

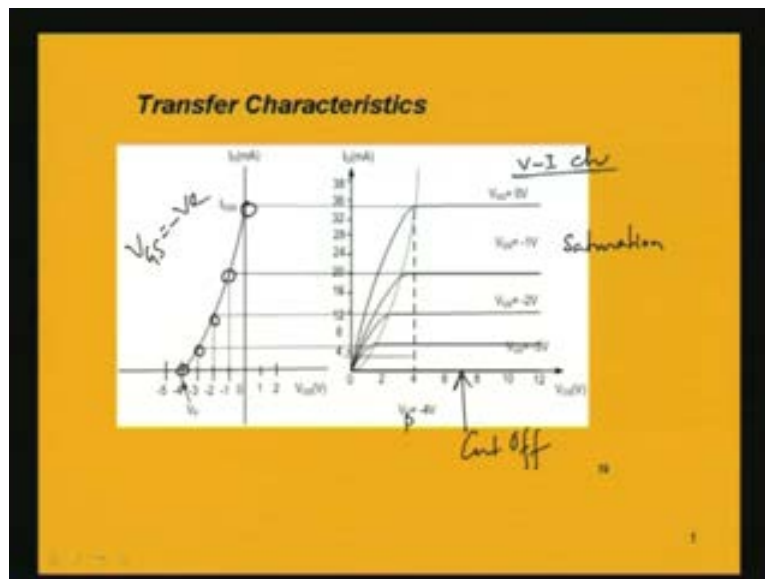
**Basic Electronics**  
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**Module: 3 Field Effect Transistors**  
**Lecture-8**

**Junction Field Effect Transistor (JFET) as an amplifier**

In the last class we discussed about the JFET or the junction field effect transistor and we have seen the physical construction as well as the V-I characteristics of the device. In order to use it in a circuit we have to find out the small signal model and using this small signal model in the amplifier circuit we can then analyze and find out the voltage gain, input impedance, output impedance, etc. First of all we must know about the small signal model and for that let us first discuss about the transfer characteristic of the JFET. Transfer characteristic of the JFET means the characteristic between the drain to source current and gate to source voltage and here we are showing the V-I characteristic and the transfer characteristic side by side for easy understanding.

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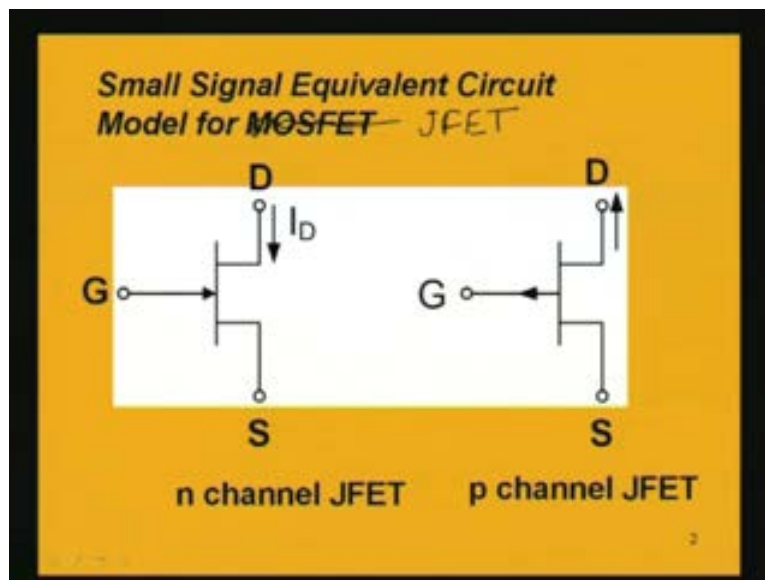
Here the V-I characteristic that is the characteristic between the drain current and the drain to source voltage, is shown for various values of the gate to source voltage. This is the V-I characteristic and from the V-I characteristic we can plot the transfer characteristic. This V-I characteristic is for various value of gate to source voltage from zero to negative because we cannot use gate to source voltage positive; we know that. There is no enhancement region in this JFET device. When gate to source voltage is zero, the corresponding saturation current in the drain is known as  $I_{DSS}$ . If we go on now increasing the gate to source voltage in the negative region that is we go on decreasing

the gate to source voltage from zero to -1 to -2 etc, then these are the different characteristics for the  $I_d$  and our important region is the saturation region. This region is saturation where we use the JFET as an amplifier and if we go on decreasing the GS, voltage between gate to source and reach the value which is known as the pinch-off voltage then your current in the drain is zero.

This is the cut off for this JFET and for a particular JFET we are considering this with the typical value of pinch-off as say -4 volt. This is the pinch-off voltage. At voltage below -4 volt between gate to source, the current is zero and at voltage between GS is equal to zero volt, we have this  $I_{DSS}$  as the saturation current. If we extend the current to the left or if we proceed this plots to the left and let it meet the ordinate from that particular gate to source voltage we get the corresponding points. That is for example when  $V_{GS}$  is equal to -1 volt, we have the saturation current of say 20 milliampere. If we extend this line to the left corresponding  $V_{GS}$  of -1 volt and this current of -20 will have this point. Similarly the points can be marked off with, the minimum point is -4 volt  $V_{GS}$  which is giving the zero drain current and the other maximum drain current is  $I_{DSS}$  which is at  $V_{GS}$  is equal to zero volt. You cannot go beyond this. You cannot increase  $V_{GS}$  in the positive direction. So the drain current is maximum at  $I_{DSS}$  and minimum at zero. In between if we mark 3 or 4 points and plot a curve through them, join these points and get a curve that is the transfer characteristic. The transfer characteristic is only in the region where  $V_{GS}$  is negative; not in the region where  $V_{GS}$  is positive.

We have earlier got small signal equivalent model for MOSFET. Now let us try to find out the small signal equivalent model for JFET.

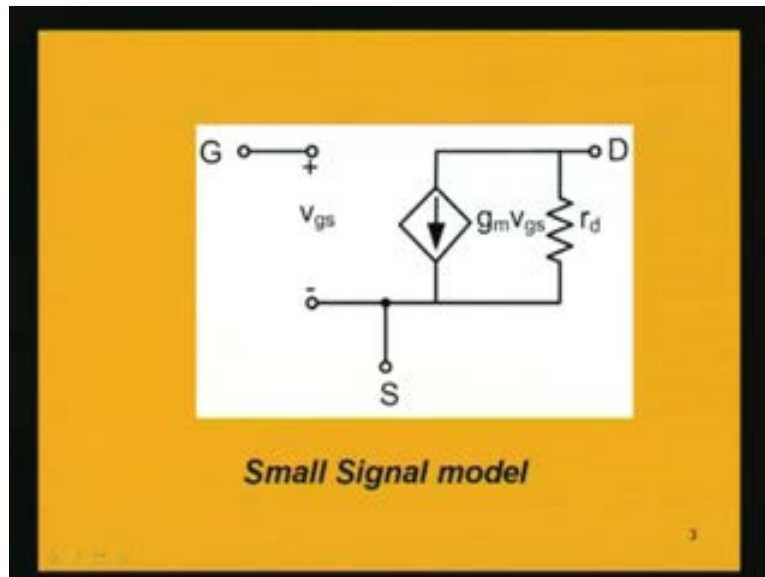
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If we now focus on the symbol or symbolic representation of the JFET, here the three terminals gate, source and drain it is like the three terminals of the transistor BJT that we discussed earlier. Now we will have to fit in the small signal model which will represent the characteristic of the JFET device or the small signal model should reflect the behavior of the JFET device. From the characteristic curve between the  $I_D$  and  $V_{DS}$  which we have plotted here we see that  $I_D$  curves are almost horizontal. But in fact there is a little slope to the right; there is a little slope in the  $I_D$  curve to the right. The resistance between the drain and source is not exactly infinite but it is having a finite value, although this value is very high. That resistance let us name it small  $r_{ds}$  and the drain to source current is given by current source. As we have seen in the earlier example of MOSFET it was  $g_m$  into  $V_{gs}$ .

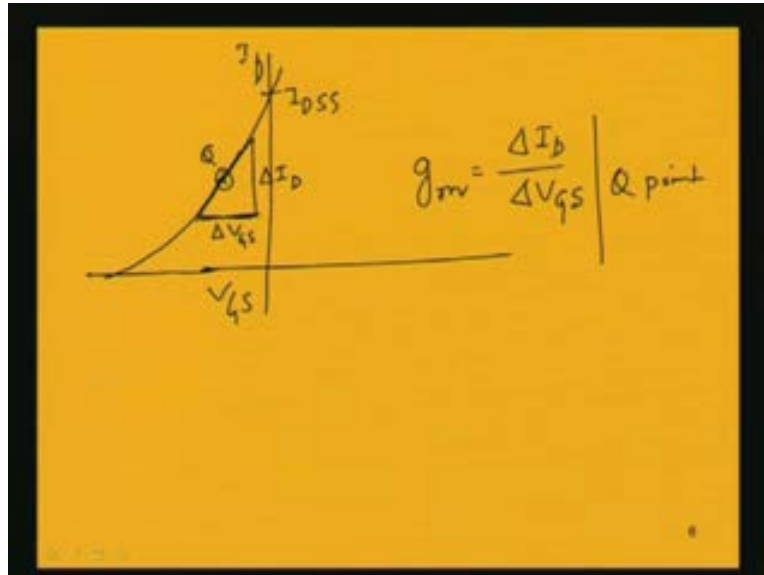
Similarly if we now draw the small signal model it will be exactly same as the MOSFET device. But what is the  $g_m$  or the transconductance that we have to know.

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The transconductance is obtained from the transfer characteristic. It is actually  $\frac{dI_D}{dV_{GS}}$ . That is to be obtained or we can analytically or mathematically also proceed to find out this derivative which is nothing but  $\frac{dI_D}{dV_{GS}}$  around the operating point. For a particular device under consideration if the operating point is given as say  $V_{GSQ}$ ,  $I_{DQ}$  this is the operating point, means the voltage between gate to source at the operating point and the drain current is giving a particular point or operating point or it is called quiescent point. Around that operating point if we find out the slope of the transfer characteristic that is the characteristic between  $I_D$  and  $V_{GS}$  that is the  $g_m$  or transconductance. Here basically if we know the operating point, suppose the operating point is here say this is  $V_{GS}$ , this is  $I_D$  in the negative region only.

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So it is like this. This is  $I_{DSS}$  and this is  $I_D$  zero. If this is the Q point, around the Q point we have to find out this slope. This is the small region around this Q point. You will have to find this  $\Delta I_D$  by  $\Delta V_{GS}$ . By changing the voltage between gate to source a little the corresponding change in the drain to source current that ratio between the  $\Delta I_D$  and  $\Delta V_{GS}$  around this operating point that will give you the transconductance. This is the transconductance around the operating point or at the operating point or Q point. That can also be found out analytically because we know the relation of the drain current with  $V_{GS}$ . What is that relation? That relation is  $i_D$  equal to  $i_{DSS}$  into  $1$  minus  $v_{GS}$  by  $v_P$  whole squared.

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$$g_m = \left. \frac{di_D}{dv_{GS}} \right|_{V_{GS}=V_{GSQ} \text{ const}}$$

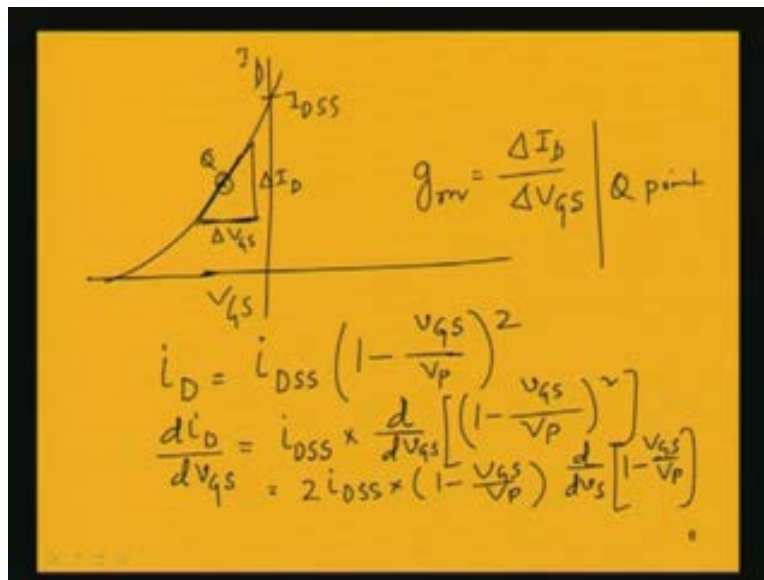
$$i_D = i_{DSS} \left( 1 - \frac{V_{GS}}{V_P} \right)^2$$

$$g_m = \frac{i_D}{V_{GS}}$$

If we know the current relation we can find out the  $g_m$  from this  $i_D$  by  $dv_{GS}$  at the operating point or Q point. That means we will have to find the differential of the drain current with respect to the gate to source voltage and mind it this is the instantaneous value of drain current. We are now going towards the AC operation because we are using the JFET as an amplifier. All this discussion will consist of the instantaneous value of current and voltage because apart from the biasing voltage we are now applying a small signal and because of this both DC and AC, we will have the corresponding quantities in current and voltage as instantaneous values which is denoted by small i capital D small v capital GS. This is to be kept in mind. If we find out this derivative and find its value at the Q point or the operating point, that will give the transconductance.

What is the derivative of this  $i_D$  equal to  $i_{DSS}$  into  $1$  minus  $v_{GS}$  by  $v_P$  whole square? Find out the derivate of this  $i_D$  equal to  $i_{DSS}$  into  $1$  minus  $v_{GS}$  by  $v_P$  whole squared.

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If we want to find its derivative with respect to  $v_{GS}$ , this is a constant term. The derivative of this term  $i_D$  by  $dv_{GS}$  of this whole term. This 2 will come to  $i_{DSS}$ . Then the derivative of this whole term will give 2 into this will come into  $1$  minus  $v_{GS}$  by  $v_P$ . Derivative of this square term will give me 2 into this. Then derivative of  $dv_{GS}$  or this term  $1$  minus  $v_{GS}$  by  $v_P$ . It will be only  $-1$  by  $v_P$ . We get  $2 i_{DSS}$ . Basically this will be  $2 i_{DSS}$  into  $1$  minus  $v_{GS}$  by  $v_P$  into  $-1$  by  $v_P$ . But that has to be evaluated at the Q point and at the Q point we have the value of  $v_{GS}$  as  $V_{GSQ}$  and this  $i_{DSS}$  is a current which is the maximum drain current when  $v_{GS}$  is equal to zero. That value is a constant value we know from this specifications. It is written as capital  $i_{DSS}$  and at the Q point this will be simply capital  $V_{GS}$  by  $V_P$ .

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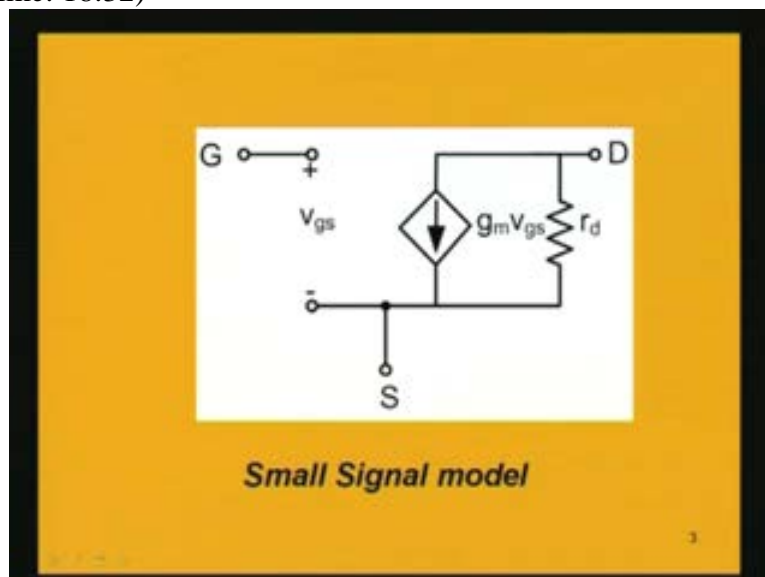
$$+ 2I_{DSS} \left(1 - \frac{V_{GS}}{V_P}\right) \left(-\frac{1}{V_P}\right) \bigg|_{Q\text{ point}}$$

$$\frac{di_D}{dv_{GS}} = 2I_{DSS} \left(1 - \frac{V_{GS}}{V_P}\right) \frac{di_D}{dv_{GS}} \left(1 - \frac{V_{GS}}{V_P}\right)$$

$$\therefore g_m = \frac{2I_{DSS}}{|V_P|} \left(1 - \frac{V_{GSQ}}{V_P}\right)$$

Finally we get  $2 I_{DSS}$  by  $V_P$  with a minus sign;  $1$  minus  $V_{GS}$  by  $V_P$ . But as this transconductance will be positive we will use modulus of  $V_P$  term. Instead of writing  $V_P$  that is pinch-off voltage, we are writing a modulus. Because  $V_P$  will have a minus sign its modulus will be taken. This relation of this transconductance is important because from this relation if we know these values we can find out the transconductance of the device. If we know  $I_{DSS}$ ,  $V_P$  and if the value of this  $V_{GS}$  that is the Q point  $V_{GS}$  is known, then we can know the transconductance. At the operating point we can write it as  $GSQ$  to make it clear that we are writing at the operating point. Once we know the transconductance we can fit it into the small signal model and draw the small signal model as we have drawn in the earlier cases of MOSFET.

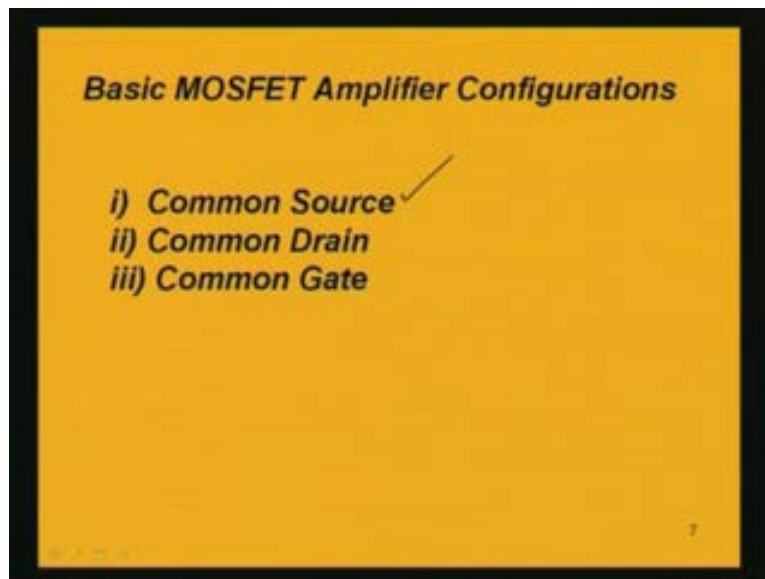
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It is similar because the gate current is zero. High infinite input impedance, so gate current will be zero. Gate and source is like open circuit. This is the current source which is between drain and source. That is a current source which is given by  $g_m v_{gs}$  and this is the resistance between drain and source which is a high resistance value and conventionally the admittance between the drain and source is given in the data sheet or specification sheet. We will have to find out its reciprocal and that will be the resistance between the drain and source. This is as simple as that; we do not have a complicated small signal model. Now what will be done is that we will have to incorporate this small signal model into the amplifier.

JFET amplifier, as we discussed in MOSFET amplifier, will have a biasing scheme for properly choosing the Q point and then a small signal will be applied which we want to amplify without distortion. It should be small enough and then depending upon which configuration we are using for the amplifier we will have the corresponding network. Earlier we have found that we have three different configurations of MOSFET amplifier. Those are common source, common drain and common gate. Similarly in JFET also we have three configurations of amplifier which are common source, common drain and common gate. All these analysis are similar to the MOSFET amplifier that we earlier discussed. If we now consider the JFET as an amplifier say for example we will discuss common source JFET amplifier.

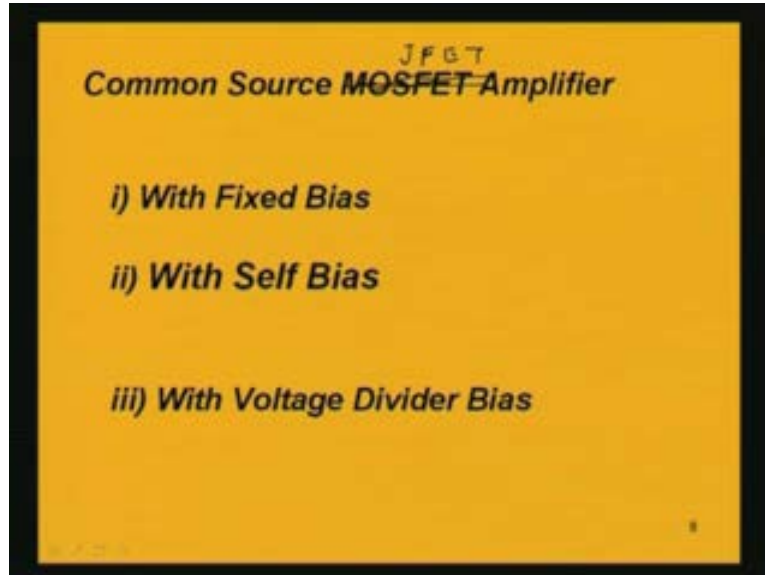
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A common source JFET amplifier will have a biasing scheme and using a particular biasing scheme we use the amplifier.

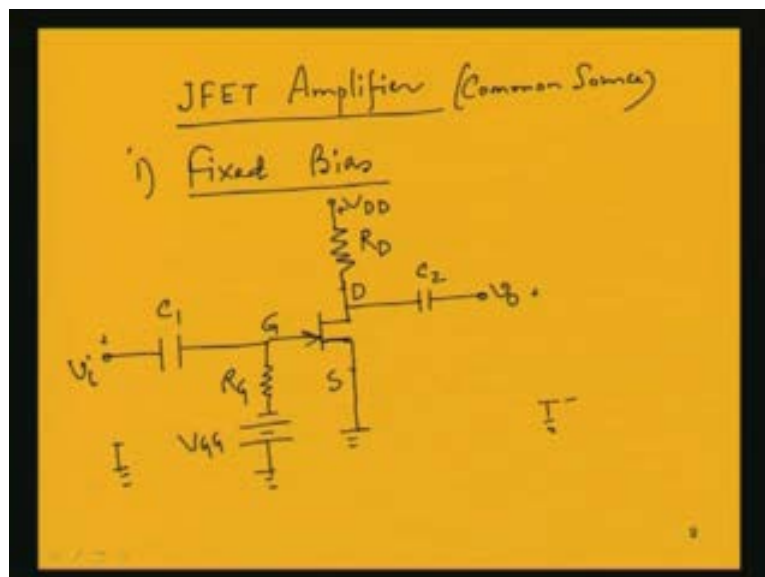


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The common source JFET amplifier has fixed bias, self bias and voltage divider biasing schemes. As we are familiar with this biasing schemes which we also had in BJT amplifier that makes the study easier. But let us recall those biasing schemes that we have once used for BJT amplifier again. Let us discuss JFET amplifier biasing schemes briefly. Instead of going again into deriving all those parameters let us revisit those biasing schemes and quickly have a look into the use of these biasing schemes in the amplifier. Let us first discuss the fixed bias scheme for this JFET amplifier.

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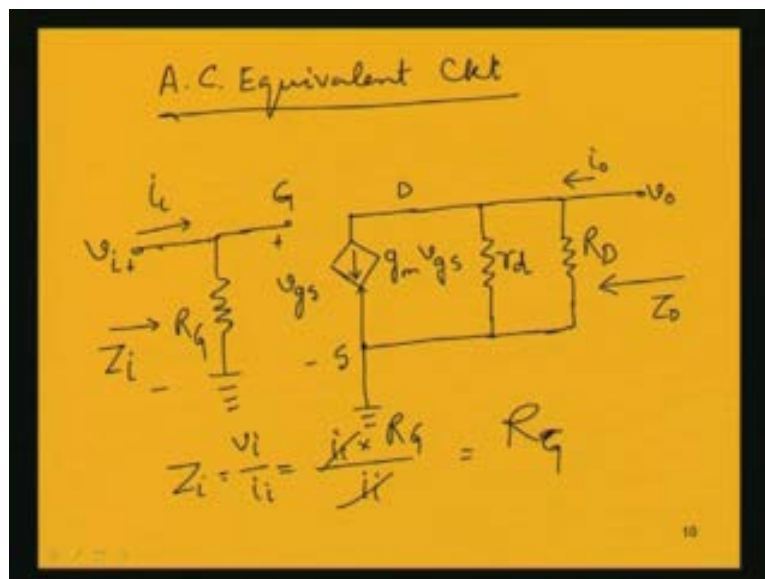


As the name suggests we have a fixed resistance and we are using common source JFET amplifier. Let us discuss common source JFET amplifier. The symbol for the JFET amplifier is like this. This is the gate, this is the drain and this is the source. For example we are taking an n-channel JFET. The direction of this arrow will convey the information whether it is n-channel or whether it is p-channel. Here it is an n-channel JFET device. We will have a biasing voltage and a resistance in the drain. This is say  $R_D$ , this is the drain terminal and this is the source terminal. This  $V_{DD}$  is positive. The source is grounded and in the gate we have a resistance  $R_G$  say to a negative voltage. Let us name it as  $V_{GG}$ . Basically this is the biasing scheme but we are considering an amplifier circuit. So we have to input a small signal and at the drain terminal we will get an output voltage which is also an AC signal. It will be in amplified form.

The input voltage is applied at a gate terminal through a coupling capacitor. The role of this capacitor is that it isolates the DC from the AC that is say  $C_1$  and here we have another coupling capacitor  $C_2$  and the drain terminal will have this output voltage say  $v_o$ . This is  $v_i$ . The polarities are shown as positive and negative lines. What will be the small signal model for this JFET device? That you can draw and then we can draw the AC equivalent circuit for the whole amplifier.

If we recall the procedure for drawing the AC equivalent circuit the first step is that which make the DC sources zero, short circuit them. Second step, the capacitance has these values which are quite large. They are like short circuit path for AC. So short circuit those capacitances and then the resistances etc, which are by passed by the short circuited paths you simply remove them and then simplify the circuit. Following this procedure if we want to draw the AC equivalent circuit for this amplifier what we will do is we will make  $V_{DD}$ ,  $V_{CC}$  zero. Then this capacitance will have a short circuit path. First let me draw the small signal model for the JFET.

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It will be  $g_m v_{gs}$  between drain and source. This is the source. There will be  $r_d$ . This is the gate terminal. Between gate and source the small signal is  $v_{gs}$  and the drain and gate terminal will have the resistances  $R_G$  and  $R_D$ . This is grounded and this is also grounded. We have the input voltage here. This is the short circuit path through the coupling capacitor. This is  $v_i$ . This is  $v_o$ . This is the AC equivalent circuit for this network using the fixed biased scheme; fixed resistance is there  $R_G$ . If we want to find out all those parameters like input impedance we will look into the circuit at the input terminals. This is  $Z_i$ ; this is your input current, this is the output current and the output resistance will be or impedance will be here looking into the device from the output terminals.

In order to find these out we follow the usual procedure. What will be the input impedance? This is nothing but  $v_i$  by  $i_i$ . The gate current is zero. The input current is nothing but this  $i_i$  which is flowing through  $R_G$ . What is this  $v_i$ ? The voltage here at the input terminal is the voltage across this resistance  $R_G$ ;  $i_i$  into  $R_G$  divided by  $i_i$ . The input impedance is  $R_G$ . For this fixed bias scheme, the input impedance is  $R_G$ . If we want to find out the output impedance, procedure is same. We have to make input voltage zero. If we make input voltage zero,  $v_{gs}$  is nothing but the  $v_i$ . So  $v_{gs}$  will also be zero. For finding out the output impedance, make  $v_i$  is equal to zero. Putting  $v_i$  is equal to zero means  $v_{gs}$  equal to  $v_i$ ; that is also equal to zero.

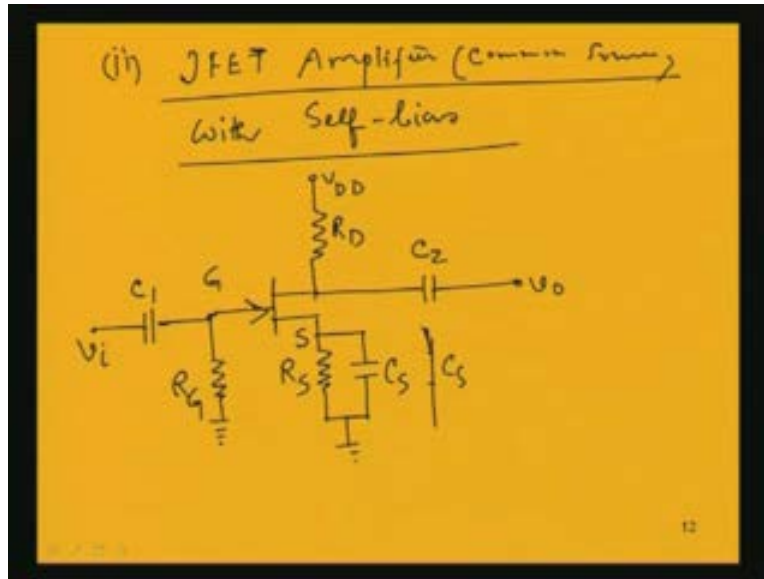
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The image shows handwritten mathematical derivations on a yellow background. The first part calculates the output impedance  $Z_o$  by setting the input voltage  $v_i = 0$ , which results in  $v_{gs} = 0$  and  $g_m v_{gs} = 0$ . The output impedance is then given by  $Z_o = \frac{v_o}{i_o} = r_d \parallel R_D$ . The second part calculates the voltage gain  $A_v = \frac{v_o}{v_i}$  using the relationship  $v_o = -g_m v_{gs} (r_d \parallel R_D)$ . Since  $v_{gs} = v_i$ , the gain simplifies to  $A_v = -g_m (r_d \parallel R_D)$ .

This current source  $g_m v_{gs}$  will be equal to zero. This is zero means what? This is like open circuit. From the output side we have only two resistances which are in parallel;  $v_o$  by  $i_o$ . If we find out  $v_o$  by  $i_o$  that is equal to  $Z_o$ . What is  $v_o$  by  $i_o$ ? That is nothing but the parallel resistance between these two  $R_D$  and  $r_d$ . That is equal to small  $r_d$  parallel capital  $R_D$ . That is obvious if you look from this circuit. This is just like open circuit and we have these two resistances in parallel. The voltage gain can be found out which is equal to  $v_o$  by  $v_i$ . Voltage gain is equal to  $v_o$  by  $v_i$ . Conventionally we are expressing the  $v_o$  as upper end is positive with respect to the lower end. But this current which flows through this  $r_d$

is nothing but  $i_o$  because one part of this current flows through here, through small  $r_d$  and other part is through capacitor  $R_D$  which is nothing but  $i_o$ . This is actually  $i_o$ . This one is  $i_o$ . If we want to express that current by current division  $g_m v_{gs}$  into  $r_d$  by  $R_D$  plus capacitor  $R_D$  and multiply it by capacitor  $R_D$  with a minus sign; because your voltage  $v_o$  conventionally its upper end is positive but this current flow is from bottom to top. So, it is negative. This  $v_o$  is equal to minus  $g_m$  into  $v_{gs}$  into small  $r_d$  by small  $r_d$  plus capacitor  $R_D$  into capacitor  $R_D$ . This is the voltage drop  $v_o$  divided by  $v_i$ . But  $v_i$  is equal to  $v_{gs}$ . This input voltage is same as gate to source voltage. These two cancel out and this two is nothing but small  $r_d$  parallel capacitor  $R_D$ . What is this voltage gain? Minus  $g_m$  into small  $r_d$  parallel capacitor  $R_D$ . These are the parameters which we can find out from this AC equivalent circuit; for the fixed bias scheme we have shown. Similarly there is a JFET self bias scheme, JFET amplifier and we are discussing common source with self bias.

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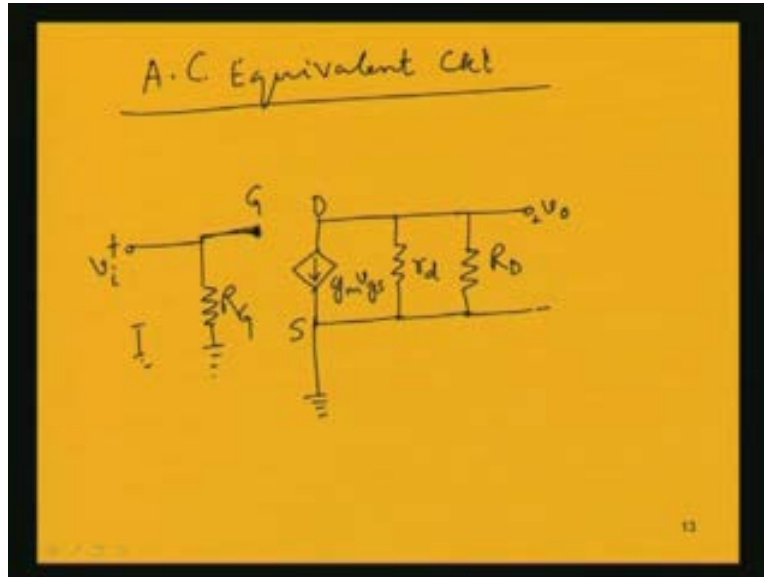


In BJT also we had self bias scheme and there the resistance was connected in the emitter and there was a bypass capacitor also. Even without bypass capacitor we may have a self bias scheme. Similarly here the resistance will be in the source. Analogous to that emitter in BJT we have the source here. Self biasing scheme will have the resistance connected in the source and we will have a bypass capacitor. In the circuit  $R_S$  is the self biasing resistor and this is the capacitance to the source resistance to the source. This is the source terminal and the rest is the  $V_{DD}$  having positive polarity through a resistance  $R_D$ . We are having this drain and the gate is having a resistance  $R_G$ . This is an n-channel and we have input voltage applied here.

In this scheme of self bias if we want to analyze drawing the equivalent circuit what we will do is we will follow the similar procedure and make the DC voltage zero, short circuit that capacitor. Next step after short circuiting the capacitor what happens is that this will be short circuiting path. This resistance  $C_S$  will have a short circuited path, so the resistance will be just bypassed. The current will take this path. This is the easiest path.

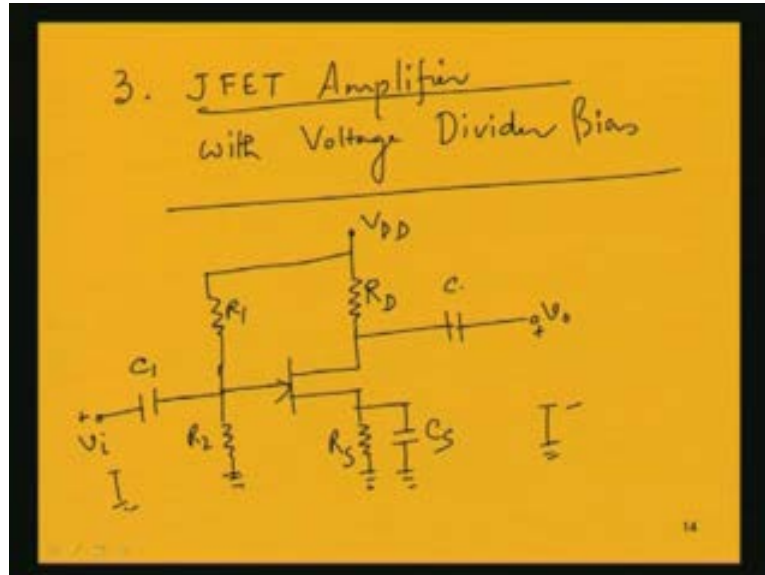
Because this is short circuited, the resistance will be avoided. This is simpler way. Because we do not have the resistance in the ammeter our circuit also becomes simpler. If we draw the AC equivalent circuit for this self biasing scheme, it will be like as shown here.

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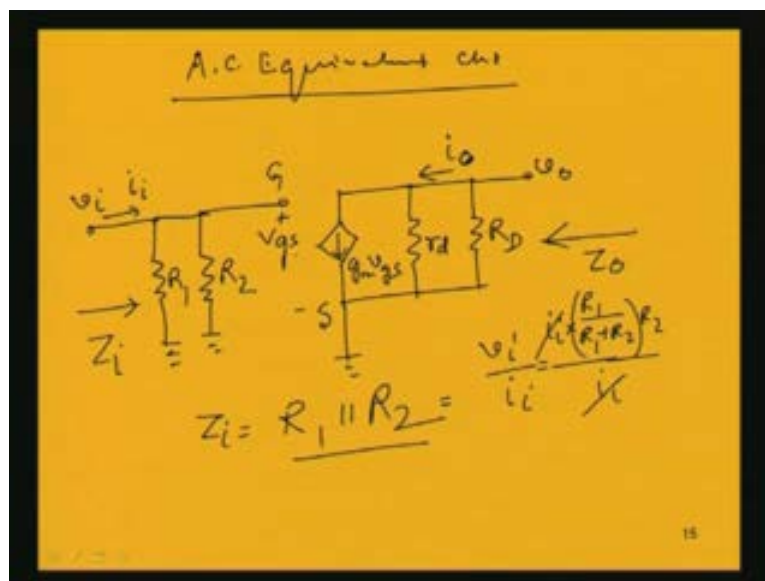
It will have the two resistances small  $r_d$  and capital  $R_D$  as it is and the source will have the path through the short circuited path by the capacitance which is short circuiting now. The resistance will be avoided. It will be simply grounded. It is a common source; source is grounded. It is a  $g_m v_{gs}$ . This is the gate terminal, this is the source terminal and in between gate and ground we have the  $R_G$ . We do not have a separate DC source here. Mind it in the gate we are not having the same source.  $V_{DD}$  is used for biasing and this is  $v_i$ . This is  $v_o$ , this is drain and this is the source. This is AC equivalent circuit for this self biasing scheme. Another popular biasing method is voltage divider biasing scheme. So let us consider JFET amplifier with voltage divider bias.

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We have a voltage divider biasing scheme given by two resistances. Here will be one resistance to gate which is say  $R_1$ . Another will be there which is say  $R_2$  and this is the source. Source is having the resistance  $R_S$  and the bypass capacitor is  $C_S$ . This is  $R_D$   $V_{DD}$  and this is the coupling capacitor. We get the output voltage with the drain terminal  $v_o$ . This is the voltage divider biasing scheme. Now if we want to draw its equivalent circuit following the usual procedure we will have two resistances  $R_1$  and  $R_2$  which are connected to gate and the ground; two parallel resistances will be there  $R_1$  and  $R_2$ . The AC equivalent circuit will have the small signal model as it is just the same.

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Right side is same small  $r_d$  parallel  $R_D$ ;  $g_m v_{gs}$ . This source is grounded. The gate terminal will have two parallel resistances  $R_1$  and  $R_2$  and this is the input voltage  $v_i$ . This is the gate to source voltage  $v_{gs}$  between gate to source. In this equivalent circuit we can find out the parameters like input impedance, output impedance, voltage gain, etc. In order to find out input impedance it is very simple because we have two resistances  $R_1$  and  $R_2$  parallel at the gate terminal. So it is simply  $R_1$  parallel  $R_2$ . You can derive it following the usual procedure like  $v_i$  by  $i_i$  where  $i_i$  is this current.  $i_{io}$  is this current and mind it we are not showing till now any source resistance and load resistance. If they are there then we will have to include them also in the circuit.  $v_i$  by  $i_i$  if we do, the voltage across  $R_2$  is the same voltage across  $R_1$  in whatever manner you take. By current division it will be  $i_i$  into  $R_1$  by  $R_1$  plus  $R_2$  into  $R_2$  by  $i_i$ . We get  $R_1$  parallel  $R_2$ .

Now the output impedance; make input voltage zero.

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Handwritten notes on a yellow background showing the derivation of output impedance  $Z_o$  and voltage gain  $A_v$  for a common-source amplifier.

Top line:  $Z_o$  Making  $v_i = 0 \Rightarrow v_{gs} = 0$

Circuit diagram: A box containing  $g_m v_{gs} = 0$  in parallel with  $r_d$  and  $R_D$ . An arrow points from the output terminal to the box, labeled  $Z_o$ .

Equations:

$$Z_o = r_d \parallel R_D$$

$$A_v = \frac{v_o}{v_i} = -g_m v_{gs} \left( \frac{r_d}{r_d + R_D} \right) R_D$$

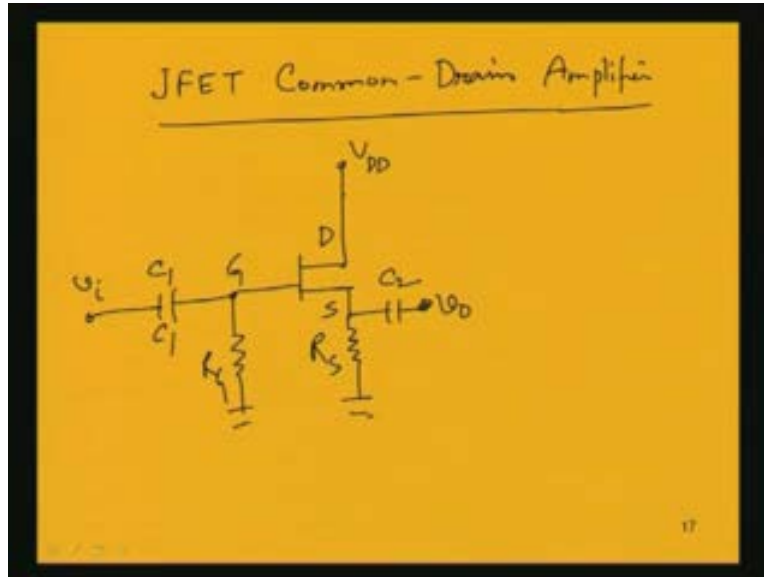
$$= \frac{-g_m v_i \left( \frac{r_d}{r_d + R_D} \right) R_D}{v_i}$$

$$= -g_m (r_d \parallel R_D)$$

Then the circuit will be like this. We have two resistances.  $g_m v_{gs}$  will be equal to zero; because  $v_i$  is equal to zero means  $v_{gs}$  is also equal to zero. We have only two resistances which are in parallel small  $r_d$  parallel  $R_D$  and if we look from the output terminal what we will get? It is small  $r_d$  parallel  $R_D$  only. This is the output impedance. Similarly voltage gain if we find out, the voltage gain is  $v_o$  by  $v_i$ . Find out  $v_o$ . This is positive and negative conventionally.  $i_o$  current which is this one, this is  $i_o$ , the current flowing through this capacitor  $R_D$  is equal to this current source multiplied by  $R_D$  by small  $r_d$  plus  $R_D$  because the current division law has to be applied. That current multiplied by this resistance gives you the voltage but in a negative way because current is flowing from bottom to top. Our voltage  $v_o$  is having top positive with respect to bottom. So minus sign will be there.  $g_m$  into  $v_{gs}$  into small  $r_d$  by small  $r_d$  plus  $R_D$  into  $R_D$  by  $v_i$ ;  $v_{gs}$  is equal to  $v_i$  and this two parallel combination small  $r_d$  parallel  $R_D$ . Finally we get the voltage gain as minus  $g_m$  into small  $r_d$  parallel  $R_D$ . The minus sign is significant because it conveys information of phase reversal. The output

voltage is 180 degree out of phase with the input voltage like in common emitter amplifier that we observed in BJT. Common source is analogous to common emitter amplifier characteristics and other types of configurations which we have are common drain and common gate.

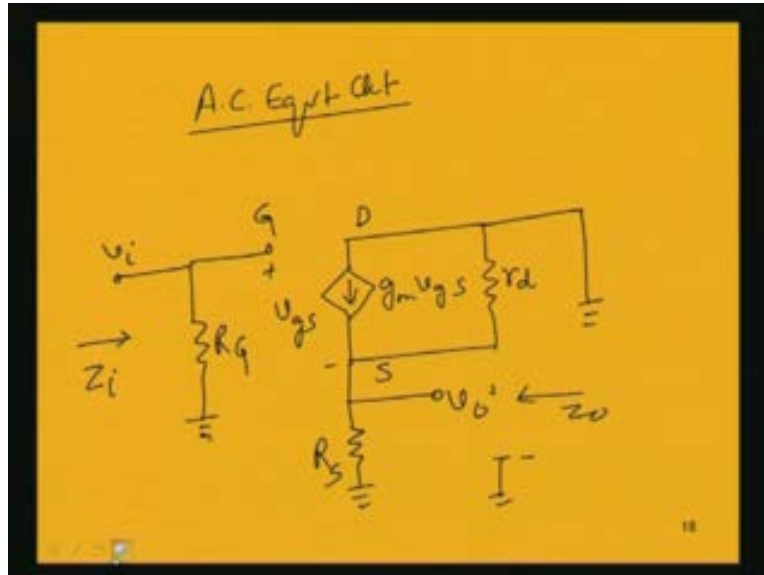
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Common drain amplifier is also known as source follower because the voltage you obtain across the resistance at the source. The common drain means drain terminal will be grounded in the AC equivalent circuit. That is why it is the common drain. In JFET common drain amplifier, if we see the circuit of the common drain, the drain will be directly connected to  $V_{DD}$ . But the source will have a resistance  $R_S$ . This is the source, this is the drain, this is the gate and gate is having a resistance  $R_G$  and this is the coupling capacitor. This is the input voltage. This is absent here because we get the voltage across the resistance at the source. This is  $v_o$ . In between there will be a coupling capacitor. This is like this. One important thing to notice here is that we have the voltage across this source resistance, not across the drain terminal that we had earlier in common source. This is the common n-channel. If we want to draw this AC equivalent circuit for this common drain amplifier, this is the current source between drain and source.  $g_m v_{gs}$ ,  $r_d$  will be there, small  $r_d$ .

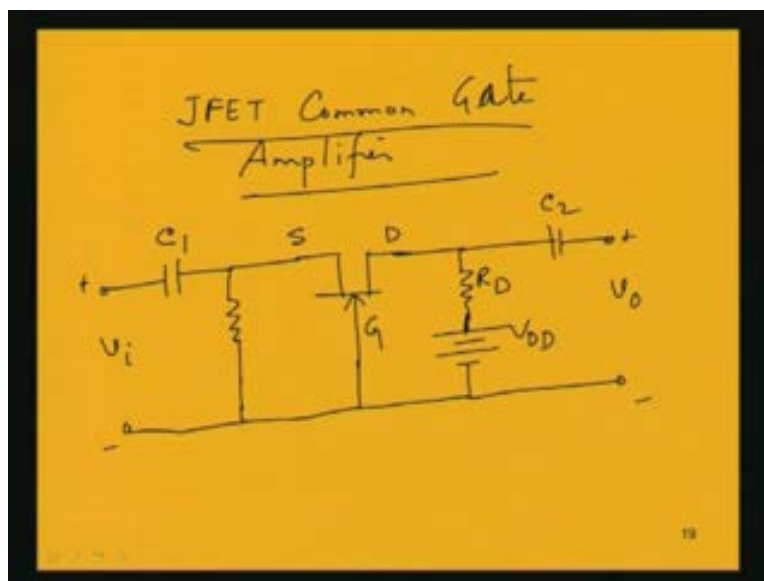


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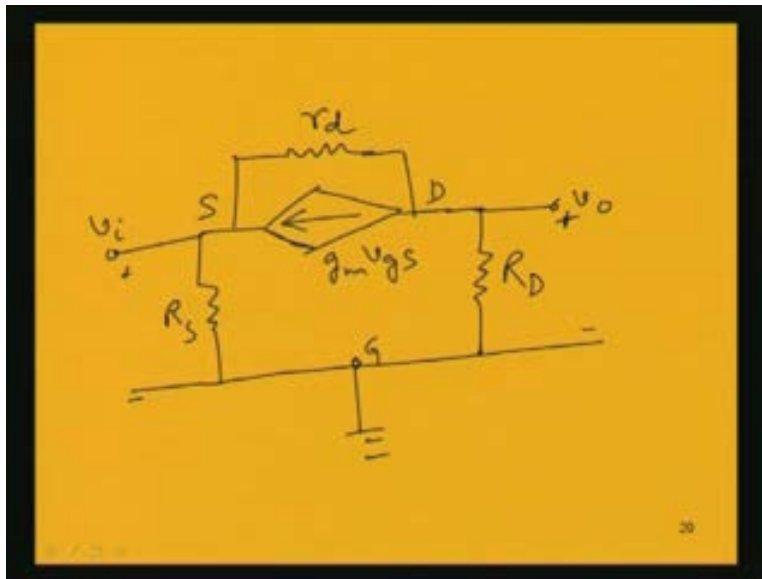
Capacitor  $R_D$  is not there. Drain is directly grounded. This is drain and this is source. This drain terminal is directly grounded; that is the important feature for this common drain amplifier and this is the gate terminal and source terminal is having the resistance  $R_S$ . We get the voltage across this resistance  $R_S$ ,  $v_o$ . The gate terminal is having a resistance  $R_G$  and this is the input voltage. This is the voltage between gate and source which is  $v_{gs}$ . This is the AC equivalent circuit for the common drain amplifier. In this AC equivalent circuit you can try this; find out the  $Z_i$ ,  $Z_o$ ,  $A_v$ , etc. Let us also take the JFET common gate amplifier configuration.

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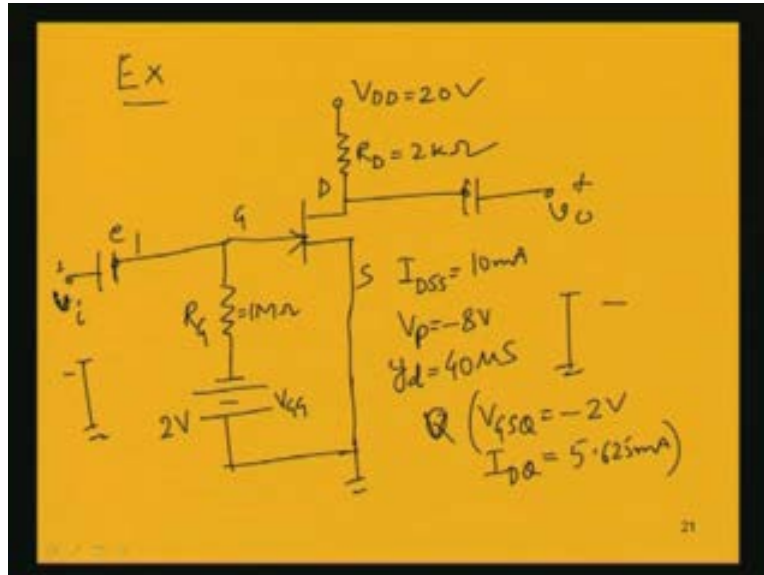
Common drain is similar to the emitter follower or common collector in the BJT and common gate is similar to common base amplifier in BJT. As the name suggests common gate means gate terminal will be grounded. This is gate, this is source and this is drain. We have the drain,  $R_D$  resistance and positive voltage  $V_{DD}$ . The gate is common between the two input and output circuits. A simple circuit is shown here. The voltage will be obtained here from the drain terminal. So this is common gate. If we now draw the AC equivalent circuit for this common gate amplifier we see that this is source, drain and gate. Gate is grounded so gate will be grounded.

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The current source is from drain to source which is  $g_m v_{gs}$  and the resistance  $r_{ds}$  will be from drain to source. Drain will have this  $R_D$  and source will have this  $R_S$  and the gate will be grounded like this and we have this  $v_i$ ; this is  $v_o$ . Here we can see that this  $R_D$ , the resistance will be between drain and source. For example if we take a fixed bias circuit as shown here we have  $V_{DD}$  is equal to say 20 volt,  $R_D$  equal to say 2 kilo ohm.

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This is drain terminal, gate terminal and source terminal. It is n-channel. We have  $R_G$  equal to 1 mega ohm. This is the gate to source  $V_{GG}$  voltage 2 volt and voltages through this coupling capacitor are obtained here. Input voltage is given through another coupling capacitor  $C_1$ . This is the  $v_i$ . This is the fixed bias scheme JFET amplifier. You are given that Q point is given as  $V_{GSQ}$  equal to -2 volt,  $I_{DQ}$ ; these are the Q point gate to source voltage current and drain current 5.625 milliampere and also given that the  $I_{DSS}$  equal to 10 milliampere. Then the pinch-off voltage is -8 volt and the drain to source admittance is 40 micro Siemens. These are given in the specification sheet and you are operating this JFET amplifier at this operating point. Now you have to find the transconductance,  $r_d$ ,  $Z_i$ ,  $Z_o$  and  $A_v$ .

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Find  $g_m$   
 $r_d$   
 $Z_i, Z_o, A_v$

Sol<sup>n</sup>

$$g_m = \frac{2I_{DSS}}{|V_p|} \left(1 - \frac{V_{GSQ}}{V_p}\right)$$

$$= \frac{2 \times 10\text{mA}}{8} \left(1 - \frac{(-2)}{(-8)}\right)$$

$$= \frac{2 \times 10\text{mA}}{8} \left(1 - \frac{2}{8}\right) = 1.875\text{mA/V}$$

How to solve this problem? We have to find out  $g_m$ .  $g_m$  we know is equal to  $2 I_{DSS}$  by magnitude of the pinch-off voltage into 1 minus  $V_{GSQ}$ , at the operating point gate to source voltage, by pinch-off voltage. By substituting these values  $I_{DSS}$  is given as 10 milliamperes; pinch-off voltage is given as -8 volt. We will take the magnitude of the pinch-off voltage which is 8 volt and within the bracketed term  $V_{GSQ}$  that is the gate to source voltage for the operating point is given as -2 volt and the pinch-off voltage is -8 volt. As it is, it will be replaced with their polarities. Now what we get? 2 into 10 milliamperes here both are in volt; 1 minus 2 by 8. If you calculate this it will come to, you check the value, 1.875 milliamperes per volt because this is milliamperes, this is volt and this has no unit. The unit volt to volt cancel; so it is equal to 1.875 milliamperes per volt.

What is small  $r_d$ ? It is the reciprocal of  $y_d$ .

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Handwritten calculations on a yellow background:

$$r_d = \frac{1}{y_d}$$

$$= \frac{1}{40 \mu S}$$

$$= 25 k\Omega$$

$$Z_i = R_G = 1 M\Omega$$

$$Z_o = r_d \parallel R_D = 25 \parallel 2 = 1.85 k\Omega$$

$$A_v = -g_m (r_d \parallel R_D) = -\frac{1.875 mS}{1.85 k\Omega}$$

$$= -3.47$$

$y_d$  we know. What is given? 40 micro Siemens. If we find out this value 1 by 40 is equal to 25 and unit will be kilo ohm because it is 10 to the power -6 and Siemens means ampere per volt. The reciprocal will give you volt per ampere and 10 to the power -6 will go up which will be 10 to the power 6, so 25 kilo ohm or 0.025 mega ohm, you will get. Similarly we can derive the input impedance from the small signal model or if we already know the input impedance because  $R_G$  we have found out. We can also proceed from the small signal model then you do not have to remember. You derive it from the small signal model by following the first principles. Then you will find that  $Z_i$  is equal to  $R_G$  and that is equal to 1 mega ohm and output impedance is small  $r_d$  parallel capital  $R_D$  means 25 parallel 2. Both are in kilo ohms. That gives you 1.85 kilo ohm and lastly voltage gain is minus  $g_m$  small  $r_d$  parallel capital  $R_D$ . Minus  $g_m$  we have found out to be 1.875 and that is micro Siemens into 1.85 kilo ohm. That gives you -3.47 with a minus sign. That is the voltage gain. In this way we can solve these examples. If we proceed by drawing the AC equivalent network incorporating the small signal model, we can derive all the

parameters easily by following the first principle. Suppose we are to get voltage gain  $v_o$  by  $v_i$ , then we will have to find what is  $v_o$ ? So in that way we can find out.

This discussion today helped us to know about the application of the junction field effect transistor which is a type of field effect transistor only and we have seen how the different biasing schemes can be used for designing the amplifier and three configurations we have discussed: the common source, common drain and common gate configurations just as in the case of BJT amplifier that we discussed earlier. Using the small signal model which is the same for the FET device that we have discussed so far be it MOSFET or be it JFET the small signal model is same. Only the transconductance computation will be a little different in JFET and by this small signal model incorporating the small signal model in the AC equivalent circuit for the amplifier we have found out all the parameters which are our interest in the amplifier.