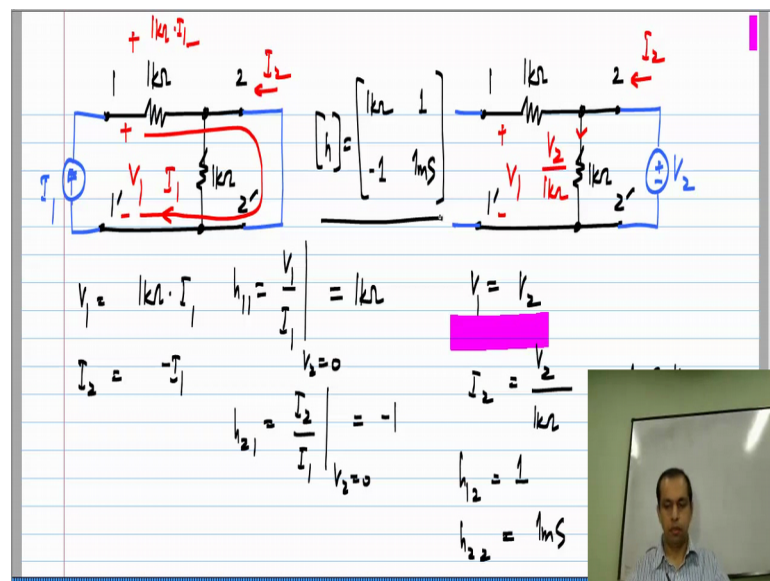


Basic Electrical Circuits
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Lecture - 86

Now, we will calculate h parameters for some examples circuit as usual we will take the same circuit as we did for the other two parameters, so that you can compare the results.

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This is the circuit for, which I would like to compute the h parameters port 1, port 2 and any two cases one invites port 2 is short circuited and you apply a current to port 1 and the second case, where port 1 is open circuited and you apply a voltage 2 port 2. Now, this is kind of getting repetitive, so those of you her very familiar with circuit analysis I suggest that you simply calculate the h parameters of this and forward to the end of the lecture and see if they match whatever I derive, if you are not very comfortable with circuit analysis and these parameter definitions and so on, so you can follow the lecture.

Again, I would still encourage you to do the calculations first, but we can follow the lecture completely. So, now, what I need to evaluate in this are I 2 in this direction and V 1 the same for both circuits I 2 and V 1. So, let us take the first circuit over here, this short circuit across port 2 is shorting out this 1 kilo ohm resistor. So, no current flows through this 1 kilo ohm and all of I 1 flows in that direction, flows that way.

So, this V_1 is nothing but, the voltage drop across this 1 kilo ohm resistor, which is 1 kilo ohm times I_1 , so after that we have a short circuit. So, V_1 is 1 kilo ohm times I_1 and I_2 you can see that it is simply the opposite of this current I_1 . So, I_2 is minus I_1 and from these two, what do we get h_{11} is V_1 by I_1 with V_2 set to 0, which comes out to be 1 kilo ohms and h_{21} , which is I_2 by I_1 with V_2 set to 0 and this comes out to be minus 1.

So, you can see that h_{11} has dimensions of resistance and h_{21} is dimensionless it is the current gain from port 1 to port 2. Now, coming to the second case over here, so here this 1 kilo ohm is in series with an open circuit, so no current flows through that all of this I_2 is simply the current through this 1 kilo ohm. And V_2 appears across the 1 kilo ohm resistor, so the current here is nothing but, V_2 divided by 1 kilo ohm and V_1 equals V_2 , because no current is flowing through this 1 kilo ohm resistor.

So, we have V_1 to be equal to V_2 and I_2 to be equal to V_2 divided by 1 kilo ohm or 1 Millisiemens times V_2 . From these two you clearly see that h_{12} is 1 that comes from this equation and h_{22} is 1 Millisiemens that comes from this equation. So, the h parameter matrix for this circuit as expected has hybrid quantities, the resistance here is 1 kilo ohms and this is just one, this is minus 1 and there we have 1 Millisiemens, so that is the h parameter matrix of this circuit.

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$V_1 = 1k\Omega \cdot I_1$ $h_{11} = \frac{V_1}{I_1} \Big|_{V_2=0} = 1k\Omega$
 $I_2 = -I_1$ $h_{21} = 1$

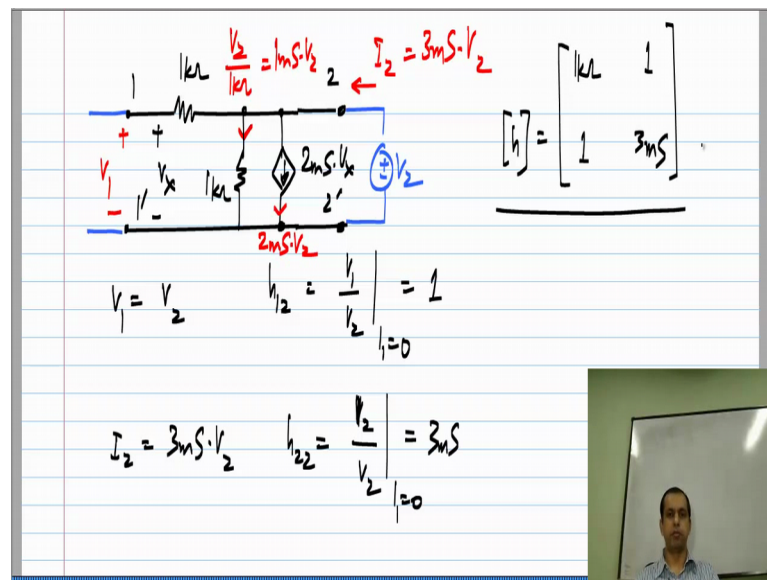
So, again taking a more complicated example with a current control source, we can also calculate the h parameters h_{11} , h_{12} and h_{21} times V_x , where V_x over here. And for the first case we said V_2 equal to 0 or short circuit port 2 apply a current I_1 and we want to find this voltage V_1 and that current I_2 . So, how do we do this, first of all is I_1 simply flows through this 1 kilo ohm . So, across this we have I_1 times 1 kilo ohm .

Now, you see that there is a short circuit from here to there, so the voltage V_1 is simply the voltage across this 1 kilo ohm resistor. So, V_1 is 1 kilo ohm times I_1 or $h_{11} I_1$, which is V_1 by I_1 with port 2 shorted is 1 kilo ohm . Now, because of the short circuit, no current flows through this 1 kilo ohm resistor whatever I_1 was there, so this I_1 flows into this 1 kilo ohm and through the short circuit.

So, I_1 flows that way, but that is not the only current that flows there, because we have the control source as well and how much of the control source 2 Millisiemens times V_x and V_x is nothing but, V_1 and V_1 is 1 kilo ohm times I_1 . So, this current over here, which flows in this direction also through the short circuit, because there is a short circuit across the control current source and all of it is current will flow through the short circuit will be remember it is an opposite direction to I_1 and that is 2 Millisiemens times V_x , which is V_1 , which is 1 kilo ohm times I_1 , which is $2 I_1$.

So, we have I_1 flowing directly this way and $2 I_1$ flowing them. So, the actual current that is flowing in this short circuit, the total current I just showed this I_1 over there it is not the current flowing here that actual current flowing there is the sum of I_1 , which is coming from there and $2 I_1$ which is going there which is equal to I_1 flowing that way. So, I_2 will be exactly equal to I_1 in this particular case if this control source as different proportionality constant it would be different. So, we have I_2 equals I_1 , which tells you that h_{21} is nothing but, 1. So, that is the value h_{21} the current gain from port 1 to port 2.

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Now, for the second case we have port 1 open circuited and a voltage V_2 apply to port 2, where V_x appears there. So, again we have to calculate this current I_2 and this voltage V_1 and you see that V_x is the same as V_1 and also no current flows to the 1 kilo ohm resistor, so the voltage V_2 here is exactly the same as V_1 . So, we have V_1 equals V_2 , which tells you that h_{12} , which is V_1 by V_2 with port 1 open circuited a simply 1.

So, now, we have to calculate I_2 first of all this V_2 appears across the 1 kilo ohm resistor. So, we have V_2 by 1 kilo ohm or 1 Millisiemens times V_2 flowing through the resistor and we also have 2 Millisiemens times V_x , which is 2 Millisiemens times V_1 , V_1 is the same as V_x which is also the same as V_2 . So, the current here as 2 Millisiemens times V_2 . So, the total current I_2 is 3 Millisiemens times V_2 , so I_2 is 3 Millisiemens times V_2 , so h_{22} is I_2 by V_2 with port 1 open circuited, which is 3 Millisiemens.

The h parameter matrix of this is h_{11} , which is 1 kilo ohm h_{12} which is 1 h_{21} , which is also 1 and h_{22} , which is 3 Millisiemens, so that is the h parameter matrix. So, again you should be able to calculate this easily calculating of the two port parameters is simply regular circuit analysis.