather almost inverse proportionality of  $V_{oc}$  with  $T$  now for silicon if you substitute  $m = 1.5$   $n = 2$   $V_{G0} = 1.16$  electron volts and  $V_{oc} 0.6$  you will land up with  $T \text{ voc} / dT$  as this value and for a temperature of  $300^\circ \text{K}$  the rate at which  $V_{oc}$  changes it  $-2.120 \text{ v} / ^\circ \text{k}$  which mean that for very degree rising temperature open circuit voltage falls by approximately 2mv.

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### Effect of temperature

$V_{oc} \downarrow$  as  $T \uparrow$  -ve temp co-eff

$I_{sc} \uparrow$  as  $T \uparrow$  +ve temp co-eff

power =  $v \cdot i$  -ve temp co-eff

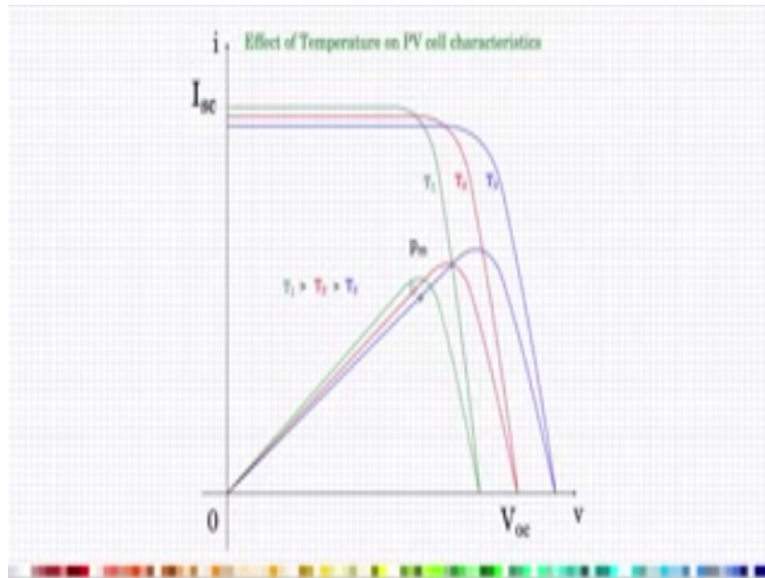
$\Rightarrow P_m \downarrow$  as  $T \uparrow$

Therefore in the case of  $V_{oc}$  we see that  $V_{oc}$  will decrease as temperature increases per as in the case of short circuit current  $I_{sc}$  we saw that  $I_{sc}$  increases as temperature increases and in the case of power being a product of  $v \times i$  as  $V_{oc}$  is having a negative temperature coefficient and  $I_{sc}$  is having a positive temperature coefficient so this is negative temperature coefficient this is positive temperature coefficient.

Power will also have a negative temperature coefficient this means this would imply that  $P_m$  would decrease as temperature increases so these are the main effects that you would see on the Pv cell parameters due to variation in temperature.

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Consider this Iv characteristic of a Pv cell and let us study the effect of temperature on the cell characteristic we have this Iv curve taken at standard insolation of  $1 \text{ kW} / \text{m}^2$  and standard temperature of  $25^\circ \text{C}$  now let us say the temperature increases and the temperature increases from  $25^\circ \text{C}$  TO  $40^\circ \text{C}$  what is the effect on the cell now let me make a duplicate of this curve let me change color to green and super impose the changed curve the  $I_{sc}$  will vary slightly and it will increase with increase in temperature that is what we studied.

And what happens to  $V_{oc}$  would decrease with increasing temperature and it will decrease in inverse ratio so the changed characteristic Pv cell characteristic curve would look like this the one shown in green so as temperature increases the characteristics shift in this manner now consider the temperatures replaced with variables  $T_1$  and  $T_2$  where  $T_2$  is the lower temperature and  $T_1$  is the higher temperature now what would happen and how will the curve look like if we have 3<sup>rd</sup> curve which is set at a temperature  $T_3$

Such that  $T_1 > T_2 > T_3$ ,  $T_3$  is a lower temperature much lower than  $T_1$  and  $T_2$  so we would expect the curve of a  $V_{oc}$  to be on this side of  $T_2$  the red line and for  $I_{sc}$  because the temperature is lower we would expect it will be low the red line so this is the curve that is expected for the interviewee: characteristic which is set at a temperature  $T_3$  now looking at the our curve now this is the power curve for the  $T_3$  curve.

And this is the peak power that the service get low of giving at temperature  $T_3$  now a temperature  $T_2$  and  $T_1$  the corresponding power curves or like this and you see that the peak

powers or decreasing so as the temperature is increasing you will see that the peak powers reduce like this is also calibrating what we just studied that  $V_{oc}$  decreases with increase in temperature  $I_{sc}$  short circuit current increases with temperature and it is product the peak power decreases with temperature.