

Course Name: Power Electronics Applications in Power Systems

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Power Electronics Applications in Power Systems

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Lec 23: SVC in enhancement of synchronizing power coefficient

Welcome again in my course Power Electronics Applications in Power Systems. In the last few lectures, I am discussing the application of static var compensator in power systems. And in the last lecture, I discuss or I started discussion on how a SVC placement at the midpoint of a lossless short transmission line can improve the synchronizing power coefficient of the system. I explained in the last lecture what is synchronizing power coefficient and why it is so important and what is its role in power system stability. So therefore, we will continue to this derivation in this lecture as well. We will come up with an expression for the synchronizing power coefficient for a lossless short transmission line.

So, let us move forward and see what we were discussing in the last class. So, we are here actually, we are deriving the expression of synchronizing power coefficient, synchronizing power coefficient of a midpoint SVC compensated line. Now, we considered at the midpoint of this transmission line, we have a SVC and SVC is modeled as a variable susceptance. So, here is our assumption is that we consider lossless line, we consider short line.

Now, in addition to that, we will consider also another assumption that the line is symmetrical in nature. As of now, we have seen all the derivation for this particular course. I consider this assumption as well, that is the line is symmetrical. Now, what do we mean

by symmetrical transmission line? Symmetrical transmission line implies to the fact that the voltage at the both end of the line would be regulated and they would be made constant. They would be equal and they would be made constant irrespective of the loading. So, for this particular system, here we arrive at this expression. So, we will move forward with this expression. We will let us find out this expression for synchronizing power coefficient. So, I will write again. Derivation of synchronizing power coefficient for symmetrical lossless short transmission line: Here our assumptions are we have symmetrical lossless short transmission line short transmission line.

Now with this assumption we will proceed further and we will rewrite the expression that we received or that we derived in the last lecture that is these two expressions. This voltage representing this V_m is basically representing the voltage at the midpoint as you can see. So it is the voltage at the midpoint and δ_m is basically representing the angle of the voltage at the midpoint of the transmission line. So, therefore, we will rewrite this expression once again, $V_m \cos \delta_m$ is equal to $\frac{1}{X_c}$ or let us write X in the denominator and numerator it is $V_1 \cos \delta + V_2$ and $V_m \sin \delta_m$ is equal to $\frac{V_1 \sin \delta}{X_c}$. These are the two expressions we derived in the last lecture.

These are the two expressions we derived at the last lecture, but this does not consider that we have a symmetrical line. So, for symmetrical line, for symmetrical lossless short line this expression would be as we know that for symmetrical line V_1 is equal to V_2 , let us consider this is equal to V . So, this expressions will be V_m and we also know that for symmetrical line δ_m is equal to $\frac{\delta}{2}$. So, this is we already derived in previous lecture when I discussed midpoint compensation of a transmission line. So, therefore, this equations will be $V_m \cos \frac{\delta}{2}$ will be equal to $\frac{V \cos \delta + V}{X_c}$ and $V_m \sin \frac{\delta}{2}$ will be equal to $\frac{V \sin \delta}{X_c}$.

So, just I replaced this V_1 and V_2 equal to V and I also replaced δ_m is equal to $\frac{\delta}{2}$. Now, you know that here, so V_m is what? V_m is the voltage at the midpoint of the line. δ is the angular difference of the voltages at both ends of the line. Already if you can recall this circuit single-line diagram that I had drawn, that V_1 , sending end voltage was V_1 at an angle δ , receiving end voltage on V_1 , V_2 at an angle 0 . So angular difference between sending end voltage and receiving end voltage is δ , which is easy to understand. And, we also have derived the expression for X_c , which is equal to, if we can go back and see, X_c is equal to what? X_c is equal to this, $\frac{2}{2 - B_{SVC} X}$. So, $\frac{2}{2 - B_{SVC}}$ multiplied by X by 2 , where X is the reactance of the line or line reactance and B_{SVC} is susceptance of the SVC which is connected at the midpoint of the transmission line. So, this is already known to us. Now, what we will be interested from this? We will be interested to find out the compensating power or compensating power flow expression due to SVC placement at the midpoint of the line what would be that? That we already derived that P_{comp} is equal to V_m divided by X by 2 multiplied by $\sin \delta_m$. Now, we will put these values of this V_m δ_m .

Assumptions: Symmetrical, lossless, short transmission line

for Symmetrical, lossless, Short line
 $V_1 = V_2 = V$, $\delta_m = \frac{\delta}{2}$

Where, V_m = Voltage at the mid-point of the line,
 δ = Angular difference of the voltages at both ends of the line

Compensating Power flow expression due to SVC placement at the mid-point of the line, $V^2 \sin \delta = \frac{V^2 \sin \delta}{2}$ Where $X_{re} = X_T$

Where $\frac{x x_c}{2} = x_T$

We know, Synchronizing power Coefficient for uncompensated line [No SVC] = $\frac{\partial P}{\partial \delta}$
 " " " " for SVC compensated line [mid-pt] = $\frac{\partial P_{\text{avg}}}{\partial \delta}$

Compensating power flow expression due to SVC placement at the mid-point of the line,

$$P_{comp} = \frac{VV_m}{\frac{X}{2}} \sin \frac{\delta}{2} = \frac{V^2}{\frac{XX_e}{2}} \sin \delta = \frac{V^2 \sin \delta}{X_T}$$

$$\text{Where, } X_T = \frac{XX_e}{2}$$

$$\text{We know, synchronizing power coefficient for uncompensated line} = \frac{\partial P}{\partial \delta}$$

$$\text{Synchronizing power coefficient for SVC compensated line [mid-point]} = \frac{\partial P_{comp}}{\partial \delta}$$

$$\text{For SVC compensated line, } P_{comp} = \frac{V^2 \sin \delta}{X_T}$$

$$V_m = \sqrt{\left(V_m \cos \frac{\delta}{2}\right)^2 + \left(V_m \sin \frac{\delta}{2}\right)^2}$$

$$= \sqrt{\left(\frac{V(1 + \cos \delta)}{X_e}\right)^2 + \left(\frac{V \sin \delta}{X_e}\right)^2}$$

$$= \frac{V}{X_e} \sqrt{(1 + \cos \delta)^2 + \sin^2 \delta}$$

$$= \frac{V}{X_e} \sqrt{1 + (\cos \delta)^2 + 2 \cos \delta + (\sin \delta)^2}$$

$$= \frac{V}{X_e} \sqrt{2 + 2 \cos \delta} \quad ($$

$$V_m^2 X_e^2 = 2V^2 (1 + \cos \delta)$$

$$\text{Let us differentiate both side with } \frac{\partial}{\partial \delta}$$

$$2V_m^2 \left(\frac{\partial X_e}{\partial \delta} \right) X_e = -2V^2 \sin \delta \Rightarrow \frac{\partial X_e}{\partial \delta} = -\frac{V^2 \sin \delta}{V_m^2 X_e}$$

$$V_m = \text{Constant irrespective of loading } (\delta)$$

$$P_{comp} = \frac{VV_m}{\frac{X}{2}} \sin \frac{\delta}{2} = \frac{V^2}{\frac{XX_e}{2}} \sin \delta = \frac{V^2 \sin \delta}{X_T}$$

Synchronizing power coefficient of mid-point SVC compensated symmetrical, lossless, short transmission line.

$$P_{comp} = \frac{V_1 V_2 \sin \delta}{\frac{X}{2} X_e} = f(\delta, X_e)$$

$$k'_s = \frac{\partial P_{comp}}{\partial \delta} = \frac{2V^2 \cos \delta}{XX_e} - \left[\frac{2V^2 \sin \delta}{XX_e^2} \right] \frac{\partial X_e}{\partial \delta}$$

$$= \frac{V^2 \cos \delta}{X_T} + \left[\frac{V^2 \sin \delta}{\frac{XX_e^2}{2}} \right] \left(\frac{V^2 \sin \delta}{X_e V_m^2} \right)$$

$$= \frac{V^2 \cos \delta}{X_T} + \left[\frac{1}{X_T} \right] \left(\frac{V^2 \sin \delta}{X_e V_m} \right)^2$$

$$= \frac{V^2 \cos \delta}{X_T} + \left(\frac{P_{comp}}{V_m} \right)^2 \cdot \frac{X^2}{4X_T}$$

For uncompensated line

$$\frac{\partial P}{\partial \delta} = \frac{V^2 \cos \delta}{X}$$

The net increase of synchronising power coefficient for SVC compensated line

$$\Delta k_s = \frac{V^2 \cos \delta}{X_T} - \frac{V^2 \cos \delta}{X} + \left(\frac{P_{comp}}{V_m} \right)^2 \cdot \frac{X^2}{4X_T}$$

$$= V^2 \cos \delta \left[\frac{X - X_T}{X_T X} \right] + \left(\frac{P_{comp}}{V_m} \right)^2 \cdot \frac{X^2}{4X_T}$$

$$\therefore k'_s = (k_s) + \Delta k_s$$

$$k'_s > k_s$$

So, δ is here $\delta/2$. I just simply replace this δ by $\delta/2$ and we know that this $V_m \sin \delta/2$ is this. So, let us replace this. So, what we get is if we replace this, then this will be V^2 square divided by, here X_c would be there, here denominator, here $X/2$ will be denominator, so this will be $X X_c/2$, then $\sin \delta/2$. Now, if we consider that this $X X_c/2$, the denominator, that is this $X X_c/2$, let us consider as X_t . So, this expression would be then $V^2 \sin \delta/2$ divided by X_t . So, this is whereas, where we consider X_t is equal to $X X_c/2$, X_c is already we determine X we know that it is line reactance. Now, what we will do is that we know the synchronizing power coefficient. So, we know what is synchronizing power coefficient, synchronizing power coefficient expression is basically for uncompensated line, let us start with uncompensated line. Let us assume that there is no SVC over here, so that means no SVC, then this will be equal $dP/d\delta$. You can see already we have explained this in the lecture before.

So, this $dP/d\delta$ is basically representing the synchronizing power coefficient. So, synchronizing power coefficient is $dP/d\delta$, $dP/d\delta$ to be more correct. Similarly, for synchronizing power coefficient for SVC compensated line S-V-C compensated line, where we have S-V-C at the midpoint is equal to this $dP_{comp}/d\delta$. And we have to show that there is a difference between these two expressions. And let us see what is that difference. If one is $dp/d\delta$, another is $dp_{comp}/d\delta$. Now $dp/d\delta$ can be easily determined. I am coming to that. So let us first determine that SVC compensated line $dP_{comp}/d\delta$ synchronizing power coefficient. So, to do so, so what we need to do? We need to differentiate this P_{comp} with respect to δ . Now, here you can see this P_{comp} is a function of V which is regulated at the both end. So, V is constant over here. It is also function of this δ . It is also function of X_t . Now, we have to see that this δ as you know, δ depends upon the line loading. X_t basically depends upon X_t is a function of this X plus B SVC. So, let us write this. So, for SVC compensated line, compensated line, what is actually we get? P_{comp} is equal to V^2 square divided by $X_t \sin \delta/2$ where V is constant and regulated at the both end. This is what the property of symmetrical transmission line we consider and δ varies with line loading. So, it is a variable and X_t is a basically function of again that X and B SVC.

Now, you know that X is constant because it is line reactance it cannot be changed, but B SVC can vary, it is a variable according to the control strategy of the SVC. I already explained that we can finally model the SVC by a simple variable susceptance. Now, the susceptance of that particular SVC can be controlled according to the our requirement. So, B SVC is variable, B SVC can be variable with respect to δ as well, but X is remain constant, so as this V . So, therefore, what we have to see is, we know that X_t is function of X and B SVC.

In fact, X_t is equal to X_c by 2 where X_c we know that it is equal to $2 \sin \delta$ multiplied by X by 2. So, that is already determined in the last lecture that is this expression. And, so what we will do is that, we know that x_c will get changed because v_s v_c will get changed. Other than that x is constant, 2 is constant, so it would have been constant. But here we are interested to change the B SVC according to the loading, so that we can improve the synchronizing power coefficient. So, first thing that we have to develop is, in this particular expression, we have two variables, one is δ , another is x_e . So, I have to find out the dependency or differential equation of this $d x_e$ or $\frac{d x_e}{d \delta}$ with $\frac{d \delta}{d t}$. In order to find out this, let us find out the magnitude of this V_m , rather this V_m , because we already consider symmetrical lossless transmission line. So, we can write that V_m is equal to root of $V_m \cos \delta$ by 2 whole square plus $V_m \sin \delta$ by 2 whole square. I think this is you understood because $\cos^2 \delta$ plus $\sin^2 \delta$ will be equal to 1.

So, I can write this. Now, I will put the expression of $V_m \cos \delta$ from here, $V_m \sin \delta$ from here. So, what I will get? Let us see. So, this will be equal to V $1 + \cos \delta$ divided by x_c whole square plus this will be, I can put this expression of $V_m \sin \delta$ by 2 from this expression as well. So, what I will get here? This is $V \sin \delta$ divided by x_c whole square and then square root of this will be equal to V_m . I just simply replace this $V_m \cos \delta$ and $V_m \sin \delta$ from the previous expressions. Then what we will get, this is equal to 1 upon X_c root of, so we know that this is, if we just bring V even outside, so then what we will see is, or rather, so I can put this V so that this becomes equal to $1 + \cos \delta$ square plus $\sin \delta$ square or $\sin^2 \delta$ Now what is this actually? You know that $1 + \cos \delta$ square is basically can be splitted to V divided by X_c root of $1 + \cos^2 \delta$ plus $2 \cos \delta$ plus $\sin^2 \delta$. Now, again this summation of $\cos^2 \delta$ plus $\sin^2 \delta$ will be equal to 1. So, therefore, this can be written as v by x_e square root $2 + 2 \cos \delta$. Now, from this expression, I can write that v_m square x_c , I just put this x in the left hand side equation, v_m square x_c square is equal to v multiplied by, or rather if we take 2 outside, so $2 v$ $1 + \cos \delta$. So, is it correct? So, it is correct.

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For SVC Compensation

$$I_{comp} = \frac{V^2}{X_T} \sin \delta \quad \text{where } V = \text{Constant}$$

δ varies with line loading
 $X_T = f(X_c, B_{svc})$
 $[X_c = \text{Constant}, B_{svc} = \text{Variable}]$

$$X_T = \frac{X_c X_e}{2} \quad \text{where } X_e = \frac{2 - B_{svc} X_c}{2}$$

$$V_m = \sqrt{\left(V_m \cos \frac{\delta}{2}\right)^2 + \left(V_m \sin \frac{\delta}{2}\right)^2}$$

$$= \sqrt{\left[\frac{V(1 + \cos \delta)}{X_e}\right]^2 + \left[\frac{V \sin \delta}{X_e}\right]^2}$$

$$= \frac{V}{X_e} \sqrt{(1 + \cos \delta)^2 + \sin^2 \delta}$$

$$= \frac{V}{X_e} \sqrt{1 + \cos^2 \delta + 2 \cos \delta + \sin^2 \delta} = \frac{V}{X_e} \sqrt{2 + 2 \cos \delta}$$

$$\Rightarrow \frac{V_m^2 X_e^2}{2} = 2 V^2 (1 + \cos \delta)$$

let us differentiate both side with $\frac{\partial}{\partial \delta}$

$$2 V^2 \left(\frac{\partial X_e}{\partial \delta}\right) X_e = -2 V^2 \sin \delta \Rightarrow \frac{\partial X_e}{\partial \delta} = -\frac{V^2 \sin \delta}{V_m^2 X_e}$$

$V_m = \text{Constant irrespective of loading } (\delta)$

So, this is what the correct expression. Now what we will do is, one thing I did not do over here is that, if we just take this square of this v_m , so x_u will be square, so as the square of the v , so this will be the correct expression. Now what we will do is that, let us differentiate both side with δ . So, what we will get in this side, we will be having this expression as $2 V_m^2$, V_m^2 square will be differentiated. So, you know that V_m^2 square, V_m can be considered to be independent of this δ , but V_m will also vary with δ . So, therefore, if we just differentiate with this. So, this side will be $2 V_m^2 \frac{\partial X_e}{\partial \delta}$ and this side v is constant. So, therefore, $2 V^2 \cos \delta + 2 V^2 \sin \delta$ is a constant if we just differentiate with respect to δ . So, this will be minus $2 V^2 \sin \delta$. So, therefore, from this we can find out $\frac{\partial X_e}{\partial \delta}$ is equal to minus $V^2 \sin \delta / V_m^2 X_e$, here since we are differentiate with respect to this X_e , so another X_e term would be there, so that X_e^2 is differentiated with respect to δ that is $2 X_e \frac{\partial X_e}{\partial \delta}$, so one X_e term would be here as well.

Now remember, here this is done considering that V_m will be kept constant irrespective of loading or irrespective of the change of the δ . So, this differentiation is based upon the assumption that V_m is kept constant irrespective of the line loading, okay. So, which is one of the, you know, goal for SVC placement at the midpoint of the transmission line to keep the midpoint voltage constant irrespective of the line loading. So, this derivation is based upon this assumption as well, that we consider V_m constant irrespective of the line loading. So, this is one expression we get. Now, we know that this P_{comp} is this and X_T is basically function of X_c as well. So, if we write it in the next page, so what we can write as, so from the previous page, I can just copy this P_{comp} is equal to P_{comp} is equal to V^2 square divided by $X_T \sin \delta$. So, what is the expression? This expression gives you the expression for power flow of the midpoint SVC compensated short symmetrical lossless

transmission line. So, where we can, we know that X_t is equal to X_c by 2. So, this can be written as $V^2 \sin \delta$ divided by X_c divided by 2.

So, as we said that here V is constant. V is constant because we consider symmetrical line for symmetrical line and x is also constant. Line reactance cannot be changed. It depends upon the line design and as long as there is no change in the design, the line reactance will be constant, not change, unchanged. So, only parameter that will vary with respect to this δ is this x_c and this δ itself. So, therefore, if we take differentiation, let us say $\frac{dP}{d\delta}$, so what we can write is, it is equal to, so here are two variables, one is this δ itself, another is x_c , which can vary with the line loading. So therefore, we can write it as a , if we assume that first x_c is constant, so we can write this is equal to $V^2 \sin \delta$ divided by x_c by 2 $\cos \delta$ plus this $V^2 \sin \delta$. Let us consider δ constant now, $\sin \delta$ multiplied by x_c . Now, here you know that if we differentiate with respect to δ , that is 1 upon x_c , so this will be equal to minus, this will be equal to square, this will be equal to 2. So, this multiplied by $\frac{dx_c}{d\delta}$. So, this is the differentiation of x_c with respect to δ .

Now, what we can write? This, let us write $V^2 \cos \delta$ divided by x_c , x_c by 2, which let us consider that this is X_t . So, this is X_t . Then this part is $V^2 \sin \delta$ divided by x_c^2 by 2 multiplied by this $\frac{dx_c}{d\delta}$. Now what we will do? We will put this $\frac{dx_c}{d\delta}$ expression what we got in the last page. So that is this. So, if I copy and this expression there, so since there is a negative, so this will be positive multiplied by, let us see what it was, $V^2 \sin \delta$, it was $V^2 \sin \delta$ divided by $V^2 \sin \delta$, $V^2 \sin \delta$. I just simply put this $\frac{dX_c}{d\delta}$ at this particular expression. Now we will keep on simplifying this. How we can keep on simplifying? So this will be as it is, this will be $V^2 \cos \delta$ divided by X_t , where you know X_t is equal to what? It is equal to X_c by 2 and plus this $V^2 \sin \delta$ and $V^2 \sin \delta$ are already there. So, we can write $V^2 \sin \delta$ square and $V^2 \sin \delta$ and x_c square are there.

So, just I am just keeping $V^2 \sin \delta$ and x_c and $V^2 \sin \delta$ within a square that I can write right. Then what we will get? This multiplied by 1 upon this x_c would be there, this x_c by 2 would be there, this x_c would be there. So, this multiplied by x_c divided by 2. Now, what is that x_c divided by 2? That can be written as X_t . So, we can write it again this is equal to $V^2 \cos \delta$ divided by X_t plus $V^2 \sin \delta$ divided by $V^2 \sin \delta$ whole square multiplied by 1 upon X_t .

So, that is what the synchronous power coefficient that is what the synchronous power coefficient of the symmetrical lossless short transmission line. That is what the, this is what the synchronous power coefficient, synchronizing power coefficient of midpoint HVC compensated symmetrical lossless short transmission line. So, this is what the expression of synchronizing power coefficient of symmetrical lossless transmission line. Now, we can

do further derivation of this. How can we do further derivation? So, let us consider because you know that we already know that this $v^2 \sin \delta$ divided by x_t basically equal to p_{comp} .

So, we can write this as a $v^2 \cos \delta$ divided by x_t plus this $v^2 \sin \delta$ divided by V_m , I am just multiplying x by 2 inside this square. So, what I have to do is, I have to, since I have divided this x by 2 here, so I have to multiply x square by 4 here divided by x d. Now, what we know that this $V^2 \sin \delta$ divided by this, this is nothing but X_t which is this, so this can be written as P_{comp} , so this is equal to, this is equal to $V^2 \cos \delta$ divided by X_t plus, so this is basically P_{comp} . So P_{comp} divided by V_m whole square multiplied by x square divided by 4 x_t . So, this expressions we got from for the synchronizing power coefficient of the midpoint SVC compensated line.

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$P_{comp} = \frac{V^2 \sin \delta}{x_t} = \frac{V^2 \sin \delta}{\frac{x x_c}{2}}$ [$V = \text{constant for symmetrical line}$
 $x = \text{constant}$]

Synchronizing Power coefficient of mid-point SVC compensated Symmetrical, lossless, short transmission line

$$\begin{aligned} \frac{\partial P_{comp}}{\partial \delta} &= \frac{V^2 \cos \delta}{\frac{x x_c}{2}} - \frac{V^2 \sin \delta}{\frac{x x_c}{2}} \left(\frac{\partial x_c}{\partial \delta} \right) \\ &= \frac{V^2 \cos \delta}{x_t} + \frac{V^2 \sin \delta}{\frac{x x_c}{2}} \left(\frac{V^2 \sin \delta}{V_m^2 x_c} \right) \quad \left[x_t = \frac{x x_c}{2} \right] \\ &= \frac{V^2 \cos \delta}{x_t} + \left[\frac{V^2 \sin \delta}{V_m x_c} \right]^2 \cdot \frac{1}{\frac{x x_c}{2}} = \frac{V^2 \cos \delta}{x_t} + \left(\frac{V^2 \sin \delta}{V_m x_c} \right)^2 \cdot \frac{1}{x_t} \\ &= \frac{V^2 \cos \delta}{x_t} + \left(\frac{P_{comp}}{V_m} \right)^2 \cdot \frac{x^2}{4 x_t} \\ \text{For uncompensated line } \left(\frac{\partial P}{\partial \delta} \right)_{uncomp} &= \frac{V^2 \cos \delta}{x} \\ \text{The net increase of Synchronizing power coefficient for SVC compensated line} &= \frac{V^2 \cos \delta}{x_t} - \frac{V^2 \cos \delta}{x} + \left(\frac{P_{comp}}{V_m} \right)^2 \cdot \frac{x^2}{4 x_t} \\ &= V^2 \cos \delta \left[\frac{x - x_t}{x x_t} \right] + \left(\frac{P_{comp}}{V_m} \right)^2 \cdot \frac{x^2}{4 x_t} \end{aligned}$$

So, this is what our expression final expression is. What was the expression for uncompensated line? This $\frac{\partial P}{\partial \delta}$ was how much? We know that here for uncompensated line, what would be the expression of P ? Look at this single-line diagram. So, for uncompensated line, for uncompensated line, what would be the expression for P ? P will be equal to this $v_1 v_2$ divided by $x \sin \delta$. And since we consider v_1 and v_2 are equal for symmetrical line, so this will be expression of the power flow for uncompensated line, since v_1 is equal to v_2 . That we are, since v_1 is equal to v_2 for a symmetrical line. So, if we just differentiate with respect to δ , so what we will get $v^2 x$ is here constant because v is the voltage of both end which is regulated by the consideration of symmetrical line x is constant.

So, therefore, $\frac{dP}{d\delta}$ will be equal to $V^2 \cos \delta$. So, we can write this is equal to $V^2 \cos \delta$. So, this is synchronizing coefficient for uncompensated line, uncompensated line. And this is what the synchronizing power coefficient for compensated line. So, what is the difference of these two? So, you can see if we just compare this with this, this is having an additional term, which means that the synchronizing power coefficient when we have midpoint SVC compensated line will be higher than the uncompensated line.

So, therefore, the net increase of synchronizing power coefficient for SVC compensated line would be equal to this minus this. So, this will be equal to $V^2 \cos \delta$ divided by X minus $V^2 \cos \delta$ divided by X plus this plus P_{comp} divided by V_m^2 multiplied by X^2 . So, this can be written as if we take $V^2 \cos \delta$ common. So, this can be written as $X^2 \cos \delta$ minus $X^2 \cos \delta$ plus $P_{\text{comp}} V_m^2$ whole square multiplied by X^2 . So, this is what the net increase of synchronizing power coefficient.

So, this is something is very important to understand. So, when we have a SVC at the midpoint of a transmission line, irrespective of whether it is a short line or long line, it will increase the synchronizing power coefficient. Here we consider the short line, but this can be shown that this is the same thing will happen to be true for the long line as well. So, important remark over here is that, remark is that the above exercise or above derivation shows the presence of SVC in a transmission line, in a lossless transmission line improves or increases the synchronizing power coefficient, which is an important parameter in transient stability. And already I discussed the significance of synchronizing power coefficient is that it measures the stiffness of the line. How steep it is due to the fault and similar kinds of large disturbances.

So that is eventually improved with this SVC compensated line that we can mathematically show here. Now, here one thing that you can see, I discuss that here our assumption in whole discussion was that the role of the SVC will be to keep the midpoint voltage constant irrespective of the loading, in fact. And our all the previous studies are also based upon this consideration only that the role of the SVC is to keep the midpoint voltage constant irrespective of the loading. But, this has some practical deficiencies which I already discussed. First of all that to do so whatever the size of SVC we require that will be very large and that would be practically infeasible.

That is one of the bottleneck of that. But apart from that, it is also not advisable that always you need to maintain the midpoint voltage constant. There are some occasions SVC can also be useful in modulating the midpoint voltage and these are very dynamic changes and these are very short-duration changes. So, therefore, we will also see the role of the SVC in the modulation of midpoint voltage and thereby its impact on this power system stability. So, so far from my discussion, I considered the role of the SVC in improving this or enhancing the transient stability in terms of increasing the stability margin, in terms of the

increase in what we call synchronizing power coefficient. But apart from that, it can also be useful for creating damping of the system.

So, those things we will be discussing mostly in the next lecture. I want to give some of the feel or some of the core idea of this right now. So, this is the first remark. This is one of the remarks and a second remark was SVC can also increase the stability margin. So, those things I already established with mathematical analysis and the conceptual idea. Now, what we will see over here is that the role of SVC in power system damping.

If you can remember at the very first lecture of when I started this module that is application of SVC, I said that SVC can increase the steady state power transfer capacity which I have already shown. Now, I have shown that how can SVC impact on this transient stability of the power system. Then, what I am going to show right now, which I will continue in the next lecture is how it is useful in damping the power system oscillations. Now to do so, we have to come out from the idea that SVC would always maintain this midpoint voltage constant. Rather, we need to understand that, to dampen the power system oscillations, SVC can be useful in particular by providing or by enhancing appropriate damping.

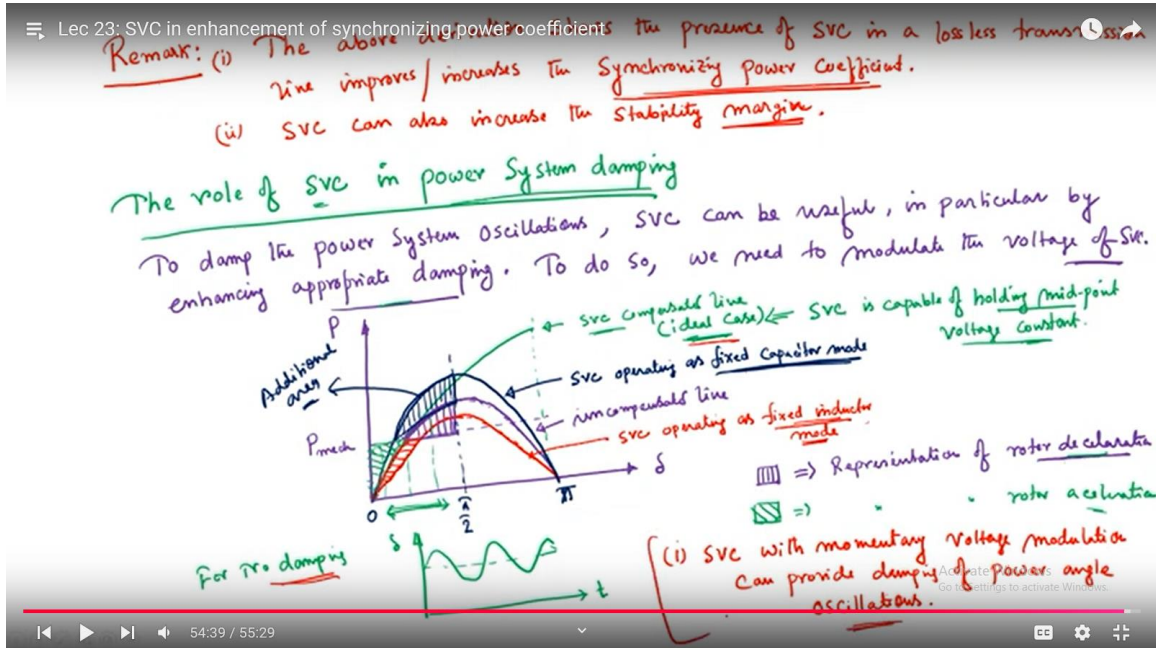
So, this is something very important and to do so, we need to modulate the voltage. So far our discussion was limited to the fact that we always planned that SVC should be capable to hold the midpoint voltage constant. But this will hold true for steady-state analysis, but for dynamic cases in particular to enhance the damping we need this SVC to modulate the voltage at the midpoint and thereby it can improve the damping. How it can improve? Let us see pictorially.

So, let us again revisit this idea with this P delta characteristics. Suppose this is the P-delta characteristic for the uncompensated line. So, this is supposed P-delta characteristic for the uncompensated line. Now, suppose this is what the mechanical power, this is what P mechanical and this is what the operating point. Now also I have seen that this, if we consider that SVC is designed to hold the midpoint voltage constant, then it will revise this P delta characteristic, something like this. So this is for the SVC compensated line providing the ideal case, providing that SVC is capable of holding.

So, the ideal case in the meaning that SVC is capable of holding the midpoint voltage constant. So, when we will design the SVC to hold the midpoint voltage constant, this will be the characteristic. However, that SVC can be also modeled as a fixed capacitor or a fixed inductor mode. So, this is the characteristic corresponds to SVC operation at the fixed capacitor fixed inductor mode.

So, here SVC operating at operating as fixed inductor mode. Why it is so? Already I explained in the, I already mathematically derived this expression and I explained over here. In the inductive mode of operation, the characteristic will be something like that.

Now, so for the inductive mode of operation, it will be something like that. Now, this is the fixed inductor mode of operation and when the SVC will be operating as a fixed capacitor mode, the characteristic will be something like this. So, this is for SVC operating as fixed capacitor mode or fixed capacitor mode of operation.



Now one thing that you can see over here is, that already I explained that the theoretical maximum limit of the stability is this, which corresponds to δ is equal to π by 2. This is δ is equal to π . So this is what the theoretical maximum stability limit. Now you can see that this hatch area, this hatch area beyond this operating point represents the deceleration area. This hatch area is basically representation of deceleration area. Now, what is that stands for? So, this hatch area is the representation of rotor deceleration, where the rotor decelerates. Now, why it decelerates? because in this particular region, the electrical power is above the mechanical power. So, that is why rotor will decelerate. However, this particular area This particular area is representing rotor acceleration. In fact, this was hatched in a different way in order to avoid the confusion I hatched the way it is shown in the figure.

So, this is the representation of rotor acceleration. Now, higher and higher this area would be better. You know actually without damping if we consider the whole line to be lossless, the rotor will keep on accelerating and decelerating and it will change from the point of this, from the operating point to the fault clearing or maximum value of δ . It will keep on increasing the value of δ and it will keep on reducing. Now we need some sort of damping of this. So basically if we, for no damping, for no damping what it would be, if we plot this δ with respect to time, then it would be something like that.

So, it will accelerate and decelerate and it will like that. We need some sort of damping to this, so that it will quickly settle to some point and that is what is called power system damping, that is what called power system damping. Now, what is the role of SVC is, it can momentarily change or modulate the voltage, so that you can increase this deceleration area and also this acceleration area. How it is possible you can see, instead of operating it a ideal case when it will be responsible to hold the midpoint voltage constant, If we use it as a fixed capacitor mode, now what is the role of the fixed capacitor? Fixed capacitor mode means it will momentarily increase the voltage at which the SVC is placed, then it will get some additional deceleration area like this, this is what the additional deceleration area. This is what the additional area, additional area by momentarily increase the voltage at which this SVC is placed by operating as a fixed capacitor mode. Similarly, here also when we need damping to descent, so instead of using it for the ideal case, if we use for fixed inductor mode, what a fixed inductor mode does, it momentarily reduces the voltage.

And, to do so, you will get this is the additional area, if we operate at fixed inductor mode. So, instead of keeping this SVC voltage constant, if we can modulate it, we can improve the system damping. And, that is exactly done by this SVC. In fact, that is done by STATCOM as well. When I will discuss this, I will again revisit and show you that the same discussion will be hold for the STATCOM, Static Synchronous Compensator as well.

So, therefore, two important comments that you can note down, one is number 1, SVC with voltage modulation or rather I should say that momentary voltage modulation can provide damping of power angle oscillations. So we will revisit this idea in the next class once again and show you how can you model this SVC and you can effectively provide damping of the oscillations or damping of the oscillations of the power angle in more detail. So thank you for your attention. Thank you.