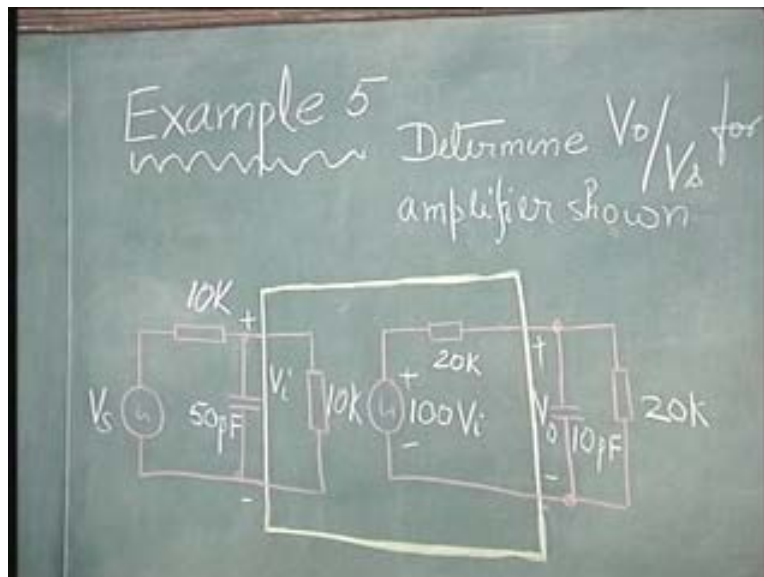


Electronics for Analog Signal Processing - I
Prof. K. Radhakrishna Rao
Department of Electrical Engineering
Indian Institute of Technology – Madras

Lecture - 18
Frequency Limitations of an Amplifier

In the last class, we were exposed to the frequency limitation of amplifiers. Let us consider this example now, which illustrates how the so called gain characteristic of the amplifier gets limited.

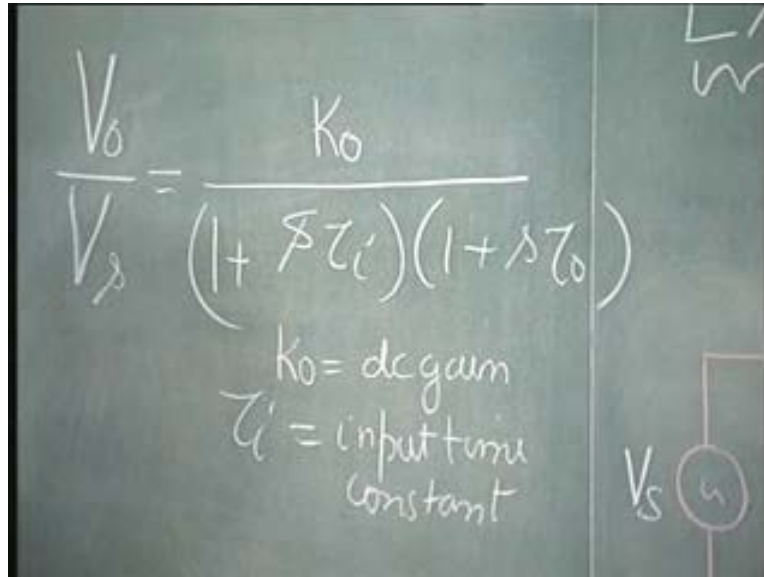
(Refer Slide Time: 01:45)



Determine V_o/V_s , V_o/V_s , that is, the amplifier gain for the amplifier shown, wherein, apart from the usual input impedance, source impedance, output impedance and the load impedance, we have the effect of stray capacitance; one at the output, 10 picofarad, one at the input, 50 picofarad. The input capacitor, total together, comes out to be 50, let us say; and the output capacitor comes out to be 10 picofarads. This is the typical order of the amplifier capacitors.

Now, under this circumstance, I would like to know V_0 over V_s . Now, you can write down the different group equations, etcetera and solve it; but, I would like to solve this by just observation.

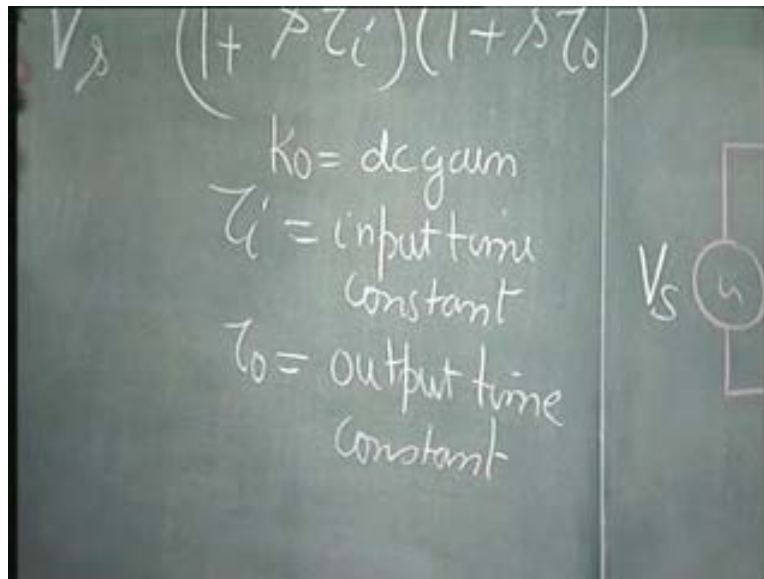
(Refer Slide Time: 03:40)



The image shows a chalkboard with a handwritten transfer function. The equation is
$$\frac{V_0}{V_s} = \frac{K_0}{(1 + s\tau_i)(1 + s\tau_o)}$$
 Below the equation, there are handwritten definitions: $K_0 = \text{dc gain}$ and $\tau_i = \text{input time constant}$. To the right of the text, there is a simple circuit diagram showing a voltage source V_s connected to a load, with a small circle containing a tilde symbol (\sim) next to it. In the top right corner of the chalkboard, there are some faint handwritten marks that look like 'L' and 'S'.

In all these cases, I have told you that the amplifier gain comes out as K_0 , which is independent of frequency, divided by $1 + s\tau_i$, $1 + s\tau_o$. This is the input time constant, τ_i is the input time constant; K_0 is the dc gain. I discussed, independent of frequency, dc gain; τ_i is the input time constant, and τ_o is nothing but the output time constant.

(Refer Slide Time: 03:52)



So, for any amplifier, this can be written this way. If there are 2 time constants, if there are 3 time constants, let us say, you have one amplifier cascaded to another amplifier; then, there will be an input time constant, an intermediate time constant and an output time constant. If we have, instead of 2 stages, 3 stages; then correspondingly, there will be 4 time constants.

If there is a single stage, there will be 2 time constants, at least. 2 stages - 3 time constants: input, intermediate, output; 3 stages - 4 time constants; n stages - at least, n plus 1 time constants.

So, this **this** is something that you can remember. That, depending upon the number of stages, we can say what is the order of the system. This is called first stage; if it has 2 time constants, it is called a second order system, second order. This is a third order; this is a fourth order, amplifier system.

(Refer Slide Time: 05:36)

V_o for the

time constants	order of system
1 stage two	2nd
2 stages three	3rd
3 stages four	4th
n stage (n+1)	

The order of the system is dependent upon the number of time constants. The first stage is already a second order system. There is nothing like first order at all. Second stage corresponds to third order, minimum. Third stage corresponds to fourth order system. So, order depends upon the number of poles. These are called the poles of the system. These are called the poles. There are no zeros here. These concepts, you have learned in your Control Engineering. These are called poles of the system.

(Refer Slide Time: 06:13)

Example

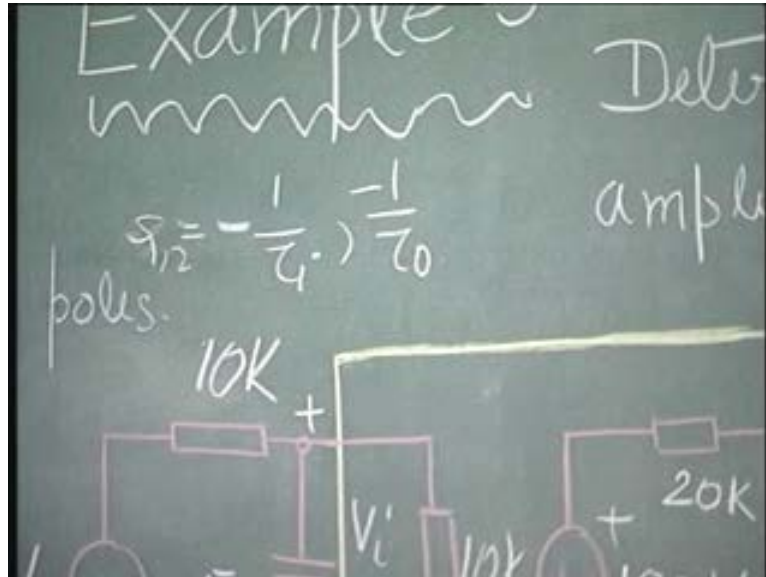
$$\frac{V_o}{V_i} = \frac{K_o}{(1 + s\tau_i)(1 + s\tau_o)}$$

poles.

$K_o = \text{dc gain}$
 $\tau_i = \text{input time constant}$
 $\tau_o = \text{output time constant}$

The poles are located at ω equal to, or actually, s equal to minus 1 over τ_i ; s^2 and 1 over τ_{naught} . Equate this to zero; you will get the pole. s is equal to minus 1 over τ_i is one pole; and minus 1 over τ_{naught} is the other pole.

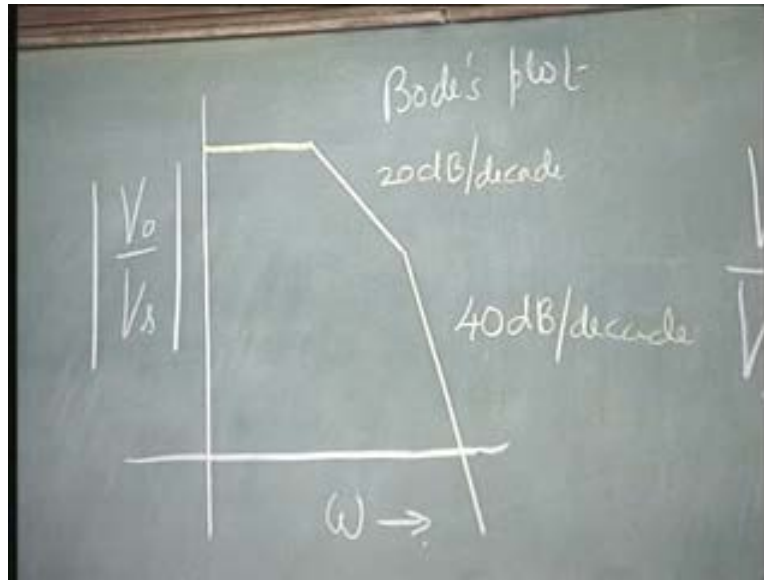
(Refer Slide Time: 06:46)



The poles of this system always rely on the negative real axis. The poles of this... such systems will always lie on the negative real axis. This corresponds to negative real axis. So, of the s domain; s domain has real part and imaginary part; in that, it will lie on the negative real axis. So, this is a two pole system or a second order system. There are 2 time constants connected with this system and we have obtained the Bode's plot in the last class.

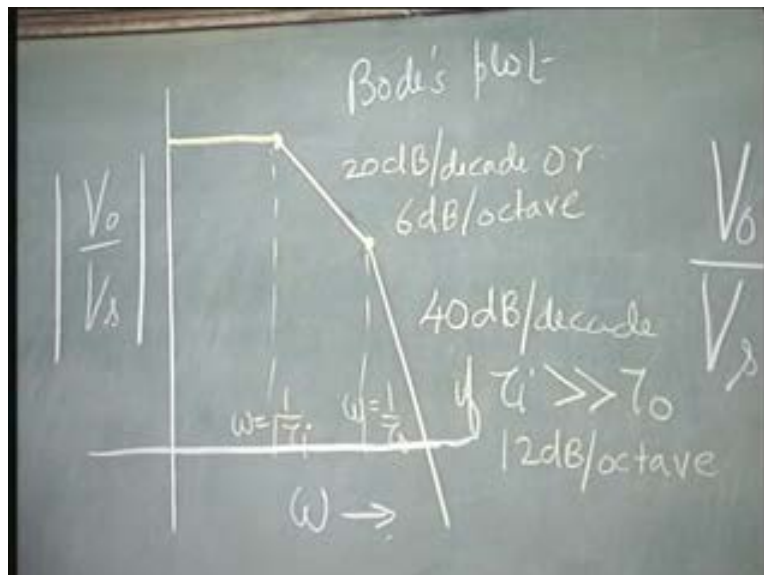
We have seen that a Bode's plot for the magnitude of V_{naught} over V_s versus ω will look like... these are asymptotic; K_{naught} which is independent of frequencies at low frequencies. At frequencies much lower than $1/\tau_i$ and $1/\tau_{naught}$, the constant equal to K_{naught} ; and then, it will decrease at... we have discussed this - 20 decibels per decade, 20 decibels per decade; and then, the next time constant will bring about 40 decibels per decade attenuation. All these things we have understood.

(Refer Slide Time: 08:36)



So, assuming that this is the dominant time constant and this is less dominant; so, we can say that, for example, if τ_i is much greater than τ_{naught} , then this corresponds to ω equal to $1/\tau_i$ and this corresponds to ω equal to $1/\tau_{naught}$. These are called corner frequencies. In the last class, we have understood. These are called corner frequencies. This fall off is a 20 decibels per decade; this is at 40 decibels per decade; or 6 decibels per octave, 12 decibels per octave.

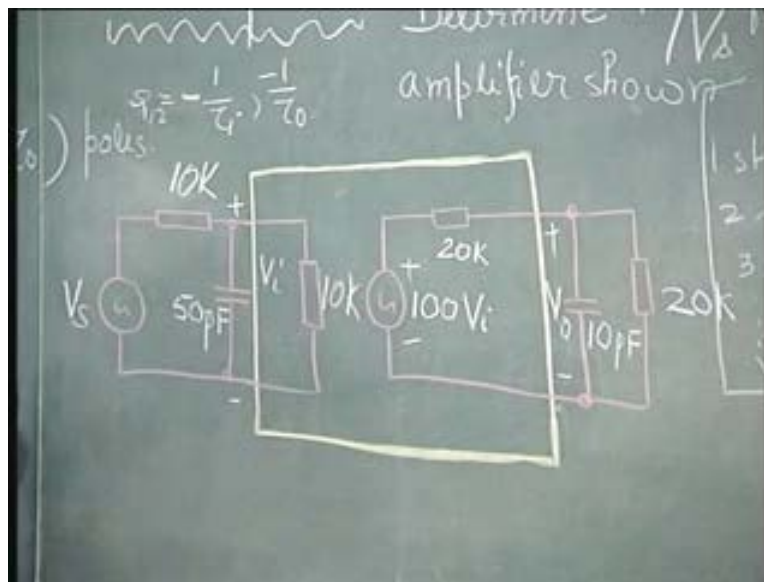
(Refer Slide Time: 09:42)



So, this is what we have seen. We have understood how, therefore, the frequency response characteristic of any amplifier will change. Now, let us take this for the example that is chosen; how much it is going to be. What is K_{naught} ? How do you evaluate K_{naught} ?

Now, I would not like to write down any equation. Look at this circuit. K_{naught} ... you forget about the existence of the capacitor.

(Refer Slide Time: 10:14)



It is ((frequency... Refer Slide Time: 10:10)). So, V_i is going to be half of V_s because you have 10 K here, 10 K here; V_i is going to be half of V_s . Again, that half of V_s is going to be multiplied by 100; so, 50 times V_s appears here. That 50 times V_s again is going to be halved because you have 20 K, 20 K; so, we have 25 times V_s . So, K_{naught} is 25.

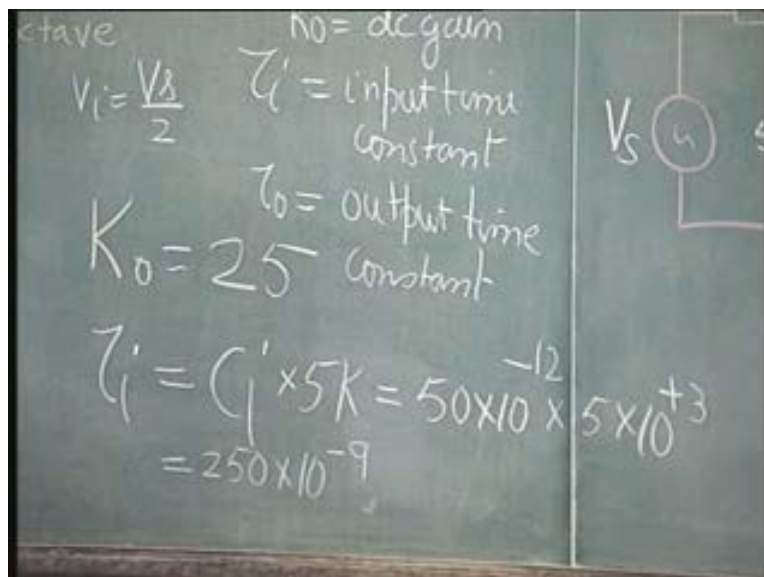
Again, let us go through this. V_s is going to be halved and appears here as V_s by 2. So, V_i is equal to V_s by 2. So, V_i equal to V_s by 2, for the example. So, 100 times V_i becomes 50 V_s . This 50 V_s is again divided equally between 20 K, 20 K; appears as 25 V_s . So, K_{naught} is equal to 25.

(Refer Slide Time: 11:23)



So, just by observation, we are now able to write down the value of K naught, for this example. Next, what is τ_i ? I have told you, τ_i is equal to C_i , this capacitor, into effective resistance across it, which is 10 K ; you short this; and 10 K , which is, 10 K parallel 10 K is 5 K . So, you have C_i into 5 K , which is 50 picofarads into 5 K ; which is nothing but 250 , 250 into 10 to power minus 9 . Or, 250 nanoseconds . That is the time constant of the input.

(Refer Slide Time: 12:22)



So, τ_i is known. τ_0 similarly is nothing but C_0 , which in this case is, 10 picofarads. And again, short the sources. So, 20 K parallel 20 K is the effective resistance across the capacitance, which is 10 K. 20 K parallel 10, 20 K is 10 K; so, which is, 10 picofarads. I would take again; this is equal to 100 nanoseconds, **100 nanoseconds**.

(Refer Slide Time: 13:28)

The chalkboard shows the following calculations:

$$K_0 = 25$$

$$\tau_0 = C_0 \times 10 \times 10^3$$

$$= 10 \times 10^{-12} \times 10 \times 10^3$$

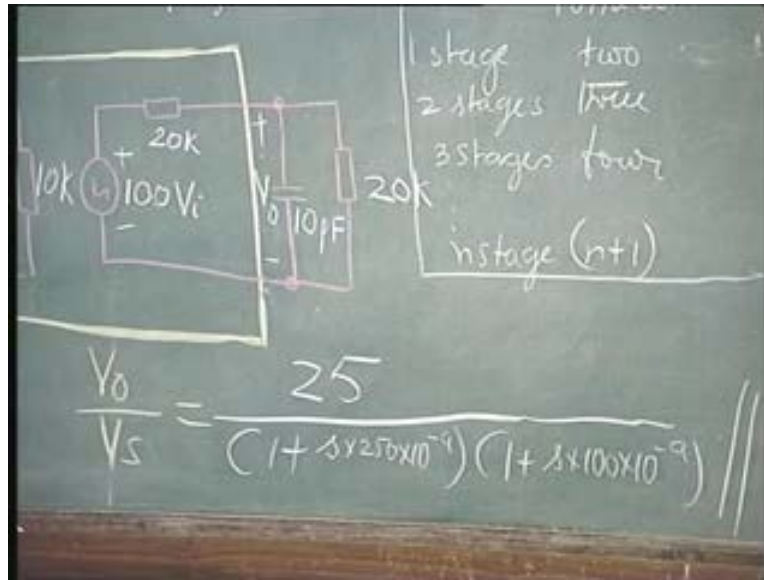
$$= 100 \times 10^{-9} \text{ sec}$$

$$\tau_i = C_i$$

$$= 250$$

So, we have solved the problem. So, I can write down the transfer function V_0 over V_s as, **V_0 over V_s as**, 25 divided by 1 plus s into 250 nanoseconds, 1 plus s into 100 nanoseconds. That is the answer.

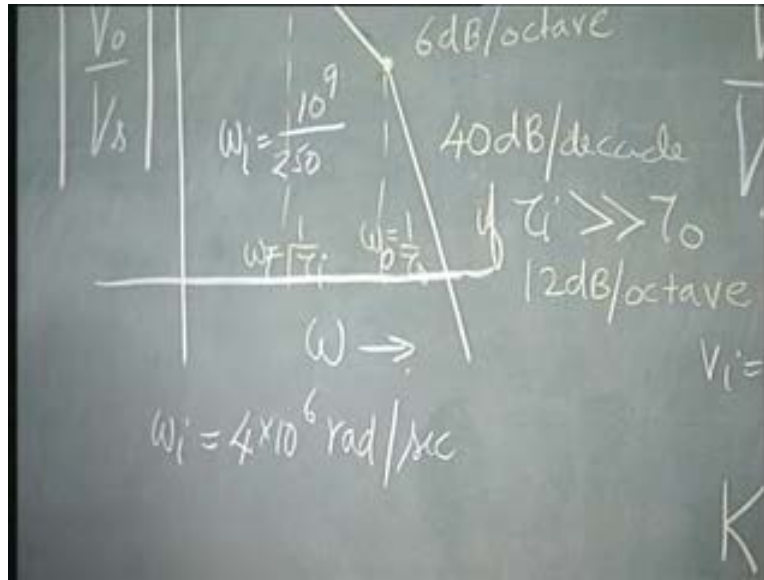
(Refer Slide Time: 14:08)



Now, I would like to expand here. Suppose we plot the Bode's plot. Then, this corresponds to gain of 25, remaining constant. If you convert it into decibels, it will be 20 log to the base 10 of 25. That is the decibels. 20 log to the base 10 of 20; whatever it is. That is the gain, constant gain, at low frequencies.

And then, at one corner frequency corresponds to 1 over 250 into 10 to power minus 9 or omega 1, we will call it omega i; corresponds to... this is omega i, this is omega naught. So, 1 over 250 nanoseconds. Or, this is equal to, omega i equals, therefore, 1000 divided by 250, that is, 4 into 10 to power 6 radians per second; or, 4 mega radians per second. 1000 divided by 250 is 4, into 10 to power 6 radians per second. That is omega i.

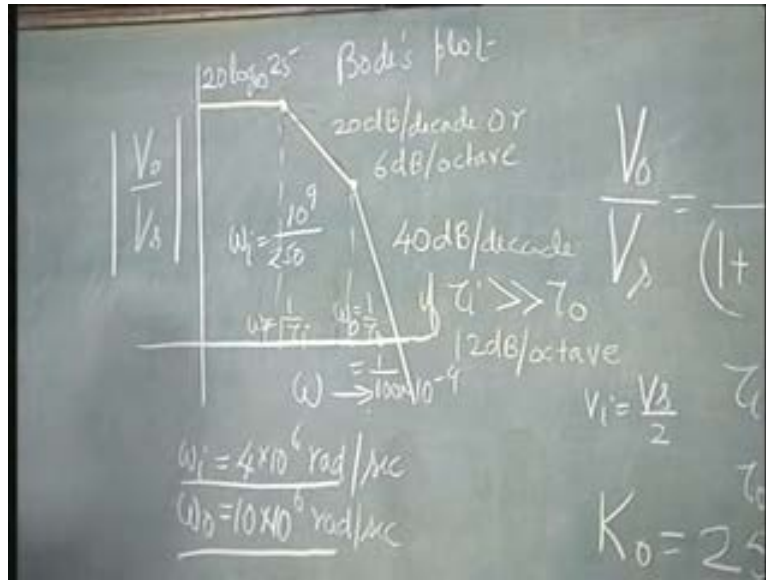
(Refer Slide Time: 15:39)



Similarly, omega naught is going to be, **is going to be**, 1 over 100 nanoseconds; or, 10 into 10 to the power 6 radians per second. So, we have got the corner frequencies also for this so called Bode's plot; and this is the complete frequency response of the circuit.

4 is comparable to 10. So, suppose I ask you to determine the upper cut-off frequency of this. Upper cut-off frequency or upper 3 dB frequency is going to be defined... I told you clearly. If this corner frequency is far away from this, then, this itself is the upper cut-off frequency, because this does not influence this. But now, in this case, 4 and 10 are pretty close to one another; so, upper cut-off frequency actually is going to be less than 4 mega radians per second, because at this particular point, apart from the influence of this, this also is going to influence in reducing the gain. So, you have to evaluate the upper cut-off frequency for this.

(Refer Slide Time: 17:05)



How do you evaluate this? This is very simple. Upper cut-off frequency, we have also said, is nothing but 3 dB point, upper 3 dB point, where the gain falls to 1 over root 2 times the maximum, the low frequency gain. So, if the gain of this is 25 by this, then, when the gain falls to 25 by root 2, that is the frequency corresponding to upper cut-off frequency.

So, we will see that, if ω_i and ω_o are comparable, then, $1 + 25$ by $1 + \dots$, let us say, $j\omega_s$, $j\omega$ by ω_i , $1 + j\omega$ by ω_o is the actual gain. The magnitude of this is going to be 25 by $1 + \omega$ by ω_i^2 under the root; again, under the root, $1 + \omega$ by ω_o^2 . So, when this becomes equal to 25 by root 2, that frequency corresponds to upper cut-off frequency. So, 25 gets cancelled; that means, then, this whole factor becomes equal to root 2.

(Refer Slide Time: 18:43)

Handwritten notes on a chalkboard:

$$\left| \frac{25}{(1 + j\frac{\omega}{\omega_i})(1 + j\frac{\omega}{\omega_o})} \right|$$

$$\frac{25}{\sqrt{1 + (\frac{\omega}{\omega_i})^2} \sqrt{1 + (\frac{\omega}{\omega_o})^2}} = \frac{25}{\sqrt{2}}$$

Parameters listed:

$$\omega_i = 4 \times 10^6 \text{ rad/s}$$

$$\omega_o = 10 \times 10^6 \text{ rad/s}$$

So, we can square this. So, 2 becomes equal to 1 plus omega by omega i whole square into 1 plus omega by omega naught... So, this is going to be a quadratic equation, which if you solve, will give you the upper cut-off frequency. So, I would like you to work this out; solve this quadratic equation. This is a quadratic equation in omega by omega naught, omega square; to get omega to the power 4 and omega square. We can solve for omega square and get the upper cut-off frequency here.

(Refer Slide Time: 20:12)

Handwritten notes on a chalkboard titled "Problem 1":

$$2 = \left[1 + \left(\frac{\omega}{\omega_i} \right)^2 \right] \left[1 + \left(\frac{\omega}{\omega_o} \right)^2 \right] \frac{V_o}{V_s}$$

Additional notes:

- $20 \log$
- $\omega_i =$
- ω

So please, as a homework problem complete this. That is not part of the example problem. Obtain the upper cut-off frequency for the example. Obtain the upper cut-off frequency for the amplifier. So, you will notice that the upper cut-off frequency is going to be less than the lowest of the corner frequencies.

So, let us consider the Example 6. An amplifier has V_o over V_s given as 100 by $1 + s/\pi \times 10,000$; that whole thing multiplied by $1 + s/\pi \times 10$ to the power 6. So, this is the characteristics of the amplifier. You are asked to find out its bandwidth.

(Refer Slide Time: 20:48)

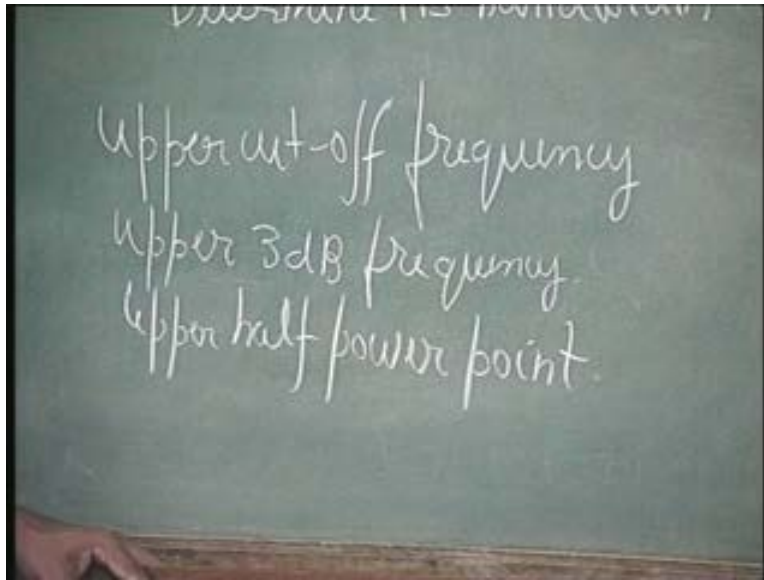
EXAMPLE 6

An amplifier has $\frac{V_o}{V_s} = \frac{100}{\left(1 + \frac{s}{\pi(10000)}\right) \left(1 + \frac{s}{\pi(1000000)}\right)}$

Determine its bandwidth.

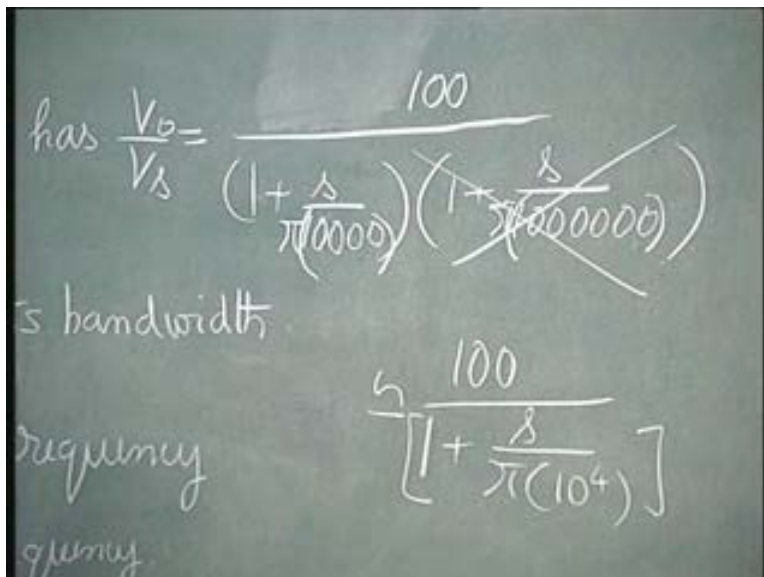
Now, I have told you earlier that upper cut-off frequency is the same as upper 3 dB frequency; also same as half power point, upper half power point. Also known as upper half power point, upper 3 dB frequency, upper cut-off frequency; all are one and the same.

(Refer Slide Time: 21:42)



Now, in a situation where this particular frequency is dominant compared to this; this, its influence is far away. This is the first frequency which comes into picture. So, this dominates the attenuation characteristic of the amplifier; and this becomes of low significance. Therefore, even though this is a second order system, this can be equated for practical purposes; within the range of interest, it is only 100 divided by 1 plus s by pi into 10 to the power 4. So, this is half, we can approximate.

(Refer Slide Time: 22:29)



This is 10 to power 4, this is 10 to power 6; there is a 100 magnitude difference. So, we can ignore the effect of this, within the useful range of the amplifier. So, even though this is a second order system, in effect, we can, as an amplifier, we can consider it, approximate it, as a first order. That means, when the next corner frequency is an order of magnitude different, that is, 10 times higher, then, you can approximate the system as one order less, first order. So, please remember that.

So, if the frequencies, corner frequencies, are far apart from one another such that they are 10 times... then, it can be considered that the other one, far away one, can be ignored within the... So, 100 divided by this. And then, the bandwidth becomes... because s equal to j omega, I substitute; and this whole quantity should become equal to 1. That means that is the bandwidth.

(Refer Slide Time: 23:54)

Handwritten notes on a chalkboard:

$$as \frac{V_o}{V_s} = \frac{100}{\left(1 + \frac{s}{\pi(10000)}\right) \left(1 + \frac{s}{\pi(1000000)}\right)}$$

2nd order

↓ approx

1st order

$$\frac{100}{\left[1 + \frac{s}{\pi(10^4)}\right]}$$

bandwidth frequency unity point

bandwidth

So, bandwidth becomes equal to this itself. So, if you want to convert this into frequency, radians per second, to hertz, then, you have to divide it by... So, in terms of hertz... So, this is going to be pi into 10 to power 4 divided by 2 pi or this is equal to... pi, pi, gets cancelled, 5 into 10 to power 3.

(Refer Slide Time: 24:33)

idth

approx

$$\frac{100}{\left[1 + \frac{s}{\pi(10^4)}\right]}$$

1st order

$$\text{bandwidth} = \pi \times 10^4 \text{ rad/sec}$$
$$\text{Hz} = \frac{\pi \times 10^4}{2\pi} = 5 \times 10^3$$

Or, answer is, bandwidth is equal to 5 Kilohertz.

(Refer Slide Time: 25:23)

EXAMPLE 6

An amplifier has $\frac{V_o}{V_s} = \frac{100}{\left(1 + \frac{s}{\pi(10^4)}\right) \left(1 + \frac{s}{\pi(10^6)}\right)}$

Determine its bandwidth

Upper cut-off frequency

Upper 3dB frequency

Upper half power point

5 kHz

$$\frac{100}{\left[1 + \frac{s}{\pi(10^4)}\right]}$$
$$\text{bandwidth} = \pi \times 10^4 \text{ rad/sec}$$
$$\text{Hz} = \frac{\pi \times 10^4}{2\pi} =$$

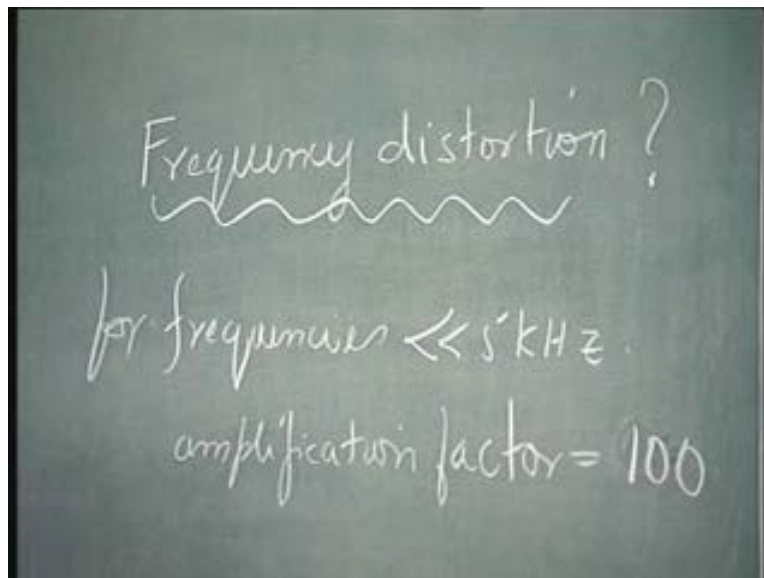
So, bandwidth; this is an important parameter associated with an amplifier, is essentially the first corner frequency, if other corner frequencies are far away from the first corner frequency. Otherwise, as will be given out in your example problem corresponding to Example 5, it will be dependent upon the other corner frequency as well.

In normal cases, the first corner frequency is the dominant time constant which is going to therefore fix up the bandwidth primarily this way. So, 5 Kilohertz in this case is the bandwidth of the amplifier. That means, the useful range, wherein the signal is not going to be much getting affected due to frequency; that range corresponds to 5 Kilohertz.

So, this is an important parameter associated with amplifiers. What does it mean? At 5 Kilohertz, already attenuation is going to be by 3 dB. At 5 Kilohertz, if you see, this becomes $\frac{1}{\sqrt{2}}$ plus j ; so attenuation becomes 3 decibels. It goes to 1 over root 2 - half power. So, beyond that, it is of no interest to us.

So, that means, all frequencies beyond this will be subjected to more attenuation and therefore will get distorted. This is called frequency distortion. What is it? That means, for frequencies much less than 5 Kilohertz, for the example, all frequency components in the example, the amplification factor is equal to 5, 100 in this case; remains constant, 100. Whereas, frequencies around 5 Kilohertz and much beyond 5 Kilohertz is going to be different for different frequencies.

(Refer Slide Time: 27:12)



So, the input signal, if it is comprising of any frequencies with certain amplitude, the same amplitude ratio is not going to be maintained at the output. That is what is called distortion. Let us say, we have, say 100 Hertz signal and 100 Kilohertz signal at the input. 100 Hertz signal is definitely going to be amplified by 100. But, 100 Kilohertz signal is going to be attenuated and its amplification factor is going to be much less. So, the ratio of the amplitudes of 100 Hertz and 100 Kilohertz will not be maintained at the output; which means, what is going to be available at the input will be distorted at the output. Its shape is going to change.

Not only that, this is amplitude distortion. Further, these different frequency components will be subjected to phase shift also. As I told you, at 5 Kilohertz, the phase shift suffered is going to be 45 degrees; $1 + j$ corresponds to 45 degrees. Already, there is a phase shift of 45 degrees. So, different frequency components will be suffering different phase shifts. So, this phase shift also will cause the signal to be distorted.

So, both amplitude distortion and phase distortion will occur because of the frequency dependence of gain. So, it is necessary that we must make sure that when we amplify signals, in this particular case, for this example, the signal frequency component should not be beyond 5 Kilohertz. Its useful range is only about 5 Kilohertz. So otherwise, if you have signals to be amplified which contain frequency components which are higher than this, we should have a upper cut-off frequency of bandwidth of the amplifier, which is much beyond whatever signal frequency, maximum frequency signal has.

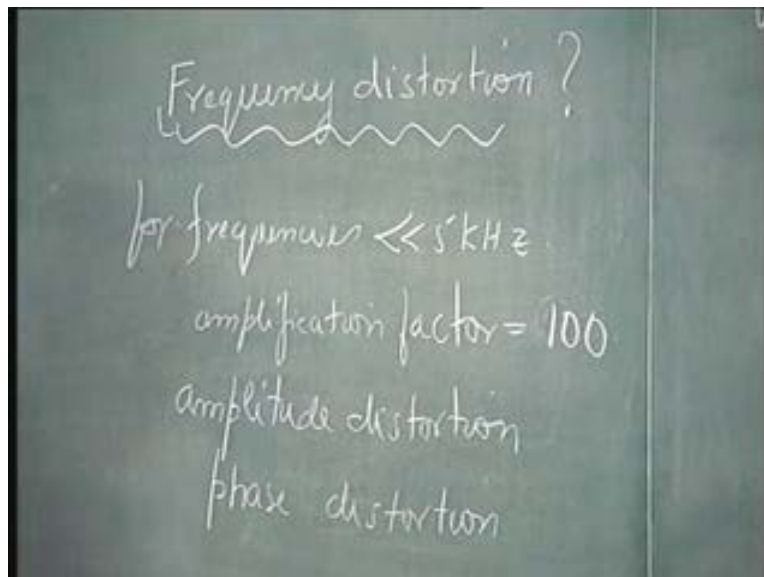
For example, video amplifier; if it is that that we are designing, then the frequency components will be up to about megahertz. That means, upper cut-off frequency of that amplifier should be corresponding to tens of megahertz so that no distortion occurs in the signal.

If it is an audio amplifier, may be, the signal frequency components of interest will be only about 20 Kilohertz, the best audio amplifier, let us say. And therefore, the upper cut-off frequency need to be only about 20 Kilohertz. So, this is the essence of frequency

distortion. Because of frequency dependence of amplifier gain, we have distortion, if we use amplifier for amplifying signals beyond its capability. So, we should always restrict amplifiers' use within its bandwidth.

Now, this frequency distortion will be causing amplitude distortion. What is amplitude distortion? Different frequency components will be subjected to different attenuations; that is why amplitude distortion is caused. Then, there is phase distortion. What is phase distortion? Different frequency components will be subjected to different phase shifts; that is going to cause phase distortion. So, both these cause frequency distortion.

(Refer Slide Time: 31:17)



Apart from this, we have now some other aspect that we have to touch upon as far as amplifier performance is concerned. This is different from what we have been discussing so far. What is this? Consider an amplifier. Amplifier is a block. So, output is going to be related to input. Let us consider V_{naught} , a voltage amplifier, we will consider. It could be current amplifier. I could as well consider I_{naught} or anything. It is a function of input voltage, let us say. I am considering, let us say, voltage amplifier.

(Refer Slide Time: 32:20)



Strictly speaking, in general, any device will give me an output which is a function of V_i ; not just necessarily proportional to V_i . So, if it is a general function of V_i , then, that function can be split up as something, let us call it as a voltage, which is going to be called offset. This is independent of the input voltage. This is a voltage which is independent of V_i . That voltage is called, as you have already seen, it is called offset voltage.

In an ideal amplifier, we do not want to have this kind of offset voltage. In an actual amplifier, this might also be called quiescent voltage. You have to get rid of it by decoupling it by means of a capacitor. So, this offset voltage is either called quiescent point voltage or offset voltage, depending upon your design of amplifier. This is independent of V_i . Then, something that is going to be K multiplied into V_i . This is what we have been calling as voltage gain. This K is the factor that we have been calling as voltage gain.

(Refer Slide Time: 34:08)

The image shows a chalkboard with the following handwritten text and equations:

$$V_o = f(V_i)$$
$$= V_{\text{offset}} + K_0 V_i$$

Annotations on the board include:

- A bracket above $V_o = f(V_i)$ labeled "Voltage amplifiers".
- An arrow pointing from V_{offset} to the text "independent of V_i ".
- An arrow pointing from K_0 to the text "Voltage gain".
- The word "offset" written below the first arrow.
- The word "for" written to the right of the equation.

Linear dependence upon V_i . Then, something that is going to be K_1 times V_i square; then, K_2 times V_i cube, so on... These terms are called nonlinearities.

(Refer Slide Time: 34:43)

The image shows a chalkboard with the following handwritten text and equations:

$$V_o = f(V_i)$$
$$= V_{\text{offset}} + K_0 V_i + K_1 V_i^2 + K_2 V_i^3 \dots$$

Annotations on the board include:

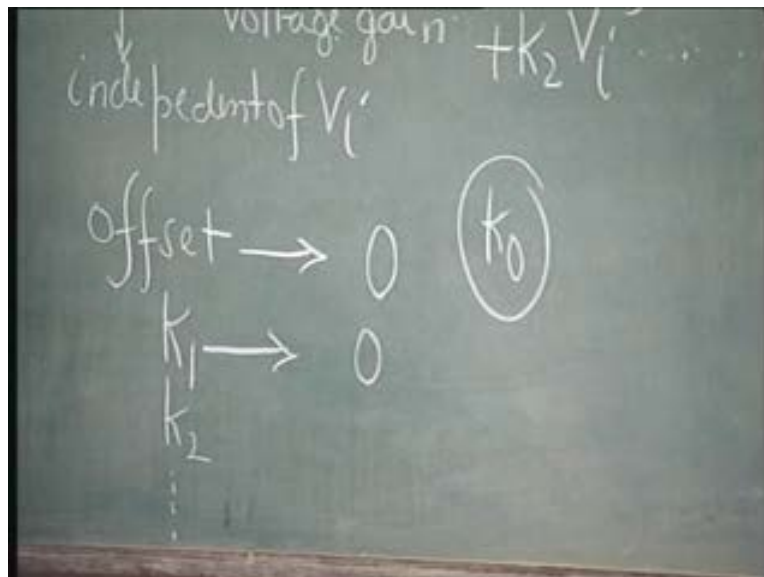
- A bracket above $V_o = f(V_i)$ labeled "Voltage amplifiers".
- A bracket above the terms $K_1 V_i^2 + K_2 V_i^3 \dots$ labeled "nonlinearities".
- An arrow pointing from V_{offset} to the text "independent of V_i ".
- An arrow pointing from K_0 to the text "Voltage gain".
- The word "offset" written below the first arrow.
- The word "for" written to the right of the equation.
- The word "freq" written to the right of the equation.
- The word "amp" written to the right of the equation.

These are the nonlinearities. It is supposed to be only dependent upon V_i ; but the block that you have got, the active device you have got, is something that simply gives you a function of V_i . So, in general, any amplifier that is designed by anybody will only give

you output voltage or output current as a function of input voltage or input current. That can only have an offset voltage which is independent of V_i ; then something that is linearly dependent upon V_i ; that we call as voltage gain, plus, terms which are non-linear terms; it will be V_i square, V_i cube, V_i ...

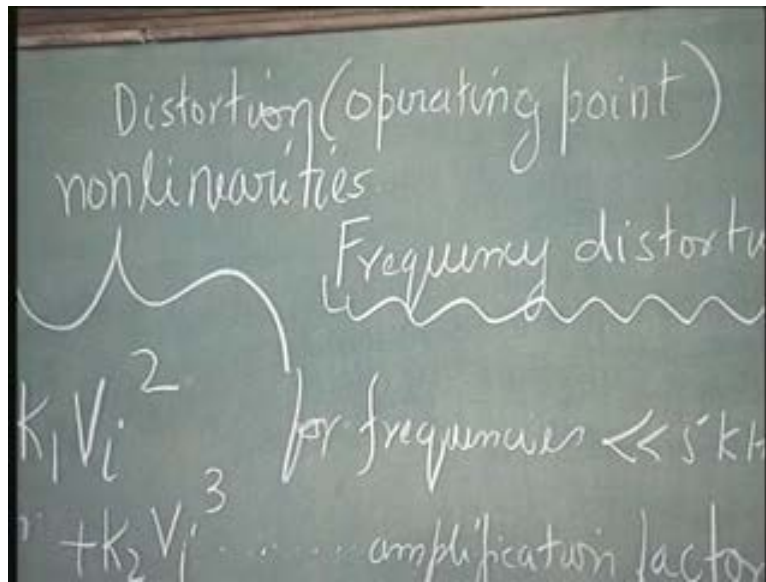
Now, in a good amplifier, what should happen? The offset should be as small as possible. It should go towards zero and then K_1 should be zero. K_1 , K_2 , etcetera, all these things should be going towards zero; and K_0 should be as constant as possible, as stable as possible.

(Refer Slide Time: 36:10)



So, K_0 is something that should be as stable as possible. Offset should go towards zero; K_1 should go towards zero; K_2 should go towards zero; all the nonlinearities should go towards zero. So, amplifier nonlinearities cause, again, distortion. This has nothing to do with frequency. This has only to do with amplitude of the input signal. So, this distortion, this depends upon where exactly we are operating in the amplifier, so called amplifier.

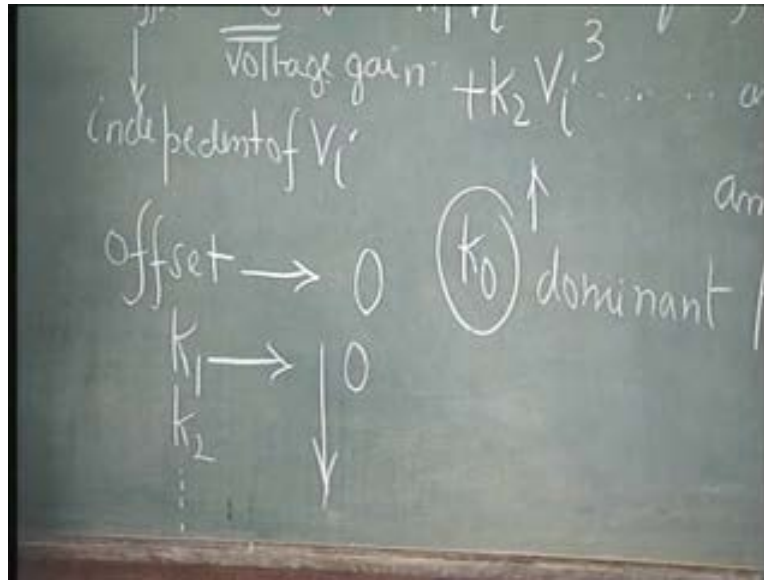
(Refer Slide Time: 37:14)



We can therefore select the operating point of the amplifier. We will select the operating point of the amplifier in such a manner that, the offset is zero; K_1 , K_2 , K_n are as small as possible. Or, we will select the device for designing the amplifier in such a manner that this is valid.

That means, after selecting the device, then, we will select the operating point for the device. That means, biasing of the amplifier is done in order to make the device work in a region where the linearity is dominant, K_0 is dominant. This should be maximized. K_0 should be maximized and K_1 , K_2 and K_n should be minimized. This, it indicates this should be minimized; this should be maximized.

(Refer Slide Time: 38:12)



So, we will bias the active device; or, we will select the operating point of the device; or, we will design the circuit, the complex circuit, containing large number of devices, active devices, in such a manner that this whole thing is true. So, design of an amplifier involves selection of the operating point and the bias in such a way as to make the nonlinearities the minimum, linearity the maximum and offset voltage the minimum.

If you have the nonlinearities coming into picture, that will cause distortion. So, if V_i is a sinusoid for example, V_i^2 will become sine square. So, it will have harmonic components. At the input there was no harmonic; it is now generating a harmonic at the output. V_i^3 will generate a third harmonic. V_i^4 will generate the fourth harmonic, like that...

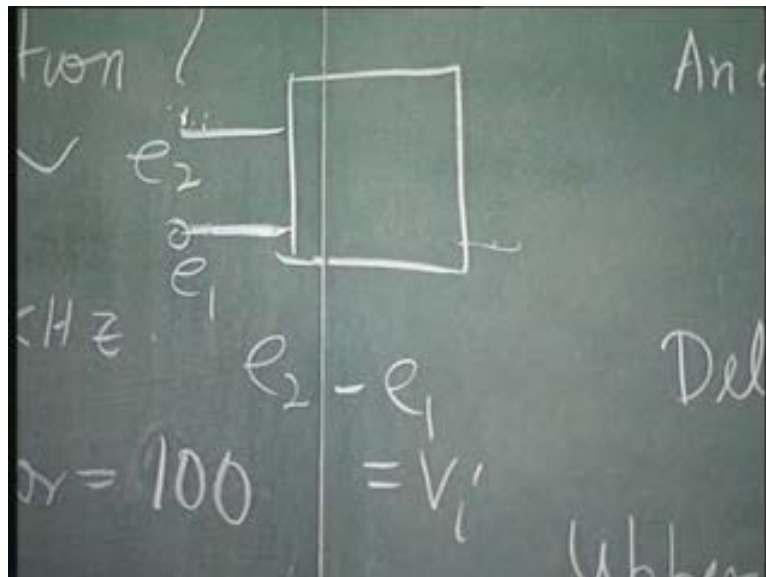
So, that means all these nonlinearities will create unwanted components at the output. So, that causes distortion. If it is a sine wave at the input, output will now no longer be a sine wave. It will have all the harmonic components also present. That is what is going to be causing this distortion.

So, this part of the design is going to take up lot of time for us; after identifying the device, how to bias the device; how to range these different circuits in such a manner as to make the offset zero; and make the nonlinearity minimum and maximize the linearity. That will be the purpose of most of the design lectures of the future.

So, this is the case for an amplifier with input port and output port. The input port may be the two terminals of a differential stage. That means, you can also call the input port of the amplifier, instead of always referring the voltage with respect to this, you can call this as e_1 and this as e_2 ; and e_2 minus e_1 as being equal to V_i .

So, that means now, it becomes a differential input operation. That means voltage reference can be taken with any point, arbitrary point; and these two voltages can be taken as absolute values from that arbitrary point. Earlier, we had taken the voltage reference as from here, and for this, from here. So, if you take these voltage references as from an arbitrary point, then, this becomes a differential input.

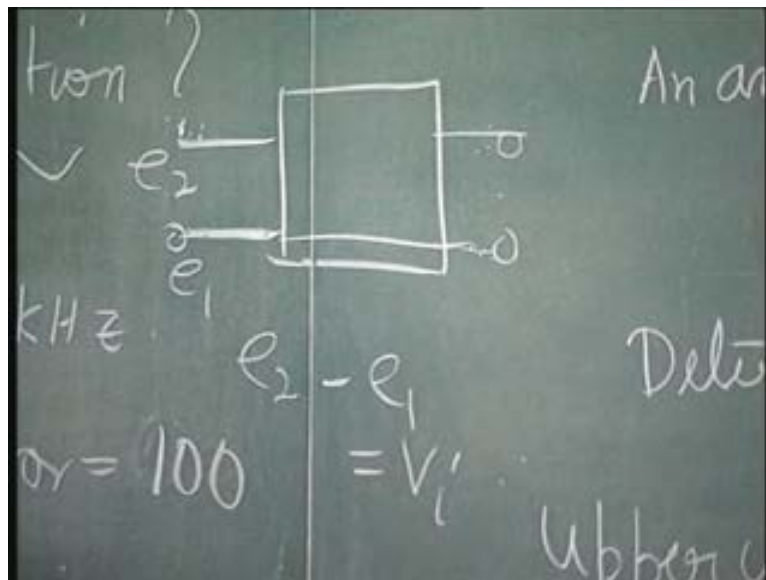
(Refer Slide Time: 41:31)



Similarly, if you take this from an arbitrary point, the same arbitrary point, this will become differential output. So, this becomes a differential input, differential output, amplifier, if the voltage reference, this is only a concept, is shifted somewhere else.

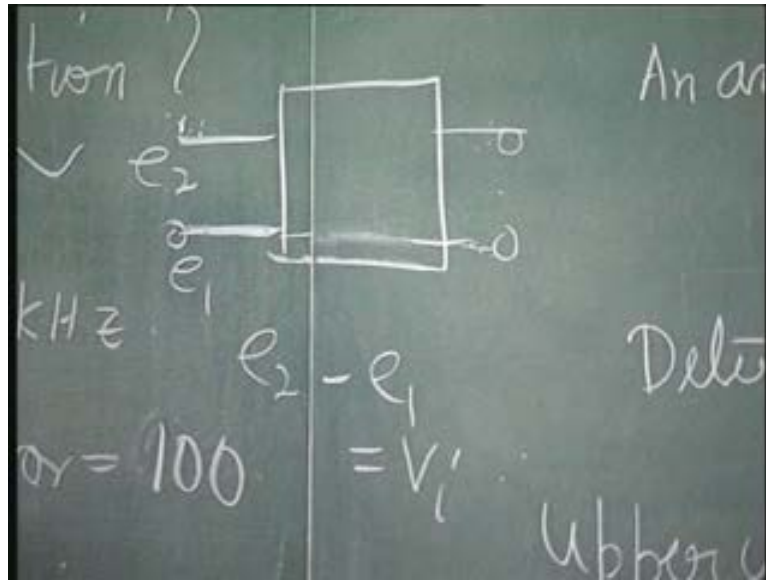
So, in a two port amplifier, this thing, you can treat it as differential input and differential output amplifier. So, what all we have said is valid whether it is differential input and differential output amplifier or just one port, with this as common terminal. That means, actually this becomes 4 terminal, becomes 3 terminal now because, we are connecting these two together and using this as a reference.

(Refer Slide Time: 42:14)



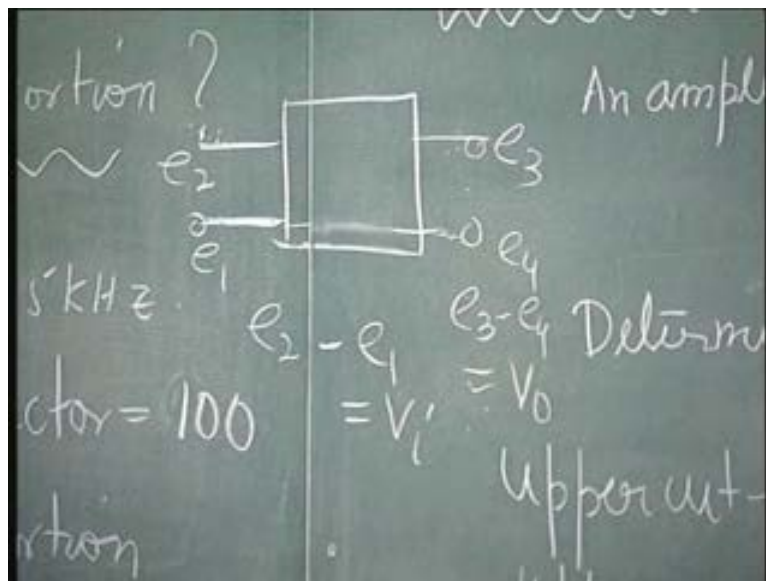
So, this becomes a 3 terminal amplifier. If this is not there, then it is a 4 terminal in 2 port amplifier.

(Refer Slide Time: 42:26)



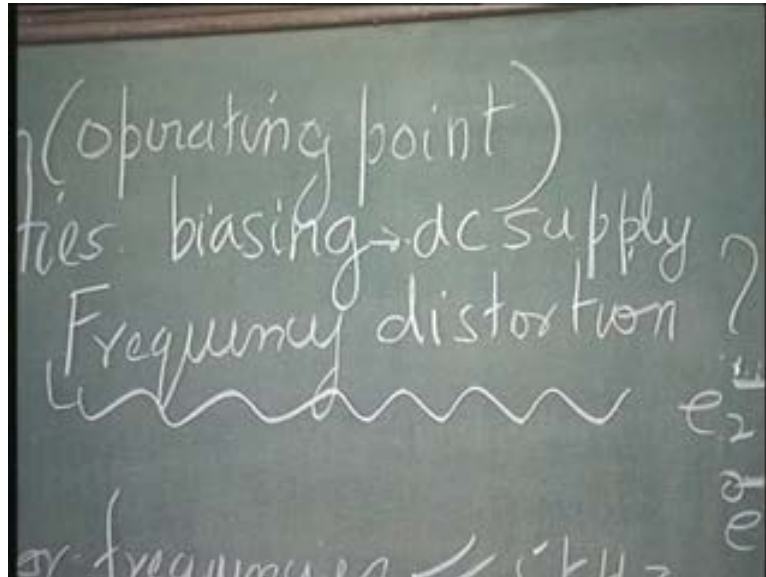
So, these discussions that we have had is going to be perfectly general and it is valid for three terminal as well as four terminal amplifiers. These are only conceptual references. Now, if you take arbitrary reference here, this will become differential input and differential output amplifier. So, even e_2 , let us say, e_3 , e_4 ; so, e_3 minus e_4 is what we have been calling as V naught.

(Refer Slide Time: 43:02)



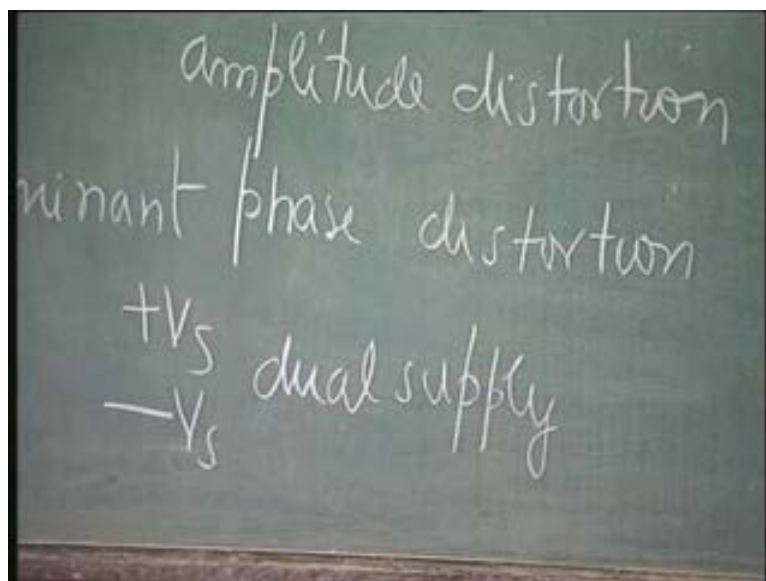
So finally, I would like to indicate that the amplifier works with power delivered from a separate source which is always called the dc power source. So, for biasing, we require a dc supply. So, this dc supply delivers the power required for biasing the amplifier.

(Refer Slide Time: 43:46)



So, this dc supply, let us say, is plus V s and minus V s; then it is called dual supply.

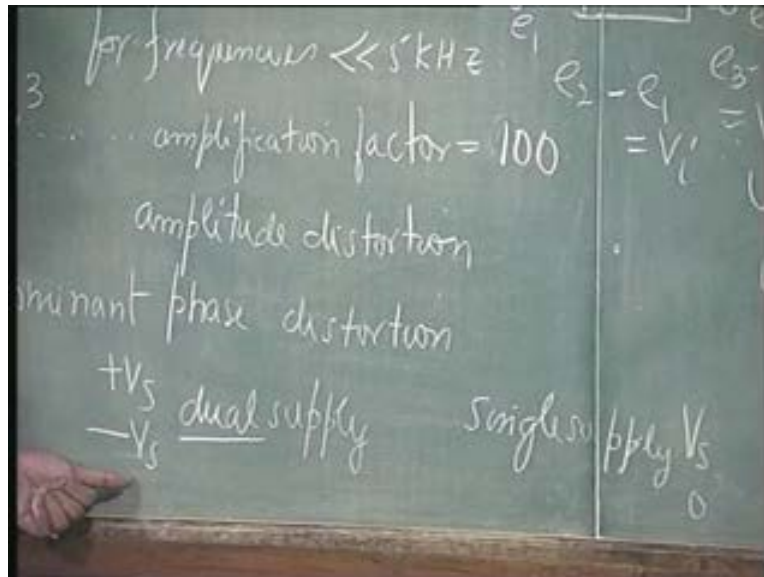
(Refer Slide Time: 44:00)



Why do you go for dual supply, plus V_s and minus V_s ? Suppose this signal could be positive or negative, V_i could be positive or negative. Then, in order to obtain this, we have to have both plus and minus supplies. The operating point should be such that output should be zero when the input is zero; so, which means, necessarily, in order that the offset of that is zero, you must operate the output at a voltage which is equal to zero. With plus V_s and minus V_s , the quiescent operating point for this should be zero. So, that is what requires a dual supply.

We can have single supply; then it will be V_s and ground, zero; or, minus V_s and zero. Then obviously, the operating point, in order to have maximum range for the output signal, output signal can be, minimum equal to zero, maximum equal to V_s . Here also, output signal could be maximum equal to plus V_s , minimum equal to minus V_s .

(Refer Slide Time: 45:20)



This is what is called the range for the output signal. Beyond this point, the output is said to go to saturation. This is another limitation. So, apart from these limitations, we also have what is called saturation.

Let me again explain this in terms of figures. This is V_{naught} , this is V_i . This is the output input characteristic of this amplifier, let us say. It should be, ideally speaking, linear. This is linearity. V_{naught} and V_i should be linearly related. That means, V_{naught} is equal to K_{naught} times V_i . This is...this line passing through the origin. If it does not pass through the origin, it will be this; or, it could be the other one.

So, if it does not pass through the origin, this voltage is called the offset voltage; this or this. When V_i is equal to zero, there is an output voltage. This is called a quiescent point. So, if it does not pass through the origin, then we are said to have an offset voltage. Now, that is clear, what is offset voltage.

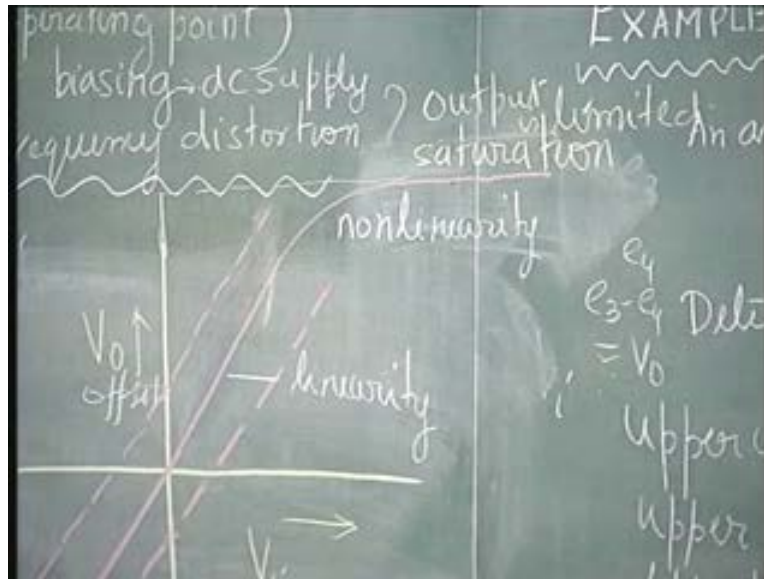
There could be nonlinearity; that means, it is not going on being linear, it is going to a nonlinear region. The ΔV_{naught} by ΔV_i , the slope here, is the same as the slope here; it is same as the slope here. But here, the slope is less. So, this is called the nonlinearity. This is the linearity. This is the offset. Then ultimately, it will go to what is called saturation. Let us say, this is the maximum voltage your output of the amplifier can give; this is the minimum voltage the output of the amplifier can give; this is called saturation.

(Refer Slide Time: 48:40)



Beyond this, output is not going to change. Beyond that, output is not going to change further. Even if the input is changed by any amount, output remains constant. Output is limited. So, output gets limited.

(Refer Slide Time: 49:08)



So, if power supplies are used for biasing, normally, these are the limits: plus V_s and minus V_s . It is made symmetric so that the quiescent point could be zero.

So, we have learnt a lot about distortion. That means, distortion occurs because of V_i increasing; and then, further increase in the output voltage is not the same as the earlier increase for the same amount of V_i change. So, that is called nonlinearity. Then, there is a region beyond which, further increase in V_i does not cause any change in V_{output} ; that is called saturation.

That can occur both on the higher side as well as the lower side. So, saturation nonlinearity, the nonlinearity because of the device, this non linearity; these are this kind of nonlinearities. In fact, the nonlinearity that I have put down here; it is symmetric here. That simply means that K_1 is zero. You can test it out.

(Refer Slide Time: 50:13)

$$V_o = f(V_i)$$
$$= V_{\text{offset}} + K_0 V_i + K_1 V_i^2 + K_2 V_i^3$$

Annotations:
- V_{offset} is independent of V_i .
- K_0 is the voltage gain.
- $K_1 \rightarrow 10$
- K_0 is circled with an arrow pointing up.
- A bracket groups the terms from $K_1 V_i^2$ onwards, with "Fre" written above it.

K_1 is zero; K_2 is present. This is going to have this kind of nonlinearity which is symmetric both for positive going and negative going signal, has K_1 , K_3 , etcetera, going to zero. But, K_2 , K_4 , etcetera, existing. So, this is one type of nonlinearity; so that depending upon the device that you select, the nonlinearities will change.

So, in the next class, we will learn more about these aspects: distortion, what does distortion cause, how distortion can be measured quantitatively, etcetera. This distortion that we have talked about for the second time is different from the frequency distortion, which comes about because of frequency dependence of the gain.