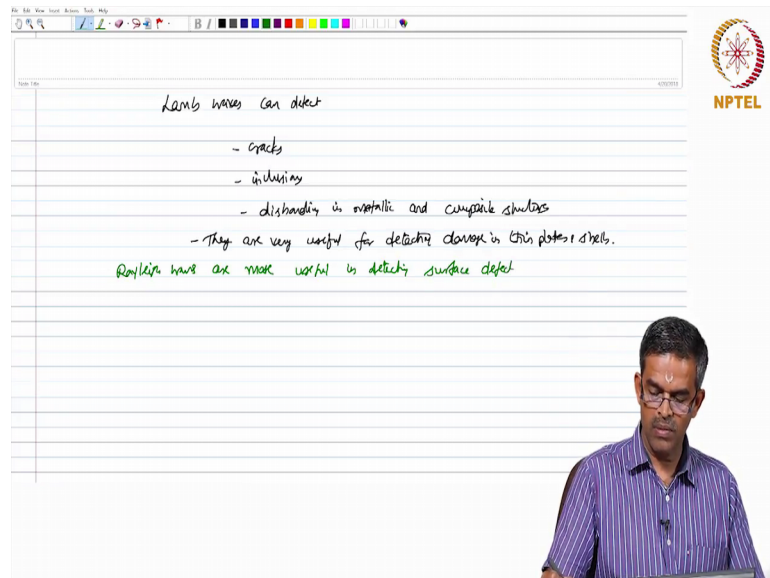


Structural Health Monitoring (SHM)
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Lecture - 40
Part - 2: Non-Destructive evaluation - I

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Lamb waves can detect

- cracks
- inclusions
- disbonding in metallic and composite structures
- They are very useful for detecting damage in thin plates and shells.

Rayleigh waves are more useful in detecting surface defect

Lamb waves can detect cracks inclusions, disbonding in metallic and composite structures; they are very useful for detecting damage in thin plates and shells. However, Rayleigh waves are more useful in detecting surface difference.

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Embedded NDE

sensor network, used for monitoring can be completely embedded (permanently fixed) into the structure. These sensors can be used for monitoring.

passive SHM
uses passive sensors that are monitored over a period of time
- monitored data will be useful in updating the system characteristics

Example of passive SHM

- 1) load
- 2) stress
- 3) Environmental conditions

4) acoustic emission from cracks
etc

Let us now pay attention to something called embedded non destructive evaluation.

Interestingly friends, sensor network used for monitoring, can be completely embedded that is permanently fixed into the structure, then these sensors can be used for monitoring. There are two ways by which this can be done: one is the passive SHM which uses the passive sensors that are monitored over a period of time. The monitored data will be useful in updating the system characteristics. Now, example of passive dampers, load sensors, sensors to measure stress sensors to measure environment conditions, acoustic emission from cracks etcetera.

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Passive SHM only listens to the structure
It doesn't interact with the structure

Active SHM detects presence of damage and
also estimates its extent and severity

One of the Active SHM is piezoelectric wafer active sensor (PWAS)

- These sensors send signal (Lamb waves) and also receive Lamb waves
to identify presence of damage in the structure
(cracks, delamination, debonding, corrosion, etc)

Interestingly, passive SHM only listens to the structure. It does not interact with the structure. Active SHM detects presence of damage and also estimates its extent and severity. One of the active SHM piezoelectric wafer active sensor, which we call as pediatric wafer active sensors, these sensors send signal which are essentially lamb waves and also receive lamb waves presence of damage in the structure.

The damage could be cracks, delamination, debonding corrosion etcetera.

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In flat plates, ultrasonic guided waves travel as Lamb waves and
shear horizontal waves.

Lamb waves are vertically polarized while shear horizontal waves are
horizontally polarized.

In flat plates ultrasonic guided waves travel as lamb waves and shear horizontal waves. Lamb waves are vertically polarized, while shear horizontal waves are horizontally polarized.

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plate thickness: $2d$

Egn. of motion for an isotropic elastic motion is given by:

$$\mu \nabla^2 U + (\lambda + \mu) \nabla \nabla \cdot U = \rho \frac{\partial^2 U}{\partial t^2} - W$$

where λ, μ - Lamé's constant
 ρ - mass density
 U - displacement vector

Assuming the displ. vector as below: $U = \nabla \Phi + \nabla \times H \quad \text{---(1)}$

Let us consider a plate, stress free upper and lower surface as shown in the figure.

The local axis are marked as shown in the figure, the thickness of the plate is $2d$, let us take a free body diagram of a small area extracted from this plate, let us mark the axis σ_{xx} σ_{yy} , which is 0 and σ_{yx} also 0 and σ_{yz} also 0, which will be σ_{zz} .

So, let us say this is my free body diagram of a small area, extracted from the plate that is this figure let us say 2, this figure 1 consider as a plate with free boundary. Plate thickness is $2d$, equation of motion for an isotropic elastic motion is given by where λ and μ or called λ is constant ρ is the mass density u is the displacement vector, assuming the displacement vector as below u is $\text{del } \phi$ plus $\text{del } \times H$.

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When Φ & H are potential functions, and given by:

$$\Phi = f(x) e^{i(\xi x - \omega t)}$$

$$H = (h_x(x) i + h_y(y) j + h_z(z) k) e^{i(\xi x - \omega t)} \quad (2)$$

where ω - circular frequency
 ξ - wave number
 wave speed, $c = \omega/\xi$

Where phi and H are potential functions and given by phi is f(x) e^{i(xξ - ωt)} on H is h_x y i plus h_y y j plus h_z y k e^{i(xξ - ωt)}, where omega is the circular frequency and zeta is the wave number and wave speed c is given by ratio between omega and zeta in that omega zeta and z.

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Assuming (ω, ξ, c) , governing equation is now written by:

$$\nabla^2 \Phi = \frac{1}{C^2} \frac{\partial^2 \Phi}{\partial t^2}$$

$$\nabla^2 H = \frac{1}{C^2} \frac{\partial^2 H}{\partial t^2} \quad (4)$$

$$\nabla \cdot H = 0$$

The governing equation is now written by del square phi is 1 by C p square dou square phi by dou t square, del square H is 1 by C s square dou square H by dou t square and del dot H is 0 equation 4.

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for the plane strain, (which is z invariant)
Eq(4) now reduces to the following form:

$$f'' - z^2 f = -\frac{\omega^2 f}{C_p^2}$$

$$h''_x - z^2 h_x = -\frac{\omega^2 h_x}{C_s^2}$$

$$h''_y - z^2 h_y = -\frac{\omega^2 h_y}{C_s^2}$$

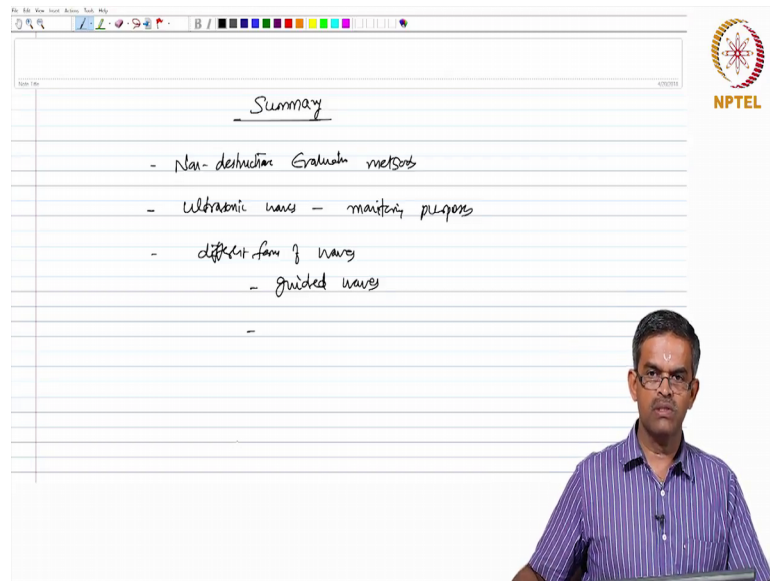
$$h''_z - z^2 h_z = -\frac{\omega^2 h_z}{C_s^2}$$

where
 C_p : pressure wave speed
 - longitudinal component
 $C_p^2 = \frac{\lambda + 2\mu}{\rho}$
 $C_s^2 = \frac{\mu}{\rho}$
 C_s : shear wave speed
 - transverse component

Now, for the plane strain, which is z in variant, equation 4 now reduces to the following form for a plane strain problem; $f'' - z^2 f = -\omega^2 f / C_p^2$ $h''_x - z^2 h_x = -\omega^2 h_x / C_s^2$ $h''_y - z^2 h_y = -\omega^2 h_y / C_s^2$ $h''_z - z^2 h_z = -\omega^2 h_z / C_s^2$.

$h''_y - z^2 h_y = -\omega^2 h_y / C_s^2$, $h''_z - z^2 h_z = -\omega^2 h_z / C_s^2$, where C_p which is a longitudinal component and is given by $\lambda + 2\mu / \rho$, whereas C_s^2 this is equation 5 this is C_p^2 , whereas this is C_p / C_s^2 is given by μ / ρ , whereas C_s is called shear waves p and this is transverse component.

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The image shows a digital whiteboard interface. At the top, there is a menu bar with options like 'File', 'Edit', 'View', 'Insert', 'Action', 'Task', and 'Help'. Below the menu bar is a toolbar with various drawing tools. The main area of the whiteboard contains the following text:

Summary

- Non-destructive Evaluation methods
- Ultrasonic waves - monitoring purposes
- different form of waves
 - guided waves
-

In the bottom right corner of the whiteboard, there is a small inset image of a man with glasses and a purple striped shirt. To the right of the whiteboard, there is a circular logo with a star-like pattern and the text 'NPTEL' below it.

In this lecture we tried to understand; what are the various non destructive evaluation methods, what is the speciality about these ultrasonic waves which are used for monitoring purposes. What would be the different forms of ways and what would be the use of guided waves in comparison to the conventional ultrasonic waves.

And we are in the process of identifying understanding how these guided waves like lamb waves can be used for monitoring purposes. We will continue this lecture in the next class.

Thank you very much and bye.