

**Advanced NMR Techniques in Solution and Solid-State**  
**Prof. N. Suyaprakash**  
**Department of NMR Research Centre**  
**Indian Institute of Science – Bengaluru**

**Module-34**  
**T1 Relaxation Mechanisms and T2 Relaxation**  
**Lecture – 34**

Welcome all of you. Since the last class we have been discussing about relaxation; why last class, since the last two or three classes we discussed a lot about relaxation mechanisms, relaxation phenomena. I introduced T1 and introduced what is the concept of T1 especially spin lattice relaxation, how the spins lose energy with the lattice and what is the mechanism of relaxation, what are the fluctuating fields, what is the frequency of the fluctuating field.

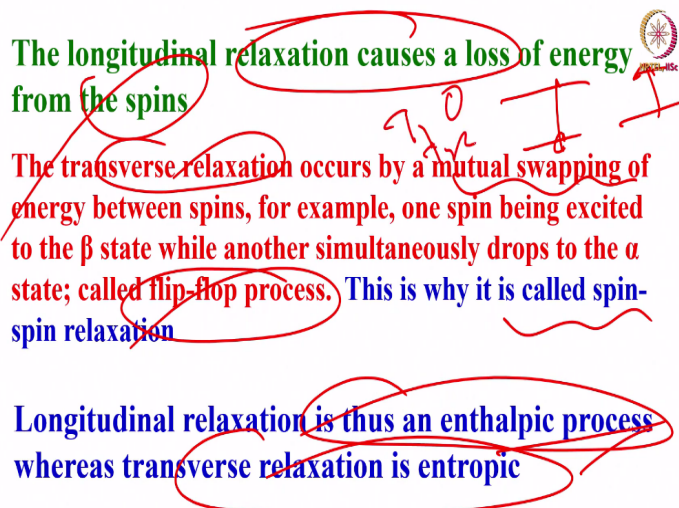
We discussed a lot about the spectral density function, correlation time  $\tau_c$ ; how they are related and also correlation time depends upon the size of the molecule, varieties of things we discussed and we understood lot about relaxation phenomenon, mechanism of relaxation like dipole-dipole interaction, chemical shift anisotropy interaction, quadrupolar relaxation, spin rotation relaxation, etc. These are the various mechanisms that aid relaxation, especially spin lattice relaxation which makes the spin to go back to thermal equilibrium. Then I introduced what is called as spin lattice relaxation; sorry spin-spin relaxation which is again nothing but dephasing of the magnetization vectors in the XY plane, bring the magnetization from Z axis to XY plane, instantaneously there is the phase coherence.

All the magnetic moment vectors are aligned in the particular axis. Bring the magnetization by applying 90 degree pulse from Z to X axis. All of them are along X axis all the nuclear magnetic moments spins, but because of the local fields fluctuating fields, the spins will start dephasing. They will lose coherence, phase coherence; slowly they will start losing phase coherence, go around in the XY plane.

And if we take the vector addition of all those things, as time passes by the intensity of these vector addition of the total magnetization keeps coming down, coming down. After a particular time when the spins completely fan out in the XY plane, there is complete decoherence and if we take the vector addition of all these magnetic moments you will not see any signal; it will be 0.

And this is the time which is required for the complete decoherence of the magnetic moment vectors in the XY plane, called spin-spin relaxation time. The time required for that is called spin-spin relaxation time; that is what I said. Now I also said for small molecules T1 is approximately equal to T2 and all those things.

(Refer Slide Time: 03:04)



The longitudinal relaxation causes a loss of energy from the spins

The transverse relaxation occurs by a mutual swapping of energy between spins, for example, one spin being excited to the  $\beta$  state while another simultaneously drops to the  $\alpha$  state; called flip-flop process. This is why it is called spin-spin relaxation

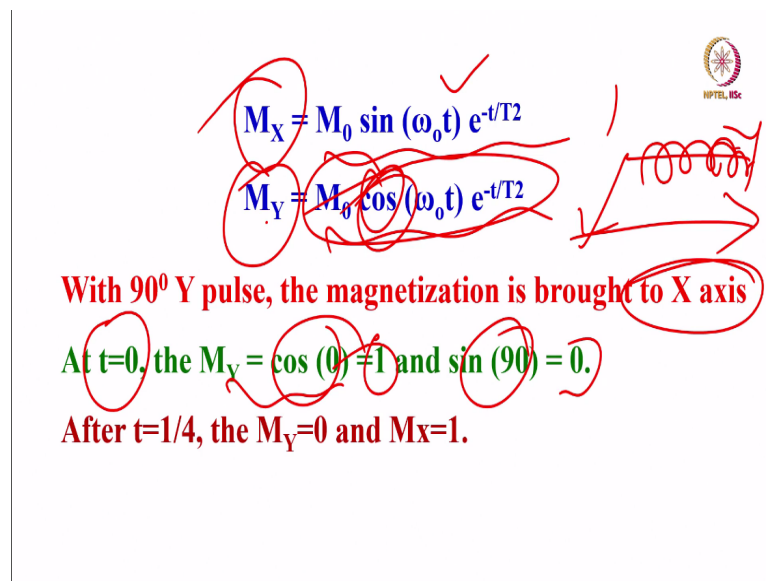
Longitudinal relaxation is thus an enthalpic process whereas transverse relaxation is entropic

Now we will continue further today. The longitudinal relaxation causes loss of energy from the spins to the lattice, the transverse relaxation occurs by a mutual swapping of the energy between the spins. For example, one spin in the excited state can come to beta state, while another drops to the alpha state. You see one spin, let us say, from alpha can come to beta from beta it can go to alpha.

See it can happen simultaneously mutual swapping of the energy between spins can take place. One spin being in the beta state can go to alpha state, alpha to beta state can happen. This is called flip-flop process. Flip and flop simultaneously spins from alpha can come to beta; then another spin because of this interaction can go from beta to alpha. And this is why it is called spin-spin relaxation.

One spin aid in other spin to undergo relaxation, this is called a flip-flop process and it is called spin-spin relaxation. Longitudinal relaxation is thus an enthalpic process; whereas transverse relaxation is a entropic process. Please remember this is entropic process longitudinal relaxation is an enthalpic process. And of course you know what is enthalpy everything, you would have understood, there is no point in going with the details of that. At least remember T1 is an enthalpic process and T2 is an entropic process.

(Refer Slide Time: 04:36)



The slide contains the following content with handwritten red annotations:

- Equations:  $M_X = M_0 \sin(\omega_0 t) e^{-t/T_2}$  and  $M_Y = M_0 \cos(\omega_0 t) e^{-t/T_2}$ . The  $M_Y$  equation is circled in red.
- Diagram: A 3D coordinate system with X, Y, and Z axes. A coil is drawn around the Z-axis, with an arrow indicating a pulse along the Y-axis.
- Text: "With 90° Y pulse, the magnetization is brought to X axis".
- Text: "At t=0, the  $M_Y = \cos(0) = 1$  and  $\sin(90) = 0$ ".
- Text: "After t=1/4, the  $M_Y=0$  and  $M_X=1$ ".

So, now you can work out the decay of the magnetization in the XY plane. We can have two components sine component cosine component; and  $M_x$  and  $M_y$  component I consider, and  $M_0$  into  $\sin$  of  $\omega_0 t$  into  $e$  to the power  $-t/T_2$  and  $M_y$  is a cosine of it. And of course depending upon where you are keeping the receiver. If my receiver is along X axis, then this will become cosine if the receiver is along Y axis this will become sine; does not matter so depends on the convention.

In this case receiver is along Y axis this is Y axis and this is X axis taken; so this is  $M_0 \cos \omega_0 t$  into  $e^{-t/T_2}$ . This is where  $M_y$  component this one is  $M_x$  component. So, with a 90 degree Y pulse the magnetization is brought to X axis at  $t = 0$ ;  $M_y = \cos$  of 0 at  $t = 0$ . So,  $\cos 0 = 1$  and  $\sin 90$  is 0. So, only one component is present  $M_y$  component is present immediately after  $t = 0$  that means my receiver is along Y axis you get maximum signal.

And there is no other component at all because  $\sin 90$  is 0; and after certain time what will happen other component starts developing; they will also start coming up. After time  $t = 1/4$  the  $M_y$  component = 0 and  $M_x$  becomes 1; we will work out from this equation by simply plugging in the values; it is a simple number, simple arithmetic you can do.

(Refer Slide Time: 06:09)

The  $e^{-t/T_2}$  represents the fanning out of each vector in the XY plane



$T_2 = 2\text{ms}$   
57.8 10ms

Time (t)	Amount of coherence left (%)
$t = T_2$	36.8
$t = 2T_2$	13.5 %
$t = 3T_2$	4.99 %
$t = 5T_2$	0.007 %

And you will see that  $e^{-t/T_2}$  represents the fanning out of each vector in the XY plane. So, it decays exponentially, that is what I said. The magnetization growth along Z axis is also exponential; the decay in the XY plane is also exponential. That is given by  $1 - e^{-t/T_1}$ , it is  $e^{-t/T_2}$ ; it is a decay. Now again put this value here let us see what happens, if we put  $t = T_2$  now 36.8%, but earlier it was 1 – something was there it was 63%.

Now it is,  $t = 2$  if you put it here, you will find out it is going to be 36.82; and  $t = 2 T_2$  is like 13.5%,  $t = 3$  times  $T_2$  is 4.99 after 5 times  $T_2$  it is 0.007. See the total magnetization if you take  $T_2$  is some value, let us say some 2 milliseconds; then 5 times  $T_2$  if you wait after 10 millisecond almost entire magnetic moment vectors would have completely undergone dephasing; there is no coherence at all. It is almost zero magnetization there in the XY plane. This is again just plugging in of the number I did that.

**(Refer Slide Time: 07:33)**

## Spin-Spin relaxation ( $T_2$ )



The transverse magnetization starts with a particular value (the  $x$  and  $y$  components are denoted  $M_x(0)$  and  $M_y(0)$ , respectively) and goes to zero with time  $T_2$ .

$$M_x = M_y = M_0 \exp(-t/T_2)$$

So, more about spin-spin relaxation  $T_2$ . Transverse magnetization starts with a particular value  $x$  and  $y$  components denoted as  $M_x = 0$ ;  $M_y = 0$  and goes to 0 with time  $T_2$  that is what it is. Initially when it come here full magnetization, let us say, this is  $M_y$  is maximum;  $M_x$  is 0. After sometime you will see that it starts changing I told you in the previous equation plug it in after  $1/4$  of tau value then this will become 0, this will become maximum.

And undergo rotation like this; and then it goes to 0 completely with a time  $T_2$ . So, in other word  $M_x$  and  $M_y$  can change based on this equation; it is given by  $M_x = M_y = M_0$  into exponential  $-t/T_2$ . This is an equation for measuring  $T_2$ ; earlier equation was for measuring  $T_1$ . Here you have to measure  $M_x$  component or  $M_y$  component, does not matter and this is given by this equation.

(Refer Slide Time: 08:37)

## $T_2$ Relaxation accompanying $T_1$ Relaxation



$T_1$  relaxation occurs when a spin exchanges energy with its external environment.

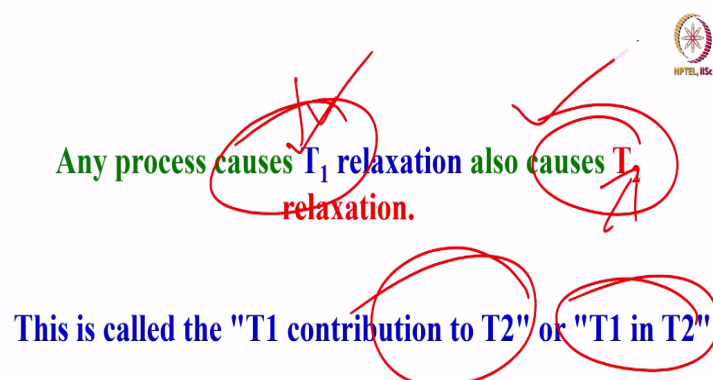
If such an energy exchange affects one of the spins contributing to  $M_{xy}$ , both the transverse and longitudinal components of its angular momentum would be randomly changed

It would immediately lose phase relations with other spins

So, T2 relaxation always accompanies T1 relaxation; that is point you must remember. T1 relaxation occurs when a spin exchanging energy with the environment, that is lattice it gives to the surroundings. When it exchange energy with the lattice, with the surroundings; T1 relaxation occurs and if such an energy affects one of the spins contributes to transverse magnetization  $M_x$  or  $M_y$ . Then both the transverse and longitudinal components; see angular momentum would be randomly changed, simple logic you understand. T1 is an exchange of energy with the environment. Let us say at that time if one such exchange mechanism affects the spins which is contributing  $M_x$  or  $M_y$ ; XY component let us say; in which case what happens the longitudinal relaxation mechanism also affects transverse relaxation mechanism.

Both can take place, because some component of the angular momentum gets changed randomly; because of this T2 relaxation accompanies T1 relaxation. As a consequence, it will immediately lose phase relation with other spins.

**(Refer Slide Time: 09:54)**



So, any process that causes T1 relaxation also causes T2; that is T1 relaxation and T2 relaxation processes go together. Any process which causes T1 mechanism also causes T2 relaxation. This is why it is called T1 contribution to T2; or T1 in T2; it is a word. Remember this is a definition T1 contribution to T2 or T1 in T2; means any process that causes T1 also causes T2 relaxation.

**(Refer Slide Time: 10:36)**

## $T_2$ Relaxation Occurring Without $T_1$ Relaxation



Most of the times the  $T_2$  relaxation accompanies  $T_1$  relaxation

Sometimes it may also occur without  $T_1$  relaxation

This is referred to as the "secular contribution to  $T_2$ ,"

Now you may ask me a question; any process which causes  $T_1$  causes  $T_2$  that is fine, can there be a  $T_2$  process without  $T_1$ ? Can there be a process? All  $T_1$  processes will affect  $T_2$ , I agree, but can there be  $T_2$  without  $T_1$ ? Of course most of the time  $T_2$  relaxation always accompanies  $T_1$ , but there are one or two examples. Sometimes it can happen; not always let us not go into the details of this because  $T_1$  relaxation phenomena is the biggest and toughest topic to understand in NMR; a lot more to understand, lot more to discuss.

We will not go into the details of that please understand sometimes  $T_2$  can also occur without  $T_1$  relaxation. Then this is called secular contribution to  $T_2$ . This is a statement I am giving you just to understand; always in all the book you read  $T_2$  accompanies  $T_1$ . There are examples  $T_2$  can also occur without  $T_1$ ; that is called secular contribution to  $T_2$ ; when  $T_2$  accompanies  $T_1$  it is called  $T_2$  in  $T_1$ .

**(Refer Slide Time: 11:46)**

## **T<sub>2</sub> Relaxation Occurring Without T<sub>1</sub> Relaxation**

**T<sub>2</sub> relaxation without T<sub>1</sub> relaxation can happen in a special form of dipolar interaction known informally as a spin-spin or called flip-flop**

**In this mechanism a pair of spins simultaneously exchange their longitudinal angular momentum components,  $\{\alpha\beta\}$  to state  $\{\beta\alpha\}$**

**This results in no net T<sub>1</sub> effect but loss of T<sub>2</sub> coherence**

So, now what is that T<sub>2</sub> relaxation occurring without T<sub>1</sub> relaxation. This can happen only because of one form of dipolar interaction, called flip-flop interaction. The flip-flop interaction is alpha beta spin go to beta alpha state; in which case alpha is going to beta and beta is going to alpha, because alpha is going to beta and vice versa, I said this as flip-flop process; one of the spin flipping process.

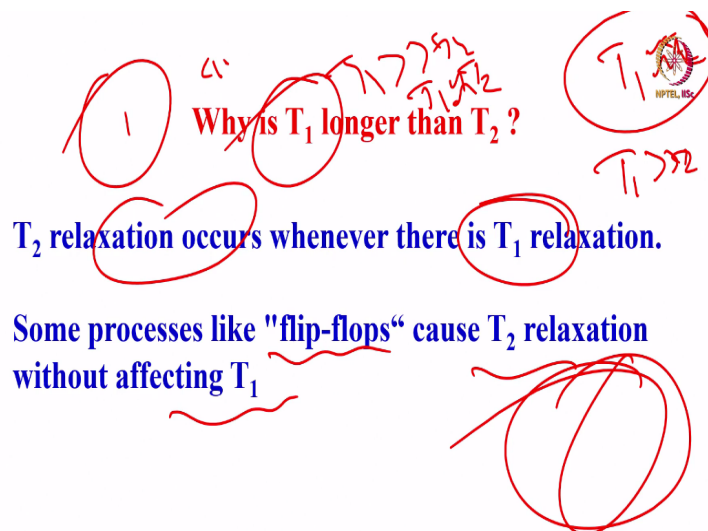
Here simultaneously one is going up other is coming down, alpha is going to beta, beta is coming to alpha. This is called flip-flop process. This is called spin-spin interaction, also dipole interaction called flip-flop interaction. This can happen only in such situations. If the pairs of spins simultaneously exchange the energy, the longitudinal angular momentum components like alpha beta to beta alpha states, there will be transition.

This results in no change in T<sub>1</sub>, but causes loss of T<sub>2</sub> coherence. It can happen remember several phenomena I explained today. T<sub>2</sub> always accompanies T<sub>1</sub>, T<sub>1</sub> any process which affects T<sub>1</sub> will also affect T<sub>2</sub> most of the time, but there can be T<sub>2</sub> without T<sub>1</sub>; it can happen one such example is dipole-dipole interaction; where alpha beta spin state changes to beta alpha spin state; it is called flip-flop processes, it can happen that can also cause.

So, T<sub>1</sub> process affecting T<sub>2</sub>, that is T<sub>1</sub> in T<sub>2</sub>; sometimes T<sub>2</sub> can also occur, without T<sub>1</sub>; that is called secular contribution to T<sub>1</sub>. So, the mechanism for that to occur is flip-flop process.

**(Refer Slide Time: 13:25)**





So, next thing is  $T_1$  is always equal to  $T_2$  in solution state, I told you approximately and  $T_1$  can never be shorter than  $T_2$ . This is always the case. You will never find situation where  $T_1$  is shorter than  $T_2$ , because spin lattice relaxation  $T_1$  is very much greater than  $T_2$  or approximately equal to  $T_2$  in solution state; that is what I said.

That means  $T_1$  relaxation occurs whenever there is  $T_2$  relaxation. Only some process like flip-flop cause  $T_2$  relaxation without affecting  $T_1$ . Why  $T_1$  is longer than  $T_2$ ? It is a simple logic; unless the magnetization of the XY plane completely undergo decoherence there is no growth along Z axis. XY magnetization unless it decays how can it grow along Z axis? so it has to decay first.

So, for  $T_2$  first magnetization has to completely undergoes decoherence, that is why  $T_1$  is always longer than  $T_2$ . Very rarely you will find situation  $T_1$  is equal to  $T_2$ , but it can happen most of the time in solution, but by and large you can always remember  $T_1$  is always larger than  $T_2$  in solution state. Next we will go further.

**(Refer Slide Time: 14:56)**

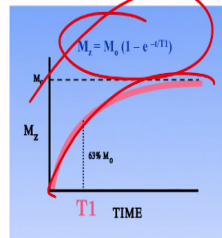
## Growth and Decay functions: Graphical illustration



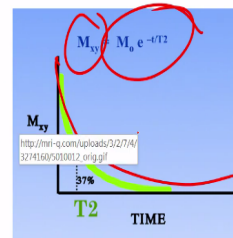
$T_1$  is the growth of the magnetization along Z axis

$T_2$  is the decay of the magnetization in the XY plane

Signal (measure of  $M_z$ )



Signal (measure of  $M_x, M_y$ )



And this is a graphical representation of the growth and decay functions.  $T_1$  is the growth of magnetization and exponential it is growing;  $T_2$  is the decay of magnetization in the XY plane this is  $M_{xy}$  which decays like this;  $M_z$  grows like this, with this term. Diagrammatically both can be shown one is exponentially increasing function other is exponentially decreasing function. Exponentially decreasing function is this one.

(Refer Slide Time: 15:24)

## Relaxation Rates vs Times : What is the difference?



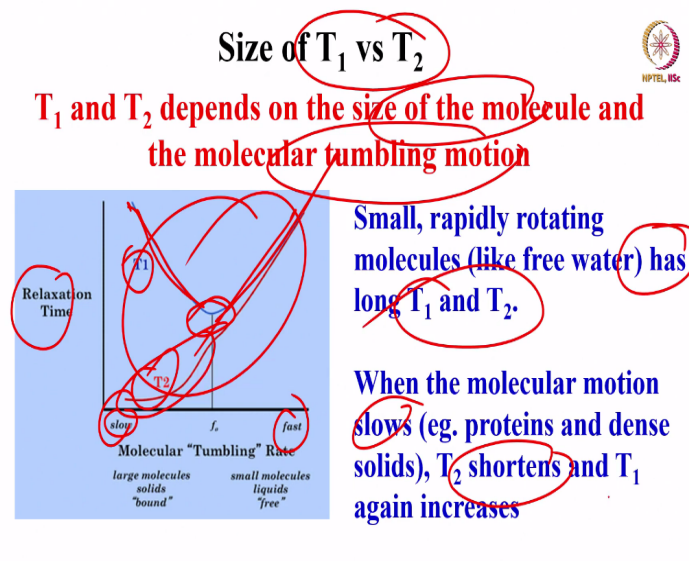
Relaxation times and relaxation rates  
are inverses of each other

$$R_1 = 1/T_1 \quad \text{and} \quad R_2 = 1/T_2$$

So, relaxation rates versus time if we consider sometimes in some books they use relaxation rates and relaxation times. What is the difference between relaxation time and relaxation rate? Relaxation time is what you are going to measure by doing an experiment  $T_1$  and  $T_2$  you can measure by doing certain experiments. I will show you how to measure it now, in this class if there is time, I will show you what an experiment we do to measure  $T_1$  and  $T_2$ . And these are called  $T_1$  and  $T_2$  is called relaxation times.

If I say  $T_1$  is 10 millisecond, it the time of 10 millisecond for the spins to lose energy with lattice that is 1. What is the relaxation rate, rate is inverse of this relaxation time, see this is denoted by terms called  $R_1$  and  $R_2$ .  $R_1$  is relaxation rate which is inverse of  $T_1$  and  $R_2$  is relaxation rate is inverse of  $T_2$ . In some of the biology studies you can see people mentioning in the paper or in books  $R_1$  and  $R_2$ .  $R_1$  and  $R_2$  are nothing but inverse of  $T_1$  and  $T_2$ , you please remember this.

(Refer Slide Time: 16:37)



So, now size of the  $T_1$  and  $T_2$  of course I told you what is  $T_1$ , what is the size of  $T_1$ . Approximate value of  $T_1$  in solution state it varies from microseconds to seconds, minutes, hours. And of course this is just a general statement. It is not always true it can vary, it varies from molecule-to-molecule, spin-to-spin, depending upon size of the molecules. And of course and in the magnetic field you are doing experiment etcetera. So, we should have the idea about size of the  $T_1$  and  $T_2$ .  $T_1$  and  $T_2$  depends upon not only on the size of molecule, but also on the molecular tumbling motion; two factors, it depends upon size of the molecule and on the molecule tumbling motion, both. So, you can see here this is what we saw earlier in the relaxation time if you measure this is  $T_1$  and this is  $T_2$ ; as the molecules undergoes slow motion here.  $T_1$  is longer as the motion rate becomes faster and faster, it decreases in intermediate regime  $T_1$  is very small. Again when the molecular undergoes fast motion it goes up. Similarly  $T_2$  it is like this, slow motion  $T_2$  is longer as the molecular motion becomes faster and faster  $T_2$  becomes smaller and smaller; this is what it is. So, this is slow motion and this is the fast motion and this is how  $T_2$  will change this is how  $T_1$  will change.

So, when the molecular motion slows T1 shortens, and T1 again increases again. For small rapidly rotating molecule like free water T1 and T2 are very long. So, these are the important things you should know that.

(Refer Slide Time: 18:25)

In reality the signal decays faster than the normal  $T_2$ .  
 This rate is denoted  $T_2^*$ .  $T_2^*$  is called "effective"  
 $T_2$ .  $T_2$  is considered the natural  $T_2$  T\* < T2

$T_2^*$  is always less than or equal to  $T_2$

$T_2^*$  results principally from inhomogeneities in the main magnetic field or from the sample placed in the field

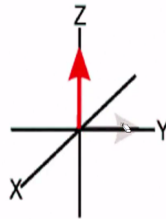
$$\frac{1}{T_2^*} = \frac{1}{T_2} + \frac{1}{T_2'}$$

In reality, the signal decays faster than the normal  $T_2$ . See we say signal decay in the XY plane; that is a  $T_2$ . Does it comes only because of this spin-spin relaxation mechanism or two spins exchanging the energy? is that is the reason why it is decaying. There can be various other factors which contribute for this. For example there could be magnetic inhomogeneity. Magnetic field inhomogeneity that can contribute for the spins that can also give fluctuating fields at the site of the nucleus, that can cause dephasing.

In reality, the signal will decay faster than the normal  $T_2$  because of various other parameters. So, the actual  $T_2$  what you measure is not the real  $T_2$ . So, that is why this is called effective  $T_2$  called as  $T_2^*$ ; it is called effective  $T_2$ . So, this  $T_2$  is a normal  $T_2$ ; then how do you get the normal  $T_2$ ? when you know  $T_2^*$ .  $T_2^*$  is always less than  $T_2$  because it decays faster because of external phenomenon. If there is less external phenomenon there is no disturbance from the other magnetic field inhomogeneity etcetera then what will happen at the most  $T_2^*$  can be equal to  $T_2$ ; it can happen. Otherwise generally  $T_2^*$  is always smaller so then how do you find it what is  $T_2^*$ ? It comes from various inhomogeneity of the magnetic fields when place this sample in magnetic field, so generally  $T_2^*$  is obtained by equation called  $\frac{1}{T_2^*} = \frac{1}{T_2} + \frac{1}{T_2'}$ . These are all the contributions from various things what it mentions is the  $T_2^*$  and the actual  $T_2$  this is inhomogeneity contributions.

$T_2^i$  means contribution coming because of other inhomogeneities of the magnetic field. So, real  $T_2$  if I want to calculate you should know  $T_2^*$  and you should know this thing; or we should at least eliminate these terms to get real  $T_2$ .

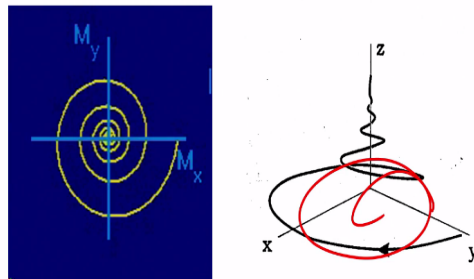
**(Refer Slide Time: 20:35)**



So, this is a diagrammatically what happens for the nuclear spins. You bring the magnetization to XY plane; see what is happening as it comes down it is dephasing in the XY plane. It is coming down in intensity simultaneously it is going up you see what is happening to the magnetization. You have brought to XY plane and then at any given extent of time immediately as soon as you bring it the magnetization is maximum and at any given time keep on decaying in the XY plane and goes along this. So unless it decays completely it cannot go along Z axis that is why I said  $T_1$  is always longer than  $T_2$ . So, this is a phenomenon simultaneously happening; look at it while decaying it is also growing simultaneously.

**(Refer Slide Time: 21:22)**

## Visualisation of the process of $T_1$ and $T_2$



### $T_1$ and $T_2$ occur simultaneously

These are simultaneous phenomenon. If you visualize a process of  $T_1$  and  $T_2$  actually this is how it sees, we should visualize the process it appears when it is decaying like this simultaneously it is going up and up; it is like a spiral. If you visualize this thing from the top here it is decaying in the XY plane simultaneously it is going up. It is like you have an umbrella closed and invertedly.

Let us say I open the umbrella first take an umbrella completely open it, spread it along XY plane. Now that means the magnetization has been brought to the X axis and now slowly I am closing the umbrella it will starts growing along Z axis; the vertical component in the umbrella starts going up. Initially it will be spread here and slowly start closing up.

Open and close it is like fanning out the nuclear spins when umbrella is open is when umbrella is completely closed then what will happen magnetization is growing along Z axis. Exactly the phenomenon, when it goes like this it keeps reducing like this, like this, like this, like this and then get closed. This is as if spiral is going with intensity coming down in the XY plane simultaneously growing in Z axis. This is how both the phenomena are simultaneously happening and that is how we have to visualize  $T_1$  and  $T_2$ .

**(Refer Slide Time: 22:57)**

In brief, the relaxation is a radiationless transition



Longitudinal or spin-lattice relaxation ( $T_1$ )

- Recovery of longitudinal magnetization
- Establishment of thermal equilibrium populations
- Exchange of energy between spins and lattice

In brief we have discussed a lot about relaxation concepts, relaxation phenomena etcetera. Now let us take some summary of these things and then go for measurement of  $T_1$  and  $T_2$ . In brief, remember relaxation is a radiationless transition; it will not give rise to signal detection. It will only aid the spins to relax; to decay in the XY plane and grow along the Z axis.

We saw it corresponds to energy state of the spins and the lattice, spin in the upper state the come down, then the spins in the lattice lower states will go up, spin in upper state will come down, lattice will go up; all these exchange phenomenon is going on, but then remember it is not giving rise to magnetization for detection. It is a radiationless transition, so relaxation is a radiationless transition. Now what you call longitudinal spin-spin relaxation it is called  $T_1$  it is nothing, but the recovery of the magnetization, or establishment of thermal equilibrium of populations and it is a exchange of the energy between the spins and the lattice and the various phenomenon for this thing we discussed.

(Refer Slide Time: 24:12)

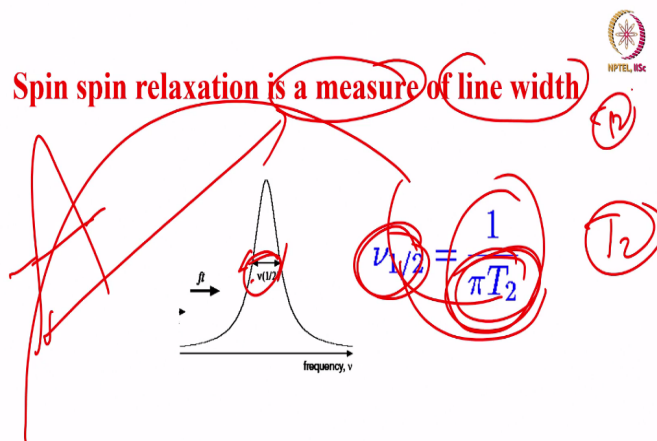


## Transverse or spin-spin relaxation ( $T_2$ )

- Decay of transverse magnetization ✓
- No exchange of energy ✓

Again transverse relaxation  $T_2$ . It is a decay of transverse magnetization in the XY plane and here there is no exchange of energy of the spins with the lattice. It can only happen when one spin exchanges energy with the other spin.

(Refer Slide Time: 24:32)



And then if I look at the NMR spectrum very clearly, looking at the width of this peak, I can get a rough estimate of the spin-spin relaxation. The spin-spin relaxation is nothing, but the measure of the line width. See this is the line width of a spectrum, I know what is the line width  $\nu_{1/2}$ . If I know the width of the full width and half height;  $\nu_{1/2}$ , this is equal to  $1$  over  $\pi$  times  $T_2$ .

So, if I take a spectrum measure the line width here, and take  $1$  over  $\pi$  times the line width then you are going to get  $T_2$  approximately. So, the rough guess is you can measure the spin



lattice relaxation time by knowing the line width, very easy, very straightforward we are measuring  $T_2$ , but of course it is the approximate value. If you want to measure accurately you have to remove field inhomogeneity contribution, etcetera there is a complicated experiment one can do. We will come to that later. But this you should remember, in case if you are going to get a very broad signal, obviously it means that  $T_2$  is very small, very broad this will bring it down, this will go up;  $T_2$  will be very short. Spins are relaxing very fast dephasing very fast in the XY plane. As a consequence, you are going to get a very, very broad signal.  $T_2$  is very short means broad signal. This is the important thing you should know.

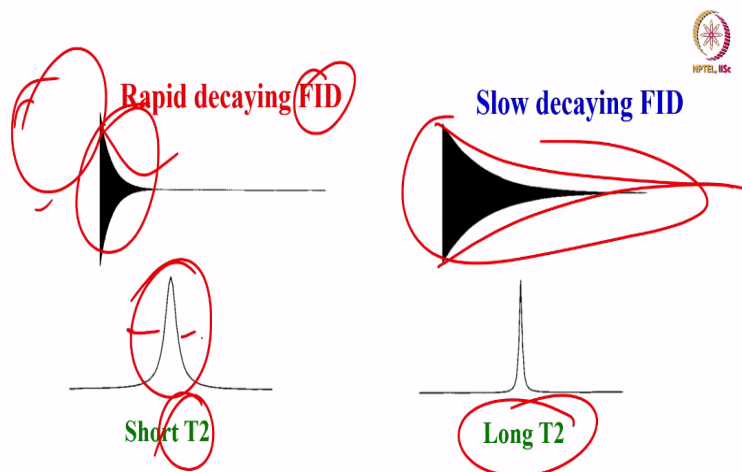
**(Refer Slide Time: 26:03)**



### **Measurement of Relaxation Times ( $T_1$ and $T_2$ )**

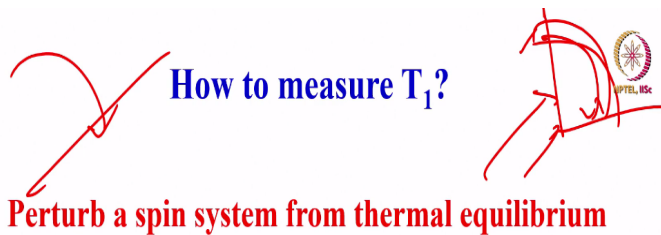
Now we will go into the measurement of the relaxation times  $T_1$  and  $T_2$ . How do you measure these two relaxation times? So far conceptually we understood, approximately we measured what is  $T_2$  by looking at the line width; fine, but we have to precisely measure  $T_1$  and  $T_2$ , get accurate values; how do we do that?

**(Refer Slide Time: 26:25)**



So, before that; I told you  $T_2$  is a measure of line width. Now the line width is what it is because of the free induction decay, time domain signal. In the Fourier transformation we understood time and frequency are inversely related to each other; they are related by Fourier transformation. If the signal is decaying very slowly in the time domain, the peak in the frequency domain is very, very sharp. If the signals decays very fast in the time domain, it will be very broad in the frequency domain. This is in the Fourier transformation, when we introduced the theory we understood lot about the Fourier transformation, you please remember, we discuss these points. So, now look at the signal like this; I have two FIDs this is the rapidly decay FID; and you get the short  $T_2$ , that shows it is decaying very fast; and spins in the XY plane has dephased very fast; that is called short  $T_2$ . Short  $T_2$  means the spins have dephased very fast in the XY plane. Look at this FID this is a long decaying FID, slow decaying; it takes more time to decay means long  $T_2$ . So, longer the time the spins takes to undergo decoherence in the XY plane, the sharper the lines you are going to get. This thing you should remember. So, that is why looking at the free induction decay you should understand what is the line width. This way I said line width is approximate measure of  $T_2$ .

**(Refer Slide Time: 28:03)**

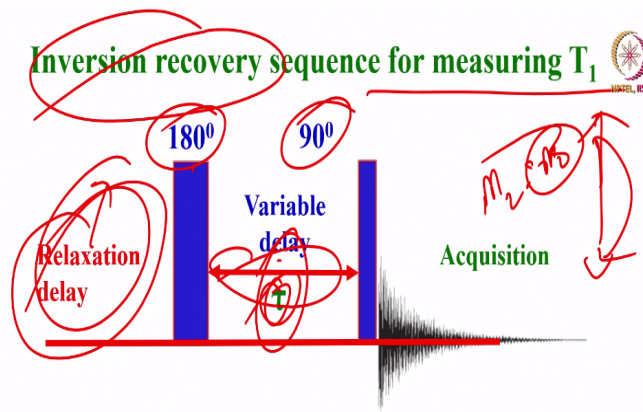


**Design an experiment to measure its recovery as a function of time**

So, now how to measure the  $T_1$ ? First of all, simple mechanism put the sample in this magnetic field, wait for some time to see the signal. Then as soon as you put the sample keep on pulsing rapidly very, very rapidly till you see the maximum signal. It is practically very difficult I cannot do the pulsing so fast and we do not know when you will reach the maximum signal how much time it takes like that. Other way out is to disturb the spin in the thermal equilibrium apply radio frequency pulse bring the magnetization from Z axis to X axis. You have perturbed it and then design an experiment to see how much time it takes to go back; that is the simple experiment. Disturb the spin system, bring the magnetization in the X axis or Y axis, now it has to go back. Design the experiment to measure the time it takes to go back to Z axis to achieve thermal equilibrium.

It has to recover as a function of time; measure this time, measure the time it requires to go back to Z axis, then you will understand, you can measure what is  $T_1$ .

**(Refer Slide Time: 29:23)**



**Signal intensity is measured as a function of the delay between pulses and used to obtain the value of  $T_1$**

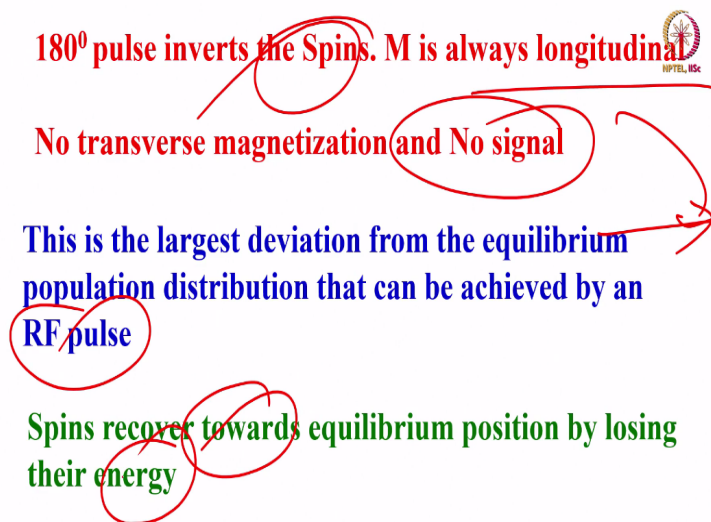
All I do is a simple experiment like this. There are four, five different experiments to measure, viz., progressive saturation, saturation inversion, null method or inversion recovering method, varieties of experiments are there. I am not going to give details of all the different experiments and you can choose experiment depending upon the  $T_1$  whether your sample has a longer  $T_1$  or a shorter  $T_1$  etcetera.

But basically commonly used experiment is the inversion recovery experiment for measuring  $T_1$ ; especially in solution state, which are for short  $T_1$ ; not when the  $T_1$  is of the order of days and hours; you cannot do that. There is a different method for that, but in most of the times solution state  $T_1$  and  $T_2$  are of the order of few milliseconds or seconds you can use an experiment called inversion recovery sequence and measure the  $T_1$ .

So, it is a very simple two pulse sequence; first pulse is a 180 pulse and second is a 90 pulse. Initially before application of 180 pulse all the spins are in thermal equilibrium, give enormous time, give a delay, make sure that spins attain the thermal equilibrium. And then apply 180 pulse; What does 180 pulse do? Bring the magnetization from Z axis to  $-Z$  axis, it will be tilted by 180 degree. Then give some delay and then apply 90 degree pulse, and start acquiring the signal. Now, what you do is; do not do one experiment; keep on varying the delay, N number of experiments we have to do. Every time vary the tau delay and measure the intensity of the signal, and then use these different intensities obtained for different tau values; and then fit to a function; there is a function which I told you  $M_z = M_0 (1 - e^{-t/T_1})$  fitting into that equation you will get the  $T_1$  values.

It is a very simple thing because you know tau you know  $M_z$  and you should get what is the equilibrium magnetization. Equilibrium magnetization is something a system has attained thermal equilibrium and full magnetization is available and then keep on varying the delay and see that intensity; initially it will be  $-Z$  starts growing slowly and after certain time it will again come back to  $M_0$ ;  $-M_z$  it will become  $+M_z$ ; which is nothing, but equilibrium magnetization  $M_0$ ; then at different values of the intensity of the peaks is fitted into this equation, you can measure the  $T_1$  accurately.

(Refer Slide Time: 32:16)



So 180 pulse invert the spins;  $M$  is always longitudinal, and no signal initially. It is the largest deviation of the equilibrium can be achieved by the first rf pulse. Bring the magnetization to this thing largest deviation you get signal. The spins recover towards equilibrium position by losing their energy, start going back.

(Refer Slide Time: 32:38)

## Magnetization after an 180° Pulse



$$\beta \frac{N/2 - \delta}{\alpha \frac{N/2 + \delta}}$$

Before 180° pulse

And then this is what I have to discuss something more about what happened to magnetization after spin dropping, I have to discuss. I will come to that later, but remember one thing one experiment, we can design where you have to disturb the spin system by applying a 180 pulse. Bring the magnetization to X axis or Y axis whatever it is depending on where you have receiver.

And then first 180 pulse brings the magnetization to – Z axis; give a delay between 180 and some delay apply 90 pulse and start collecting the signal. Measure the intensity of the signal as a function of tau value and number of experiments if you do, you fit it into the equation which is  $M_z = M_0 (1 - e^{-t/T_1})$ ; then you can measure the accurate value of T1.

So, what is happening when you apply 180 pulse, we have to understand by what is called a term called spin dropping. I will come to that, I will discuss that in the next class. So, I will stop today, but today anyway we have understood lot about spin-spin relaxation also. I have told about what is a spin-spin relaxation, mechanism of spin-spin relaxation and in summary we discussed and said the relaxation is a radiationless transition.

In the case of spin lattice there is exchange of energy between the spins of lattice and it attains thermal equilibrium. In the case of spin-spin relaxation it is only between the spins there is no exchange of energy; spin lose coherence because one spins interacts with other spins, because of flip-flop process one spin can disturb the other spin, everything happened both spin relaxation T1 and T2 happens because of fluctuations in the local field.

And  $T_1$  is a growth along Z axis  $T_2$  is a decay along XY plane both are exponential and then we understood how measure the  $T_1$ . Simply you have to measure  $T_1$  by inverting this magnetization from Z axis to  $-Z$  and see how it goes as a function of time. For that a simple experiment can be designed it is called inversion recovery experiment; 180 pulse tau 90 pulse experiment you have to do and measure the intensity of the signal as a function of tau delay. And fit it into the growth function  $M_z = M_0 (1 - e^{-t/T_1})$ ; that is what we do to get the  $T_1$  and how do we do the experiment what happens 180 pulse and how we measure  $T_2$ , quickly we will finish this in the next class and with that I can go to another topic later. Many other things we will discuss. So, I am going to stop with this thing. I will see you in the next class. Thank you.