

Basic Electrical Circuits
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Lecture - 85

Now, we looked at y parameters, where the voltages are taken as independent variables and current as dependent variables and z parameters, where the currents for independent variables and the voltages where the result of those currents. And there is no need to take voltages on both sides to be independent variables or currents on both sides, we can make some much.

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resistance

dimensionless

hybrid parameters

conductance

$$V_1 = h_{11} I_1 + h_{12} V_2$$

$$I_2 = h_{21} I_1 + h_{22} V_2$$

$$\begin{bmatrix} V_1 \\ I_2 \end{bmatrix} = \begin{bmatrix} h_{11} & h_{12} \\ h_{21} & h_{22} \end{bmatrix} \begin{bmatrix} I_1 \\ V_2 \end{bmatrix}$$

Now, let us say we have a two port and we think of applying a current to port 1 and a voltage to port 2. Now, the voltage here V_1 and the current over there I_2 will also be linear combinations of independent sources that are applied. And in this particular case, when we take I_1 that is current on port 1 and the voltage on port 2, the set of parameters we get are called h parameters. So, we have V_1 to be $h_{11} I_1$ plus $h_{12} V_2$ and we have I_2 to be $h_{21} I_1$ plus $h_{22} V_2$.

In other words, this vector $V_1 I_2$ equals $h_{11} I_1, h_{12} V_2, h_{21} I_1, h_{22} V_2$ times the vector $I_1 V_2$. Now, this is denoted by the letter h to denote that they are hybrid. So, these are known as hybrid parameters and they are hybrid parameters, because this voltage equals h_{11} times a current. So, h_{11} has dimensions of resistance, this voltage equals h_{12} times V_2

2, so h_{12} is dimensionless. So, this has dimensions of resistance that is dimensionless this is; obviously, for dimensional consistency.

Similarly, in the second expression I_2 equals h_{21} times I_1 , so this has to be dimensionless h_{21} . So, this is also dimensionless and finally, this is a current equaling something times a voltage, so h_{22} has dimensions of conductance. So, the four parameters do not have the same dimensions, so they are called hybrid parameters. Now, evaluation of this is exactly in the same as earlier, you set one of the independent variables to 0 and evaluate them. As before you can take four different sets of the independent variables and evaluate everything, but the most convenient thing is to set one of them to be 0.

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$V_2 = 0$: short circuit port #2

$V_1 = h_{11} I_1$ $h_{11} = \frac{V_1}{I_1} \Big|_{V_2=0}$ resistance looking into port 1 with port 2 shorted

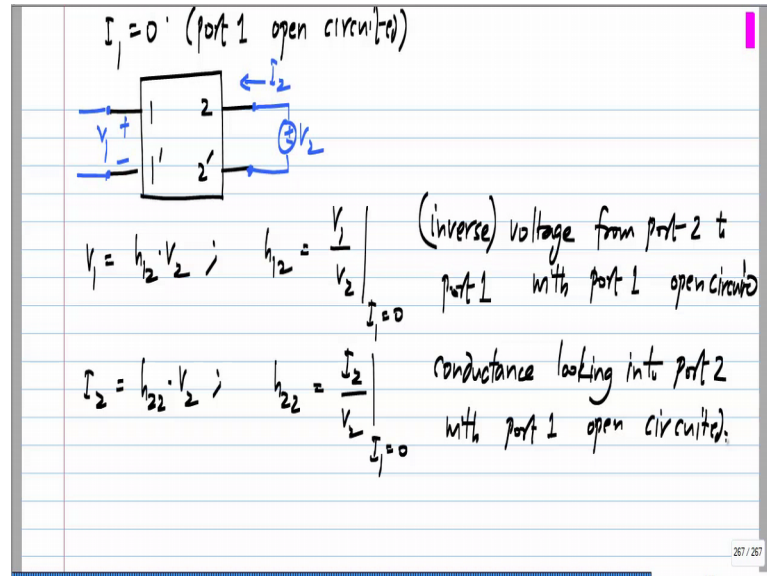
$I_2 = h_{21} I_1$ $h_{21} = \frac{I_2}{I_1} \Big|_{V_2=0}$ current gain from port 1 to port 2 with port 2 shorted

So, in the first case we set V_2 to 0; which means, your short circuit port number 2 and you apply I_1 to this side and you measure V_1 and I_2 . So, what do we get with V_2 set to 0? We have V_1 to be $h_{11} I_1$, in other words h_{11} is simply V_1 by I_1 or the resistance looking into port 1 with port 2 short circuited. And similarly, we have from the second equation I_2 is h_{21} times I_1 or h_{21} is simply I_2 by I_1 , that is the current gain from port 1 to port 2 with port 2 short circuited.

So, this is resistance looking into port 1 with port 2 short circuited and h_{21} is the current gain from port 1 to port 2 with port 2 shorted. The general principle is always the

same, you set one of the independent variables to 0 and apply stimulate on the other side and evaluate two of the parameters.

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Similarly, we set I_1 to 0; which means, we are open circuiting port 1. If I set I_1 to 0, it means that port 1 is open circuited and then, you apply V_2 and you measure both I_2 and V_1 . So, V_1 would be just h_{12} times V_2 , because I_1 is 0 and from this we get h_{12} to be V_1 by V_2 with port 1 open circuited and this is nothing but, this is called the inverse voltage gain, that is the voltage gain from port 2 to port 1 with port 1 open circuited and we get I_2 to be h_{22} times V_2 , in other words h_{22} is I_2 by V_2 with I_1 set to 0 or port 1 open circuited and I_2 is nothing but, conductance looking into port 2 with port 1 with open circuited, so these are the hybrid parameters.

Now, it turns out that this hybrid parameters for useful for describing a particular type of transistor, like I said you could use any parameter set for any element. Sometimes, some of them will have infinite values and not useful and even when all of them do exist, some or more convenient than others. Now, previously there was a particular type of transistor known as the bipolar junction transistor to describe the small signal model of the bipolar junction transistor, this h parameter was widely used, but actually the current style is to use y parameters, the admittance parameters for both the bipolar transistor and the MOS transistor. So, you will see those things when you take a course on active circuits that is, amplifiers using bipolar transistors and MOS transistors.