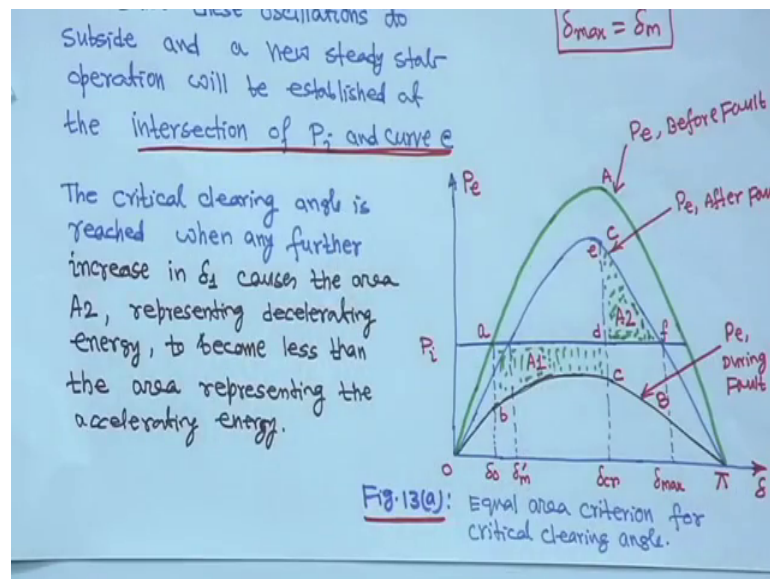


Power System Analysis
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Lecture - 60
Power System Stability (Contd.)

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So, now, we have to make A_1 is equal to A_2 , right, area A_1 is equal to area this see A_2 . So, and you have to find out δ_c . So, what you will do look before proceeding further A_1 is equal to that original graph P_i is equal to $P_{max} \sin \delta$ that means.

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This occurs when δ_{max} , or point f , is at the intersection of line P_i and curve c as shown in Fig. 13(a).

Applying equal-area criterion to Fig. 13(a), we get.

$$\int_{\delta_0}^{\delta_{cr}} (P_i - B) d\delta = \int_{\delta_{cr}}^{\delta_{max}} (C - P_i) d\delta$$

$$\therefore \int_{\delta_0}^{\delta_{cr}} (P_i - K_1 \cdot P_{max} \sin \delta) d\delta = \int_{\delta_{cr}}^{\delta_{max}} (K_2 \cdot P_{max} \sin \delta - P_i) d\delta$$

$$\delta_{cr} = \frac{1}{(K_2 - K_1)} \left[(\delta_{max} - \delta_0) \sin \delta_0 + K_2 \cos \delta_{max} - K_1 \cos \delta_0 \right] \dots (35)$$

$A = P_e = P_{max} \sin \delta$
 $B = K_1 \cdot A = K_1 P_{max} \sin \delta$
 $C = K_2 \cdot A = K_2 P_{max} \sin \delta$
 $K_1 < K_2$
 $P_i = P_{max} \sin \delta_0$
 $\delta_{max} = \delta_m$

This graph the green color one, this graph now you let the graph b that is b that is a black one, this black 1 b 1 b is equal to say some constant K_1 into A; that means, because this your this an A is equal to P e we are writing here because graph a is equal to P e. So, it will actually K_1 into $P_{max} \sin \delta$ later will see that K_1 K_2 all can be obtained and this graph C; that means, your this one this is graph C, there should listen one thing, there should not be any confusion this is graph C and this is at point c. So, there should not be any confusion, right and this one graph C is equal to K_2 into A is equal to K_2 into $P_{max} \sin \delta$. So, say and K_2 is greater than K_1 because this graph C, if you see this power is always greater than your what you call this during I mean post fault or after fault this power curve always above this graphs.

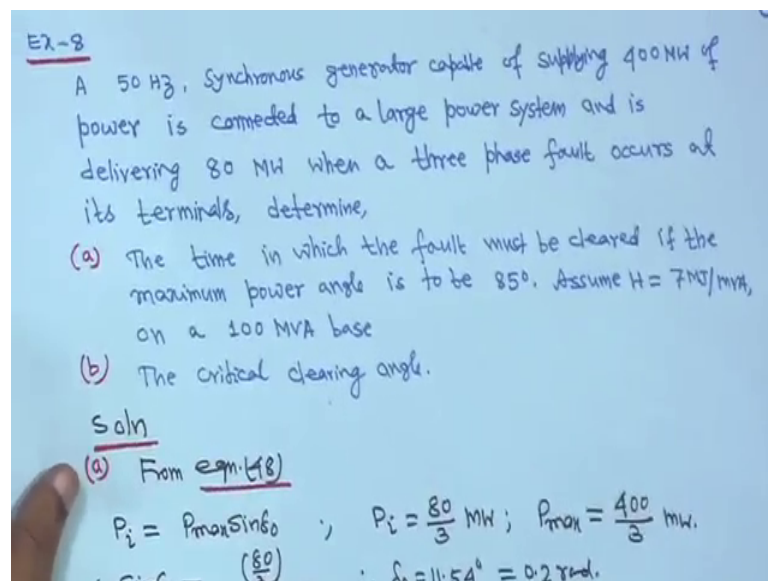
So, K_2 is greater than K_1 or otherwise K_1 less than K_2 and at δ is equal to δ_0 P_i is equal to that is P_i P_i is equal to $P_{max} \sin \delta_0$. So, at δ is equal to at this is the point green color that a point P_i is equal to $P_{max} \sin \delta_0$. Now that area A 1 is equal to A 2 means that is you take δ_0 to δ_{cr} because this is area one you have to intricate. So, intricate δ_0 to δ_{cr} , then this is your P_i graph. So, this is P_i minus the curve b; that means, this curve this curve.

Curve b P_i minus B and B is equal to K_1 into a that is $K_1 P_{max} \sin \delta$ will come to that is equal to this area a 2 that is limit integration δ_{cr} to δ_{max} integration δ_{cr} to δ_{max} , then C minus P_i this is the curve c and minus this line P_i this P_i line.

So, $P_i = P_{max} \sin \delta$; that means, $\delta = \sin^{-1} \left(\frac{P_i}{P_{max}} \right)$. This is δ actually. This is δ , right? It is equal to δ . The curve is equal to $K_2 P_{max} \sin \delta$ here it is. So, that is $\delta = \sin^{-1} \left(\frac{P_i}{P_{max}} \right)$. So, if you integrate and in this expression if you substitute P_i is equal to $P_{max} \sin \delta_0$ and I repeat δ_{max} is equal to δ_m . So, if you substitute here P_i is equal to $P_{max} \sin \delta$; that means, intricate and simplify you will get $\cos \delta_c$ is equal to $1 + \left[K_2 - K_1 \right] \left(\delta_{max} - \delta_0 \right) + K_2 \cos \delta_{max} - K_1 \cos \delta_0$. This is equation 55, this one you will get it right that this is the from which you can find out what will be the δ_c . So, this integration I am not showing this is easy. So, you can make it of your own simple thing. So, next I will take an example now.

So, I think whatever mathematical derivation was there everything is there for this course perhaps, it is over, right perhaps, it is over as far as theory is concerned and now will come to 2-3 numerical; good numericals.

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So, first one is look at that first one is that example 8 a 50 hertz synchronous generator capable of supplying 400 megawatt of power is connected to a large power system and is delivering 80 megawatt when a 3 phase fault occurs at its terminals. So, determine the time in which the fault must be cleared if the maximum power angle is to be 85 degree

assume H is equal to 7 mega joule per m V a on a 100 MVA base b the critical clearing angle.

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power is connected to a large power system and is delivering 80 MW when a three phase fault occurs at its terminals, determine,

(a) The time in which the fault must be cleared if the maximum power angle is to be 85° . Assume $H = 7 \text{ MJ/MVA}$, on a 100 MVA base

(b) The critical clearing angle.

Soln

(a) From eqn. (18)

$$P_i = P_{\max} \sin \delta_0 \quad ; \quad P_i = \frac{80}{3} \text{ MW} ; \quad P_{\max} = \frac{400}{3} \text{ MW.}$$

$$\therefore \sin \delta_0 = \frac{\left(\frac{80}{3}\right)}{\left(\frac{400}{3}\right)} \quad \therefore \delta_0 = \underline{11.54^\circ} = \underline{0.2 \text{ rad.}}$$

So, from equation 48 P_i is equal to $P_m \sin \delta_0$, you know this all equations are all equations already i have given, but let me search that where equation 48, otherwise you know this from the sin curve you know this it is equation 48 just hold on otherwise it not a problem you know everything. So, just hold on if i get it i will show you that P_m is equal to this thing this here it is you know this that P_i is equal to $P_{\max} \sin \delta_0$. This is equation 48. So, in that case it is 3 phase. So, P_i will be 80 by 3 megawatt and P_{\max} will be 400 by 3 megawatt and then $\sin \delta_0$, we can find out 80 by 3 divided by 400 by 3. So, you will get δ_0 is equal to 11.54 degree or 0.2 radian now it is given that maximum power angle is to be 85 degree this is given.

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$$\delta_1 = \delta_m = 85^\circ = 1.48 \text{ radian.}$$

From eqn (49),

$$\cos \delta_c = \cos \delta_1 + (\delta_1 - \delta_0) \sin \delta_0 = \cos(1.48) + (1.48 - 0.2) \sin(0.2)$$
$$\therefore \cos \delta_c = 0.343$$
$$\therefore \delta_c = 1.22 \text{ radian}$$

From eqn (52),

$$t_c = \sqrt{\frac{2H(\delta_c - \delta_0)}{\pi f P_i}}$$
$$= \sqrt{\frac{2 \times 7 \times (1.48 - 0.2)}{\pi \times 50 \times 0.80}}$$

$$P_i = 80 \text{ MW (3\phi)}$$
$$\therefore P_i = \frac{80}{100} = 0.80 \text{ pu}$$
$$H = 7 \text{ MJ/MVA.}$$

So, if it is given so; that means, delta one is equal to delta m is 85 degree that is 1.48 radian therefore, from equation 49; that means, this equation; this is your equation 49 that cosine delta c is equal to cosine delta 1 plus delta 1 minus delta 0, but delta one is equal to delta m is equal to 85 degree is equal to is equal to 1.48 radian; that means, you can write cosine delta c is equal to same formula I am rewriting here. So, everything put in radian. So, it is cosine 1.48 in bracket it is delta 1 minus delta 0 this is also radian 1.48 minus 0.2 the sin 0.2 this is all radian; that means, delta c you will get 1.22 radian that is your delta C and from equation 52 that your critical your what you call that clearing time expression. So, this is your 51, thus let me see if I find it that your 53 here; this is equation 52 that t c expression is given this is equation 52 and from equation 52 t c is equal to same equation we are rewriting and you put all the values you put all the values H value delta c minus delta 0 up on pi f P i. So, H is given 7.

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From eqn (49),
 $\cos \delta_c = \cos \delta_1 + (\delta_1 - \delta_0) \sin \delta_0 = \cos(1.48) + (1.48 - 0.2) \sin(0.2)$
 $\therefore \cos \delta_c = 0.343$
 $\therefore \delta_c = 1.22 \text{ radian}$

From eqn (52),
 $t_c = \sqrt{\frac{2H(\delta_c - \delta_0)}{\pi f P_i}}$
 $t_c = \sqrt{\frac{2 \times 7 \times (1.48 - 0.2)}{\pi \times 50 \times 0.80}}$
 $\therefore t_c = 0.377 \text{ sec} = \underline{377 \text{ ms}}$

$P_i = 80 \text{ MW (3\phi)}$
 $\therefore P_c = \frac{80}{100} = 0.80 \text{ pu}$
 $H = 7 \text{ MJ/MVA}$

So, 2 into 7 delta c you have computed right you are here, I think while writing, I have made it type of graph I mean writing error, I think it will be your just hold on that where is that formula it will be delta c minus delta 0.

So, it will be your this delta C actually it is 1.22. So, I have made by mistake 1.48, I have taken this value by mistake delta 1 right, it will be actually 1.22 I think answer is correct. So, t c is equal to 0.377 second or 377; 77 millisecond, but I will request you, I do not have calculator here now, right, whether I computed it using 1.48 or 1.22, but correct is 1.22 I correct it, but if answer is little different, you please check with that calculator this is my request to you I do not have calculator here. So, this is your t c is equal to it may be 3 7 millisecond or if it is based on 1.48, then this answer will come, but this is not correct answer. So, basically it will be 1.22 I have now corrected. So, please make it otherwise this is the answer and right.

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$$\begin{aligned}\delta_{cr} &= \cos^{-1}[(\pi - 2\delta_0) \sin \delta_0 - \cos \delta_0] \\ \therefore \delta_{cr} &= \cos^{-1}[(\pi - 2 \times 0.2) \sin(0.2) - \cos(0.2)] \\ \therefore \delta_{cr} &= \cos^{-1}(-0.43) = \underline{115.46^\circ} = \underline{2.01 \text{ rad.}}\end{aligned}$$

Ex-9
A synchronous generator is connected to a large power system and supplying 0.45 pu MW of its maximum power capacity. A three phase fault occurs and the effective terminal voltage of the generator becomes 25% of its value before the fault. When the fault is cleared, generator is delivering 70% of the original maximum value. Determine the critical clearing angle.

So, and from equation 53; equation 53, this one then your you will get that equation 53 cosine delta c r was given is equal to pi minus 2 delta 0 sin delta 0 minus cos delta 0. So, delta c r actually cos inverse of the all this thing you substitute all this values here all this values here you will get critical clearing angle will be 115.46 degree or 2.01 radian.

So, next is your example 9, next one is suppose a synchronous generator is connected to a large power system and supplying 0.45 per unit megawatt power of its maximum power capacity a 3 phase fault occurs and the effective terminal voltage of the generator becomes 25 percent of its value before the fault, but when the fault is cleared generator is delivering seventy percent of the original maximum value determine the critical clearing angle you have to find out the critical clearing angle so whatever.

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Soln. (4)

We know,

$$K_1 = \frac{P_{\max} \text{ during the fault}}{P_{\max} \text{ before the fault}}$$
$$K_2 = \frac{P_{\max} \text{ after the fault}}{P_{\max} \text{ before the fault}}$$

From eqn(55)

$$\cos\delta_{cr} = \frac{1}{(K_2 - K_1)} \left[(\delta_{\max} - \delta_0) \sin\delta_0 + K_2 \cos\delta_{\max} - K_1 \cos\delta_0 \right]$$

Initially, the generator is supplying 0.45 pu MW of P_{\max} .
Therefore,

We have taken before actually K_1 and K_2 ; we have seen that K_1 actually P_{\max} during the fault and ratio of P_{\max} before the fault because we have taken your curve a, b and c curve b, we have taken it is K_1 into your $P_{\max} \sin \delta$. So, K_1 actually P_{\max} during the fault for the ratio whatever the during the fault what is the maximum value of the power P_{\max} divided by before the fault P_{\max} before the fault that is K_1 and K_2 is equal to P_{\max} after the fault and P_{\max} before the fault if I get it here; if I let me find it out if it is here I will; I can show you, but I have already told you all this things just hold on if I get it here then it is otherwise you know this here that a is equal to this is your before fault and this one that b is equal to it is your during fault and c is equal to this is after fault. So, therefore, K_1 ; K_1 will be whatever that this thing will come your P_{\max} during the fault and divide I mean denominator always is P_{\max} before the fault and K_1 is equal to P_{\max} during the fault and K_2 divided by P_{\max} before the fault this ratio.

And K_2 is the ratio of P_{\max} after the fault divided by P_{\max} before the fault from here only everything is given here only, therefore, from equation 55; this is the equation 55, we are rewriting, we are rewriting the whole equation here. So, initially the generator is supplying 0.45 per unit megawatt of P_{\max} . So, initially it was supplying; that means, ; that means, your this is actually P_i as initially it was supplying your 0.45 per unit megawatt of P_{\max} ; that means, this is actually your P_i actually 0.45 P_{\max} is equal to you can write $P_{\max} \sin \delta_0$.

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$$P_i = 0.45 P_{max} = P_{max} \sin \delta_0$$
$$\therefore \delta_0 = \underline{26.74^\circ} \text{ or } \underline{0.466 \text{ rad.}}$$

Now,
$$P_{max} = \frac{|E_g| |V_t|}{x_d}$$

When the fault occurs, $|V_t|$ becomes $0.25 |V_t|$

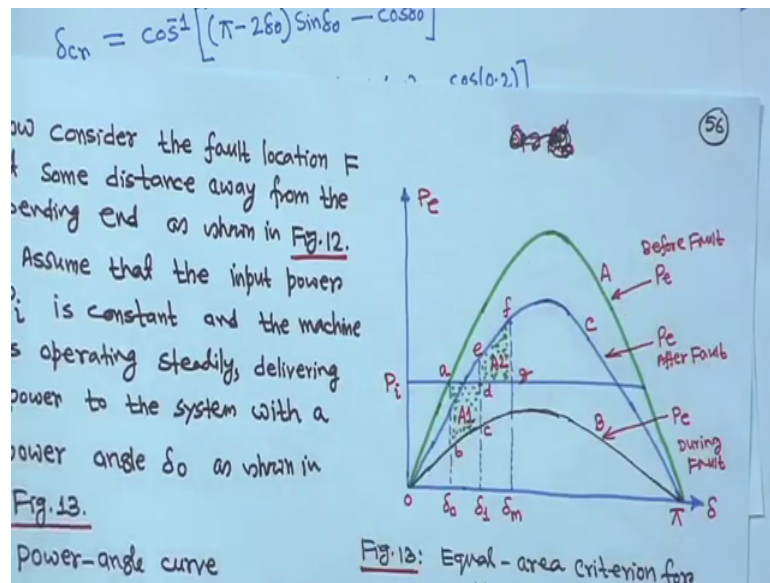
Hence,
$$K_1 = \underline{0.25}$$

After the fault is cleared, with $K_2 = \underline{0.70}$, we have
$$P_i = K_2 P_{max} \sin \delta'_m$$
$$\therefore \sin \delta'_{m0} = \frac{P_i}{K_2 P_{max}} = \frac{0.45 P_{max}}{0.7 P_{max}} = \frac{0.45}{0.70}$$
$$\therefore \delta'_m = \underline{40^\circ} \text{ or } \underline{0.698 \text{ radian.}}$$

So, this is your we can write at operating point your at a operating point anywhere you take that is your this thing for example, any operating point here this delta 0 right. So, your P i is equal to 0.45 your P max is equal to P max sin delta 0 P max P max will be cancel. So, delta 0 will become 26.74 degree; R 0.466 radian. Now P max is equal to P max is equal to magnitude e g into V t up on x d now when the fault occurs when the it gives; it is given in the problem when the fault occurs the V t becomes 0.25 V t right. So, in that case in that case your K 1 will be 0.25 because everything will remain same only this 0.25 will be there so; that means, power will from its original value it will come down to 25 percent actually.

That is why K 1 will be 0.25, now after the fault; is cleared K 2 will be 0.70 because that is also given in the problem that is also that is also given in the problem that it your that when the fault is cleared generator is delivering 70 percent of the original maximum value. So, determine the critical clearing angle I mean if you look at the graph initially it was P max, but during the fault it was actually 0.25 P max and when fault is cleared.

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It is actually $0.7 P_{max}$ right. So, this is the philosophy. So, from this graph you can make out this is P_{max} , this is $0.25 P_{max}$ and this is $0.7 P_{max}$; this blue one and black one is $0.25 P_{max}$ and this is $P_{max} \sin \delta$. So, if you take all this data that then K_1 is known K_2 also then known it is 0.7 . So, therefore, P_i is equal to $K_2 P_{max} \sin \delta_m$ dash just hold on I have to take that graph again. So, the here it is. So, this is actually this is this blue curve you take blue curve this blue one that it and this blue horizontal line that P_i line and this is δ_m dash this is δ_m dash therefore, after the fault is cleared.

So, this is the blue line it is operating in operation this is that this is the power that supplied by your what you call from the generator P_e P_{max} is equal $\sin \delta$ your into your whatever fraction is come 0.7 . So, this is that graph. So, and its and it whereas, blue line the intersection is δ_m dash. So, that is why after the fault is cleared K_2 is 0.7 and we have P_i is equal to $K_2 P_{max} \sin \delta_m$.

So, this is your graph C actually, this is your graph C. This is your graph C and here it is C is equal to $K_2 a$ $K_2 P_{max} \sin \delta$ K_2 is equal to 0.7 , then this one P_i is equal to $K_2 P_{max} \sin \delta_m$ dash so; that means, this point δ_m dash means this point this point. So, in that case you compute what is your δ_m dash. So, P_i it, we can write $\sin \delta_m$ dash is equal to P_i upon $K_2 P_{max}$. So, P_i is your $\sin \delta$ is equal to $0.45 P_{max}$ divided by $0.7 P_{max}$. So, that is actually coming 0.45 by 0.7 . So, in that case

you will get delta m dash is equal to your 40 degree because P i is equal to 0.45 P max, it was given that 45 percent of that. So, P i is equal to 0.45 P max. So, here we have put P i is equal to 0.45 P max divided by 0.7 P max is equal to 0.45 by 0.7, this actually comes to delta m dash is equal to 40 degree or 0.698 radian right so; that means, delta max; that means, your; this is your delta max. So, delta max is equal to pi minus delta m dash.

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$$\delta_{\max} = (\pi - \delta'_m) = 2.443 \text{ rad}$$

$$\therefore \cos \delta_{cr} = \frac{1}{(0.70 - 0.25)} \left[(2.443 - 0.466) \sin(0.466) + 0.7 \cos(2.443) - 0.25 \cos(0.466) \right] = 0.29$$

$$\therefore \delta_{cr} = \underline{73.14^\circ} \text{ or } \underline{1.276 \text{ radians}} \quad [\text{Eqn (55)}]$$

Ex-10
Find the critical clearing angle of the power system shown in Fig.15 for a three-phase fault at the point F. Generator is supplying 1.0 pu power under prefault condition.

The delta max is equal to; that means; from here that delta max is equal to pi minus delta m dash. So, delta m dash we have computed 0.698 radian this you have computed here we have computed.

So, if you put it here it will be 2.443 radian and in the all this data available now go back to equation 55. I have not read it and that equation again, but it is equation 55 cosine delta c r due is equal to one up on K 2 minus your K 1 then 2.443 that is delta max, right your minus 0.466 that is delta 0 that is sin of it is radian 0.466 plus your 0.7 cosine 2.443 that is K 2 cosine 2.443 and minus 0.25 that is K 1 cosine 0.466 that is delta 0 and if you compute all it will become is equal to 0.29; that means, delta critical angle will become 73.14 degree or 1.276 radian, right, directly you can put it there and you will get this answer. So, this is the answer now another one; this is this one among all this one is the easiest one, but only you need delta star star delta transformation now I will show you the figure, now I hope this you have understood, right that how to find out at your critical clearing angle or critical clearing time now this is another example it is a double

circuit line. So, find the critical clearing angle of the power system shown in figure 15, I will give you for a 3 phase fault on the point f, I will show you the diagram. So, generator is supplying initially one per unit megawatt power initially power it was supplying one per unit megawatt power under pre fault condition that is before fault before fault it was one.

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Soln.
Prefault operation.
$$X_A = 0.20 + \frac{(0.05 + 0.38 + 0.05)}{2} + 0.20$$

$$\therefore X_A = 0.64 \text{ pu.}$$

$$\therefore P_{e,A} = \frac{1.2 \times 1.0}{0.64} \sin\delta = 1.875 \sin\delta \text{ --- (i)}$$

Now this is the circuit connection this generator right reactance is given 0.20, here transformer is there 0.05 all j are there not uttering again and again.

This is line reactance 0.38, again transformer 0.05; this is also 0.05 line 0.3; 0.05, 0.20. So, before fault line; impedance was reactance was 0.3, but fault has occurred 3 phase fault is the middle of the line that is why here also I have seen this side it should be half this side it should be half. So, no confusion and total is in this line there is a fault and this side is j 0.19 this side is j 0.19, but total when there is no fault 0.38 and identical identical parameters and this side voltage generator voltage is one 0.20 per unit and this is infinite bus right. So, it is magnitude is one angle 0 per unit. So, now, pre fault condition when there is no fault. So, dont consider you put your finger here no no fault it is there so; that means, 0.2 should be added j i am not putting again and again it is reactance calculation that is your pre fault operation that is a; that means, curve a when the when look at this when when when when you are making a b c you know you have to imagine in this way that this is pre fault graph a when i will make x b it will be during

fault and when i will make c it will be after fault. So, a b c this way we will do it then we will not make any mistake. So, in this case this is your double circuit. So, this 2 line are in parallel. So, there is no fault; that means, equal equal it is 0.38 plus 0.1 0.05 0.1. So, 0.48 and 0.48 this 2 are in parallel. So, it will be 0.224 and this side 0.2 this side 0.2. So, 0.4 plus 0.24 it will become 0.64 per unit.

So, this pre fault condition this is pre fault or operation that x a will be 0.2 plus it is parallel equal. So, it will be taken half 0.05 plus 0.3 plus 0.05 by 2 plus this 1.2. So, it is coming x a is equal to 0.64 and the graph a is that your pre fault condition and voltage is given 1.2 and one throughout this 2 voltage will not change. So, it will be 1.2 into one divided by x a. So, 0.64 sin delta is equal to it will become 1.87; sin delta; that means, it will be your this graph green color graph a that is why I am making it P e a graph A; that means, this will be your graph a similarly now during fault before that you have to compute also this delta 0 angle on the green curve this delta 0 angle is also require right your P i is given 1 P i is given one per unit this is given. So, in that case in that case that delta 0 will be sin inverse one up on 8 point.

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(58)

The power angle δ_0 at the time of fault is given by

$$\delta_0 = \sin^{-1}\left(\frac{1}{1.875}\right) = 32.23^\circ \text{ or } 0.562 \text{ rad.}$$

Faulted Condition.

Fig. 15(a) shows the network connection during fault

Fig. 15(a) Circuit connection during fault.

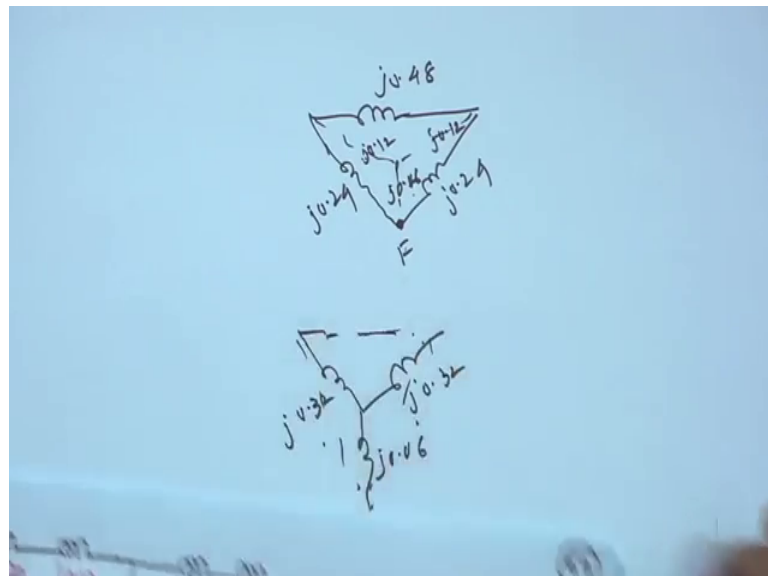
Your 7.5 because when P e is equal a is equal to P i operating at steady state right before fault. So, it will that is 1 is equal to one is given P i is equal to that is 1.875 sin delta the delta is equal to your sin inverse that is delta is equal to delta 0 at this point delta is equal

to delta 0 at this point delta is equal to delta 0 so; that means, you will get delta 0 is equal to sin inverse one on 8 point 1.875 that is coming 32.23 degree or 0.562 radian.

So, next is during fault. So, suppose fault has occurred at this middle of the line second line here. So, this side should be 0.19 this side should be 0.19. So, if it is shown, then you draw this diagram fault has occurred at the middle of the line, this is 0.2 of this line will remain same. This line will remain same. So, $j\ 0.05$, $j\ 0.38$, $j\ 0.05$, this is $j\ 0.05$ that will be half half $j\ 0.19$, $j\ 0.19$ then 0.05 .

This is 0.2, this is generator side this is infinite bus side actually this is infinite bus side somehow I have made this thing, I have removed this, but this is infinite bus and this is your circuit connection during fault right. So, this way you should know fault has occurred in the middle of the line. So, once you make this connection well look at that this is basically delta connection you have to convert it to star. So, delta star connection you can make it of your own I can give you the your final value right this is basically your just hold on this is basically your del delta delta connection I mean I just write for you only this part this part is a this is at delta connection suppose this is your fault this is fault position as a this is your f say am just putting it like this.

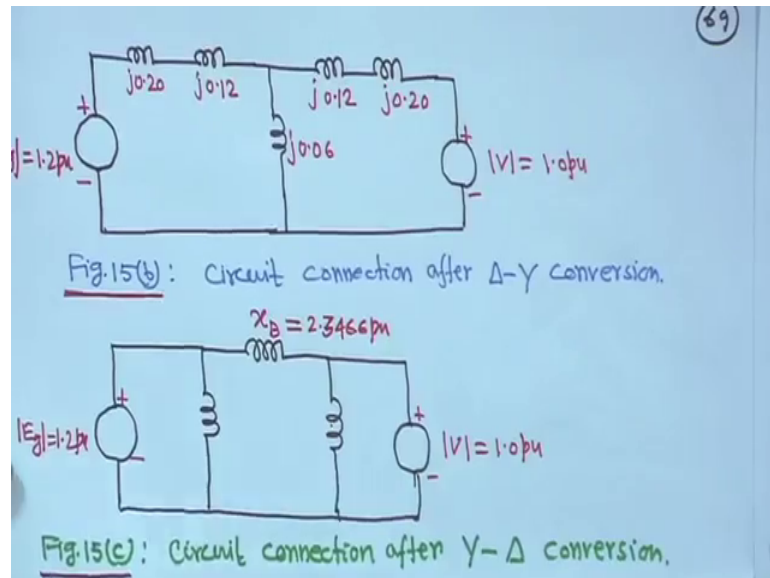
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So, this 2 are there 0.05 and 0.19. So, this should be your $j\ 0.2;4$ this side also 0.19, 0.05 this is also $j\ 0.24$ and this is 0.35, 0.05, 0.05. So, 0.48.

So, this side will be your $j 0.48$ and if you convert it to star you convert it to star if you convert it to star this side it will become your $j 0.12$ this is $j 0.12$ and this will become $j 0.06$, we just delta to star you know how to convert it you convert it. So, if you convert it then connection will be this side will be point $j 0.12$ this side will be 0.12 and to the; from here to the fault point $j 0$ point j that point f to 0.06 .

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So; that means, this one it is with that this side it was $j 0.20$ this side also $j 0.20$ so; that means, this 2 will be in series. So, $j 0.2 j 0.12$ this side $j 0.12 j 0$ point. This is $j 0.06$. So, this is the delta star conversion. Now if you make this one this is now star connection because this is this side will be 0.32 , this side will be 0.32 and this will be point and this one will be point $0 j 0.06$. So, this is now star connection this one again we have to converse star has to be converted to that delta. So, right if you converse star to the delta this 2, I have not computed no need because here you generator is there here this side is infinite bus is there for power times for we need only the x_b .

That is during fault this one is required this 2 are not required actually. So, this 2 I have not computed. So, this is a star connection I am showing you, but you will do it I am showing you. So, this is your star connection this is your star connection this side will be $j 0.32$ this side I actually I have made it for you this side 0 point 0 and this is your $j 0.06$ and this is your convert it convert it to delta convert it to delta this 2 side not

required only this one is required right. So, if we if you converse star to delta only only that side that x b.

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$$X_B = (0.2 + 0.12) + (0.12 + 0.2) + \frac{(0.12 + 0.2)(0.2 + 0.12)}{0.06}$$

$$\therefore X_B = 2.3466 \text{ pu.}$$

$$\rightarrow \therefore P_{e, B} = \frac{1.2 \times 1}{2.3466} \sin \delta = \underline{0.5113 \sin \delta}$$

Post fault condition

In this case, faulty line is open,

$$\therefore X_C = (0.2 + 0.05 + 0.38 + 0.05 + 0.2) = 0.88 \text{ pu.}$$

$$\rightarrow \therefore P_{e, c} = \frac{1.2 \times 1.0}{0.88} \sin \delta = \underline{1.363 \sin \delta}$$

So, if you convert, then it will become that 0.2; 0.12. So, 0.2 point, it is actually the formula is suppose R 1, R 2, R 3 then R 1 suppose R 1 star R 1, R 2, R 3, suppose you want to convert it to delta star to delta it will be R 1 plus R 2 plus R 1 R 2 divided by R 3. So, same way you have made it suppose for example, this is your; this side is your x 1. So, 0.2 plus 0.12, this side is you say this side is your x 2. So, it is 0.12 plus 0.2; both are equal plus product of this 2 divided by your x 3 that is your 0.06. So, if you make x b it will be 2.3466 per unit this is your what you call that that delta conversion this value, but this is not require for power transformer transfer this is not require at all.

Because nothing easier actually voltage across this one voltage across this one. So, only this one is require. So, once it is done then and this voltage 1.2 and one always remain same; that means, your electrical power P e b that is during fault it will be 1.2 into 1 divided by 2 that is x b 2.3466 sin delta this will become 0.5113 sin delta; that means, this graph; that means, this graph this graph will be 0.5113; sin delta during fault this graph and now post fault condition when that when the fault is cleared when fault is cleared when this fault is cleared. This line is isolated this line is isolated only this line will be there this fault is cleared, then you have to find out that what is the value of x c because we have to find out P e for curve c. So, this line is isolated when the fault is

clear. So, in this case fault line is open. So, this line is not there it is open, right. So, this line is gone only this line is there. So, in that case in that case just you add all the all the all the reactances; this one, this one, this one, this one, and this one just add because this line is open, right. So, in that case that faulty line is open. So, x_c is equal to 0.2 plus 0.05 plus 0.3 plus 0.05 plus 0.2 is equal to 0.8 per unit.

That means for curve c for this one that is after fault this curve for curve c. So, this is x_c and $P_e c$ is equal to 1.2 into 1.0 up on 0.88 sin delta is equal to 1.363 sin delta; that means, this graph the graph c is 1.363 sin delta right with getting all this thing. So, all the all the 3 graphs; we have got I mean power delivered during your pre fault during fault and post fault all you have got therefore, K_1 will be K_1 will be we have told you that it will be P_{max} during fault.

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$\rightarrow K_1 = \frac{0.5113}{1.875} = \underline{0.2727}$
 $\rightarrow K_2 = \frac{1.363}{1.875} = \underline{0.727}$
 Now compute δ_m' [Fig. 13(a)]
 $\rightarrow \delta_m' = \sin^{-1}\left(\frac{1}{1.363}\right) = \underline{47.19^\circ}$ or $\underline{0.8237 \text{ rad.}}$
 $\therefore \delta_m = \delta_{max} = (\pi - \delta_m') = (\pi - 0.8237) = \underline{2.317 \text{ rad}}$
 $\therefore \delta_m = \delta_{max} = \underline{2.317 \text{ rad}}$ or $\underline{132.75^\circ}$
 From eqn. (55)
 $\cos \delta_m = \frac{1}{K_2} [(\delta_{max} - \delta_m) \sin \delta_m + K_1 \cos \delta_m - K_1 \cos \delta_m]$

that is 0.5113 this one let me see I have to search it this is 0.5113 and this is we have got it that before fault 1.8 pre fault condition 1.875 that is 0.2727 K_2 is equal to your when your; after fault that is your 1.363; just now we have got graph C 1.363 divided by that your pre fault condition max 1.875. So, 0.727. Now you have to compute delta m dash. So, delta m dash actually this one this is your delta m dash that is the blue curve that is the blue curve right this is your delta m dash and in this is the intersection of this horizontal line and this blue one this is your delta m dash. So, in that case that your delta

m dash will be because we have seen that c curve it is 1.363 when delta is equal to your delta m dash that is 1.363 sin delta m dash.

So, at that time this power this is given P i is 1, this P i is 1 and when P i is 1 and delta m is equal to delta m dash. So, this graph will put that. So, in that case your delta m dash will be sin inverse one up on 1.363. So, that will come 47.19 degree or 0.8237 radian. Now delta m is equal to delta max is equal to pi minus delta m dash; that means, this one delta max is equal to pi minus delta m dash this one. So, we get delta max is equal to this 12.317 radian; that means, delta m is equal to delta max is equal to 2.317 radian or 132.75 degree once you got all this then equation 55 from equation 55 rewrite.

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$$\rightarrow K_2 = \frac{1.363}{1.875} = 0.727$$

Now compute δ_m' [Fig. 13(a)]

$$\rightarrow \delta_m' = \sin^{-1}\left(\frac{1}{1.363}\right) = 47.19^\circ \text{ or } 0.8237 \text{ rad.}$$

$$\therefore \delta_m = \delta_{\max} = (\pi - \delta_m') = (\pi - 0.8237) = 2.317 \text{ rad}$$

$$\therefore \delta_m = \delta_{\max} = 2.317 \text{ rad or } 132.75^\circ$$

From eqn. (55)

$$\cos \delta_{cr} = \frac{1}{(K_2 - K_1)} \left[(\delta_{\max} - \delta_0) \sin \delta_0 + K_2 \cos \delta_{\max} - K_1 \cos \delta_0 \right]$$

This equation this equation has been rewritten now put K 1 value K 2 value delta max value delta 0 value you will get the delta c r once you put it once you put it.

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$$\cos \delta_{cr} = \frac{1}{(0.727 - 0.2727)} \left[(2.317 - 0.562) \sin(0.562) + 0.727 \cos(2.317) - 0.2727 \cos(0.562) \right]$$

$$\therefore \cos \delta_{cr} = 0.4663$$

$$\therefore \delta_{cr} = \underline{62.2^\circ}$$

-1) A synchronous motor is receiving 25% of the power that it is capable of receiving from an infinite bus. If the load is doubled, determine the maximum value of the load angle.

soln. From Fig. 7,
 $P_{10} = 0.35 P_{max}$

$\delta_0 = 32.23^\circ$
 $\delta_m = \delta_{max} = 132.75^\circ$
 $\delta'_m = 47.19^\circ$
 $\delta_{cr} = 62.2^\circ$

Then this one you substitute all this value all are radian you have substituted all this is radian; that means, cosine delta c r will be become 0.46363; that means, delta c r will be 62.2 degree. So, results are summarized here for this problem results are here results are summarized that delta 0, we got 32.23 degree delta m dash we got 47.19 degree delta c r we got 62.2 degree and delta m is equal to delta max we got 132.7 degree.

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$$\therefore \cos \delta_{cr} = \frac{1}{(0.727 - 0.2727)} \left[(2.317 - 0.562) \sin(0.562) + 0.727 \cos(2.317) - 0.2727 \cos(0.562) \right]$$

$$\therefore \cos \delta_{cr} = 0.4663$$

$$\therefore \delta_{cr} = \underline{62.2^\circ}$$

Ex-1) A synchronous motor is receiving 25% of the power that it is capable of receiving from an infinite bus. If the load is doubled, determine the maximum value of the load angle.

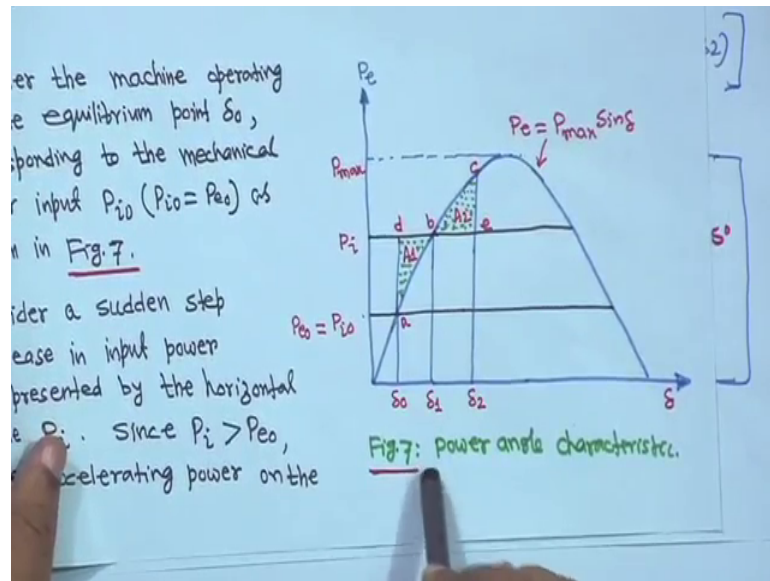
soln. From Fig. 7,
 $P_{10} = 0.35 P_{max}$

$\delta_0 = 32.23^\circ$
 $\delta_m = \delta_{max} = 132.75^\circ$
 $\delta'_m = 47.19^\circ$
 $\delta_{cr} = 62.2^\circ$

So, this is one and another one another example you take this is a this is a short example I mean small example suppose a synchronous motor is receiving 35 percent of the power

that it is capable of receiving from an infinite bus if the load is doubled determine the maximum value of the load angle right. So, it is said that it is given that synchronous motor receiving 35 percent of the power that is capable of receiving from infinite bus, but if the load is doubled determine the maximum value of the load angle. So, from figure 7; figure 7, if you go back then I think I have figure 7 in front of me.

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This is my figure 7. So, it is P_{e0} is equal to P_{i0} and this is $P_{max} \sin \delta$ this is figure 7 from figure 7. So, P_{i0} is equal to it is given 35 percent of the power. So, P_{i0} is equal to $0.35 P_{max}$ this is P_{max} this is P_{max} .

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$$\delta_0 = \sin^{-1}\left(\frac{P_{i0}}{P_{max}}\right) = \sin^{-1}(0.35) = 0.357 \text{ rad.}$$
$$P_i = 2 \times 0.35 P_{max} = \underline{0.70 P_{max}}$$
$$\therefore \delta_1 = \sin^{-1}\left(\frac{P_i}{P_{max}}\right) = \sin^{-1}(0.7) = \underline{0.775 \text{ rad.}}$$

In Fig. 7, δ_2 is the maximum value of load angle during the swinging of the rotor.

Using eqn. (46),

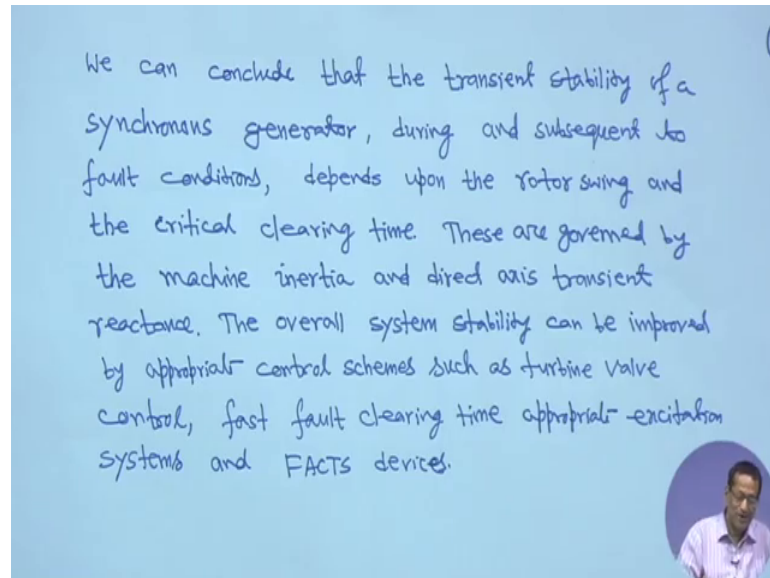
$$(\delta_2 - \delta_0) \sin \delta_1 + \cos \delta_2 - \cos \delta_0 = 0$$
$$\therefore 0.70 \times (\delta_2 - 0.357) + \cos \delta_2 - \cos(0.357) = 0$$
$$\therefore \delta_2 = \underline{72^\circ} \text{ or } \underline{1.25 \text{ rad.}}$$

So, P_{i0} is equal to $0.35 P_{max}$ therefore, you that is δ_0 is equal to $\sin^{-1} P_{i0} / P_{max}$ that is $\sin^{-1} 0.35$ is equal to 0.357 radian and now it has been doubled. So, P_i you will be is equal to 2 into $0.35 P_{max}$ because it has given if the load is doubled now, right. So, determine the maximum value of the load angle now it is doubled. So, it is P_i is equal to 2 into $0.35 P_{max}$ that is $0.7 P_{max}$ therefore, you have to you have to compute δ_1 that is your δ_1 .

So, that is δ_1 is equal to $\sin^{-1} P_i / P_{max}$ that is $\sin^{-1} 0.7$ it will become 0.775 radian. Now in figure 7 δ_2 is the maximum load angle during the swinging of the rotor. So, in this is figure 7, this is the δ_2 is the maximum rotor angle, right. So, using equation 46, you have rewriting equation 46; here the δ_2 minus δ_0 then $\sin \delta_1$ plus cosine δ_2 minus $\cos \delta_0$ only here δ_2 is unknown. So, put all these value δ_2 your this thing $\sin \delta_1$ right. So, put all these value here. So, δ_2 first I am writing this δ_2 minus δ_0 is 0.357 then $\sin \delta_1$ that is by your coming 0.7 your 0.7 and then your; here it is given that δ_1 is equal to $\sin^{-1} 0.7$; that means, $\sin \delta_1$ is equal to 0.7 . So, we have putting here $\sin \delta_1$ no confusion plus cosine δ_2 unknown minus $\cos \delta_0$ δ_0 is equal to 0.357 radian.

So, cosine 0.3 is equal to 0; that means, delta 2 maximum you are getting 72 degree or one 0.25 radian. So, this is that last example of this power system thing stability and finally, this; what is the conclusion. So, I have written something here.

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That we can conclude that the transient stability of a synchronous generator during and subsequent to fault conditions depends up on the rotor swing and the critical clearing time these are governed by the machine inertia and direct axis transient reactance, the overall system stability can be improved by appropriate control schemes such as turbine valve control fast fault clearing time appropriate your appropriate excitation systems and facts devices that is flexible transmissions devices right, but those are the thing that you can be improved.

Now, for power system stability studies whatever your; we have studied I mean little bit of steady state stability and that is basically that gradual increase of the load that is maximum your loading capability before losing synchronism then little bit we have tried to understand regarding dynamic or small signal stability that is due to small system disturbances and finally, transient stability for single machine infinite bus system that is for your; for large disturbances and we have also defined in this topic that what is infinite bus and we have tried to obtain that your critical clearing time.

So, with this those will be listening this last class one or 2 line that one or 2 few 2 things before closing this courses because this is the last one that starting from the beginning

that structural power system and various aspects of power system and there are and you have come to this transient your first system stability and within the within the given your time frame that we have tried to cover I think 9 or 10 chapters although there are many other chapters in power systems and whatever we have tried that all the all the your theories particular for classroom exercise that. So, many all the theory or theories are mathematical derivations all supported by good number of examples

And particularly for when you come to the iterative techniques that is load flows or the little bit of optimal system operation that is economic load dispatch we know that in the classroom or in the exam hall that it take it is time consuming without computer, but at least one or 2 iterations you can try from your side quickly that what is the result. So, in that in this lecture also I have shown I think 2 or 3 iterations load flow also Newton Raphson load flow also only couple of iterations and optimal economic load disperse also I have shown the step.

But that is basically coding is required not this thing, but we have tried to explain that this way this are way one can do it, but as far as classroom exam is concerned or your classroom exercise is concerned that you should make one or 2 iterations that and make every step is correct. So, with this your feedback will be more important for me and what I would like to tell that if you find any mistake or any error particularly that calculations. So, that it was all this numerical actually have been done by me I mean before coming to this lecture also that your delta star star delta transformation may be through 2 2 2 2 and half hours back I was calculating by calculator that whether everything is correct or not.

So, if I make any mistake or any error is there in calculation please mail me such that I can correct those numerical and whenever any writing is error or anything I have mistake that you please see only for 3 phase fault cases only my emphasis was to for z bus building algorithm and other thing little bit of Thevenin equivalent this that I pre assume that this are simple thing you know it with this I have to tell you that.

Thank you.