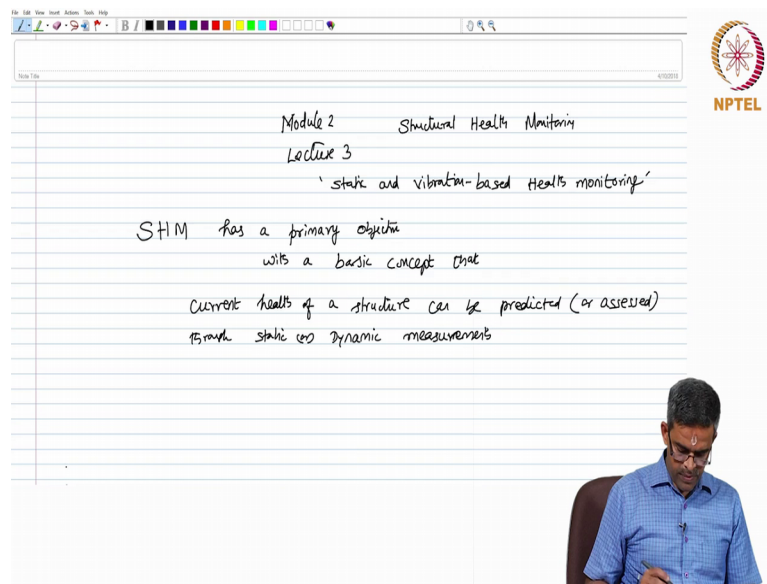


Structural Health Monitoring (SHM)
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Lecture – 21

PART – 1: Estimation of Structural Health i.e. Structural Health Monitoring (SHM)

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Module 2 Structural Health Monitoring
Lecture 3
'Static and vibration-based Health monitoring'

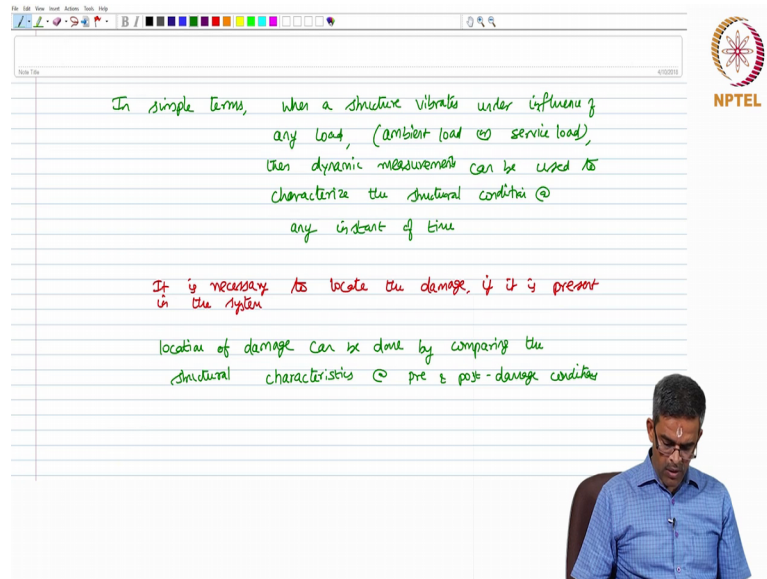
SHM has a primary objective
with a basic concept that
current health of a structure can be predicted (or assessed)
through static or dynamic measurements

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Friends, welcome to the module-2, lecture-3 on the course Structural Health Monitoring.

In this lecture we are going to introduce static and vibration based health monitoring. Having said in the previous lectures that structural health monitoring has a primary objective with a basic concept that current health of a structure can be predicted or I should say assessed static or dynamic measurements.

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In simple terms, when a structure vibrates under influence of any load, (ambient load or service load), then dynamic measurements can be used to characterize the structural condition @ any instant of time.

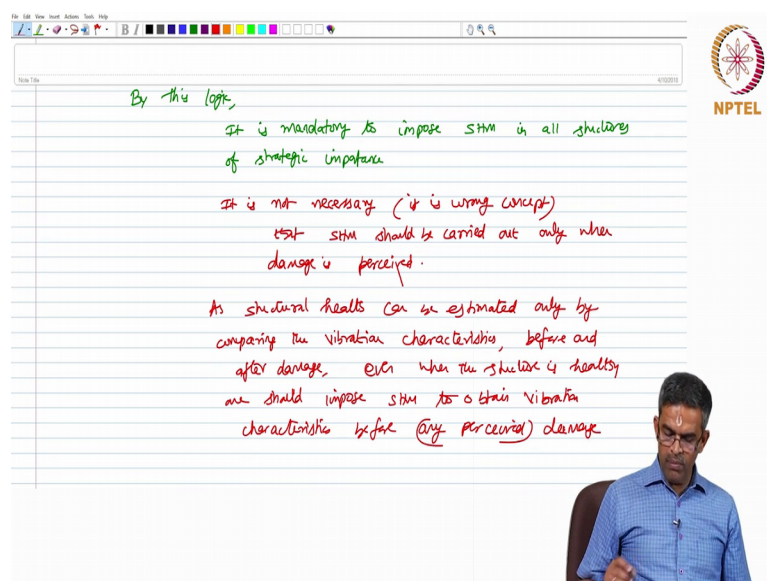
It is necessary to locate the damage, if it is present in the system.

location of damage can be done by comparing the structural characteristics @ pre & post-damage condition.

In simple terms when a structure vibrates under influence of any load it may be ambient load or service load for which the structure is designed, then dynamic measurements can be used to characterize the structural condition at any instant of time.

To do this it is necessary to locate the damage if it is present in the system so, location of damage can be done by comparing the structural characteristics at pre and post damage conditions.

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The image shows a presentation slide with a white background and a grid pattern. The text is handwritten in green and red. The NPTEL logo is visible in the top right corner. A man in a blue shirt and glasses is visible in the bottom right corner, looking at the slide.

By this logic,

It is mandatory to impose SHM in all structures of strategic importance.

It is not necessary (it is wrong concept) that SHM should be carried out only when damage is perceived.

As structural health can be estimated only by comparing the vibration characteristics, before and after damage, even when the structure is healthy we should impose SHM to obtain vibration characteristics before (any perceived) damage.

By this logic, friends, it is mandatory to impose structural health monitoring in all structures of strategic importance. It is not necessary. In fact, it is a wrong concept that SHM should be carried out only when damage is perceived.

As structural health can be estimated only by comparing the vibration characteristics before and after damage even when the structure is healthy one should impose structural health monitoring to obtain vibration characteristics before any perceived damage.

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If all structures are designed to cater to the varying dynamic characteristics, then why SHM is necessary when no damage occurs?

Dynamic characteristics vary significantly with the following

- changes in loading pattern (re-distribution)
- ageing of the material (material degradation)
 - change in Mass and change in stiffness
- changes in support conditions with period of time

- very important to periodically update the vibration characteristics of all structures (strategic importance)

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Then one may ask me a question if all structures are designed to cater to the varying dynamic characteristics then why structural health monitoring is necessary when no damage occurs? That is a very interesting question.

Friends, it is important to note that the dynamic characteristics vary significantly with the following; changes in loading pattern because loading pattern will invoke redistribution, ageing of the material which we call material degradation which can cause change in mass and change in stiffness, changes in support conditions with period of time etcetera can make the dynamic characteristics to be different from the top it is being designed.

So, it is very important to periodically update the vibration characteristics of all structures I should say, but at least for structures of strategic importance this is necessary.

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only based on pre-damaged condition & compare it with the damaged state, health of the structure can be assessed.

(U) static-based SHM

SHM, foremost step is damage identification.

Damage identification can be also done through dead load redistribution

Basic hypothesis is that

dead load of the structural system will get redistributed automatically when damage occurs in the structural system.

Because, only based on the pre-damaged state and comparing it with the damaged state, health of the structure can be assessed.

So, let us talk about static-based SHM. We all know that in structural health monitoring the foremost step is damage identification damage identification can be also done through dead load distribution. Let see how. The basic hypothesis behind this statement is that dead load of the structural system we will get redistributed automatically when damage occurs in the system.

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Measurements required?

stress and strain, developed due to dead load are used as input to identify the damage

- static load test

Let us say then in that case what are the measurements required; stress and strain developed due to dead loads are used as input to identify the damage, this is what we call as static load test.

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Algorithm:

Let us consider a fixed beam, as shown in the figure below

Let us perceive that, there is a damage @ distance 'a' from the left hand support

Let the damage region be of span δ

Let us consider a fixed beam as shown in the figure below. The beam is subjected to some loading pattern which is function of x which is considered as q_0 and x is measured positive towards the length of the member and y is measured positive towards upward.

Let us call this end as A and this end as B. Let us say we have a moment applied here which is M_A the length of the member is L and let us perceive that there is a damage at a distance a from the origin, that is from the left hand support.

Let us say at section a which is distance a from here, there is a damage in the beam. So, we call this as damaged zone therefore, this section will have $E I$ undamaged and this section will also have $E I$ undamaged whereas, this section will have $E I$ damaged.

Let us say it has got two reactions R_A and R_B . So, let us say let the damage region b of span δ . So, this is δ and this is a , ok.

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Damage zone length = δ
 Damage location = a

Moment @ any section $x-x$, in general, is given by the following expression:

$$M_x = + R a (x) - \frac{q}{2} x^2 + M_A \quad (1)$$

Let $E I_{und}$ = Modulus of Rigidity of the undamaged portion
 $E I_{dam}$ = Modulus of Rigidity of the damaged portion

We already know that, $E I \frac{d^2 y}{dx^2} = M_x \quad (2)$

So, from the figure it is clear that the damage zone length is delta and damage location is a from the left support. Let us say moment at any section X-X in general is given by the following relationship M_x is equal to plus $R a$ into x minus $q x$ square by 2, plus M_A , where M_A is this q is the downward load and $R a$ is this, equation – 1.

Let $E I_{undamaged}$ be the modulus of rigidity of the undamaged part and $E I_{damage}$ be the modulus rigidity of the damaged part. We already know that $E I d^2 y$ by dx^2 square is equal to M_x .

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Integrate $E I (2)$ once, we get:

$$E I \frac{dy}{dx} = \frac{d(M_x)}{dx} + C_1 \quad (3)$$

Further integrate,

$$E I y = \frac{d^2(M_x)}{dx^2} + C_1 x + C_2 \quad (4)$$

Substituting for M_x from the $E I (1)$,

$$E I \left(\frac{dy}{dx} \right) = \frac{R a x^2}{2} - \frac{q x^3}{6} + M_A x + C_1$$

$$E I y = \frac{R a x^3}{6} - \frac{q x^4}{24} + \frac{M_A x^2}{2} + C_1 x + C_2$$

Integrating equation – 2 once we get, E I dy by dx will be equal to d M X by dx plus integration constant C 1. Further integrating E I into y will be d square M X by dx square plus C 1 x plus C 2 substituting for M X from the equation – 1.

Equation – 1 is here, ok. Substitute to M X. So, E I into y will be E I dy by dx will be equal to R A x square by 2 minus q x cube by 6 plus M A x plus C 1. E I y is R A x cube by 6 minus q x 4 by 24 plus M A x square by 2 plus C 1 x plus C 2 , but there are different regions in the beam for which this equation should be separately written.

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a) Region $0 \leq x \leq a$
 $EI_{undamaged}(y) = \frac{RAx^3}{6} - \frac{qx^4}{24} + \frac{Mx^2}{2} + C_1x + C_2 \quad (0 \leq x \leq a)$

b) for region $a \leq x \leq a+\delta$
 $EI_{damaged}(y) = \frac{RAx^3}{6} - \frac{qx^4}{24} + \frac{Mx^2}{2} + C_3x + C_4 \quad (a \leq x \leq a+\delta)$

c) for region $(a+\delta) \leq x \leq L$
 $EI_{undamaged} = \frac{RAx^3}{6} - \frac{qx^4}{24} + \frac{Mx^2}{2} + C_5x + C_6 \quad (a+\delta \leq x \leq L)$

Let us talk about region 0 less than x less than a in that condition E I undamaged of y 1 you can see the equation. A undamaged of y 1 will be R A x cube by 6 minus q x 4 by 24 plus M A x square by 2 plus C 1 x plus C 2 this is for 0 less than x less than a.

Now, for region a less than x which is further less than a plus delta E I damaged because at the damage region of y 2 will be R A x cube by 6 minus q x 4 by 24 plus M A x square by 2 plus C 3 x plus C 4. So, this is a less than x less than delta plus a.

For region a plus delta less than x less than L we can also write again it is an undamaged region. So, undamaged will be V A x cube by 6 plus q x 4 sorry minus q x 4 by 24 plus ma x square by 2 plus C 5 x plus C 6. This is a plus delta less than x less than L.

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Boundary condition

$$\begin{array}{l} y_1(0) = 0 \\ y_2(0) = 0 \\ y_3(0) = 0 \end{array} \quad \text{①}$$

$$y_1(a) = y_2(a) \quad \Rightarrow \quad E \omega = \frac{M \alpha \gamma}{E I_{undamaged}}$$

$$y_2(a+\delta) = y_3(a+\delta) \quad \Rightarrow \quad E \omega = \frac{M \alpha \gamma}{E I_{damaged}}$$

Let us see what are the boundary conditions. Now, let us replace this is the R A, let us see what are the boundary condition to solve. This equation $y_1(0) = 0$, $y_2(0) = 0$ and $y_3(0) = 0$ or $y_3(L)$, this the first set we have.

The second set is $y_1(a)$ will be also equal to $y_2(a)$ and $y_2(a + \delta)$ will be $y_3(a + \delta)$ which imposes an additional condition $E \omega$ is $M \alpha \gamma$ by $E I_{undamaged}$ $E \omega$ is also equal to $M \alpha \gamma$ by $E I_{damaged}$ depending upon the region once this is said.