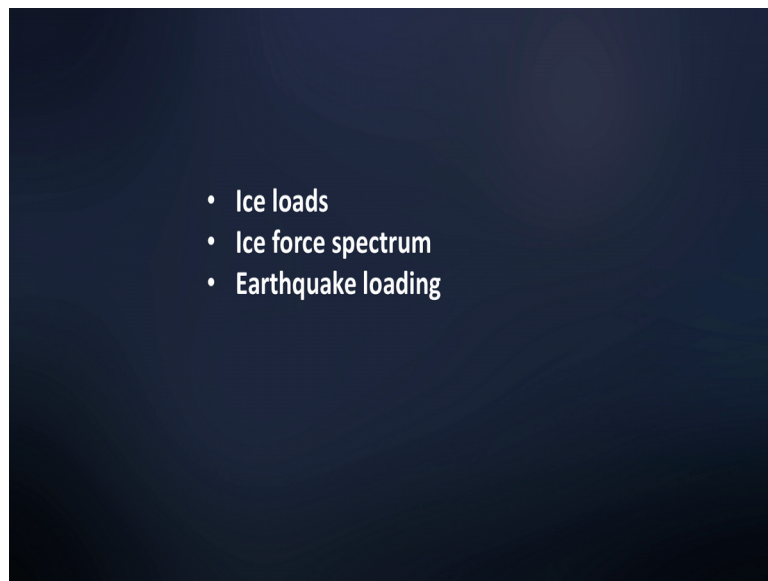


Computer Methods of Analysis of Offshore Structures
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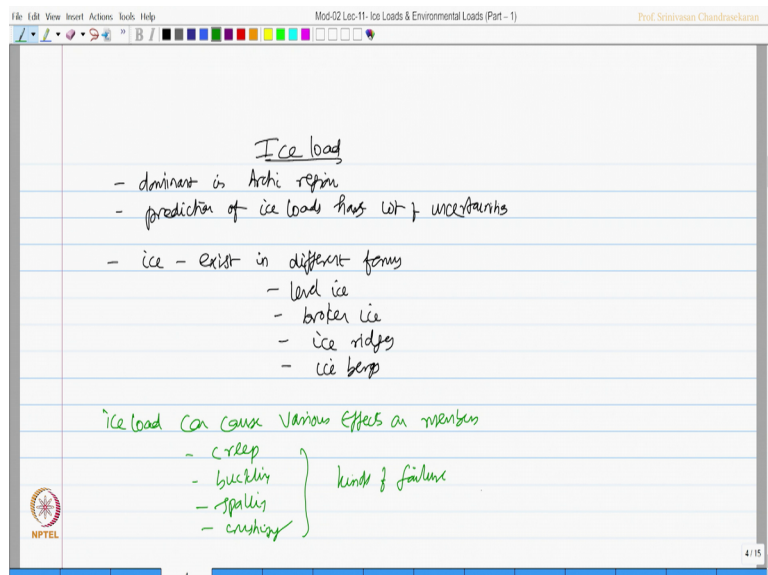
Module - 02
Lecture - 11
Ice load and earthquake load

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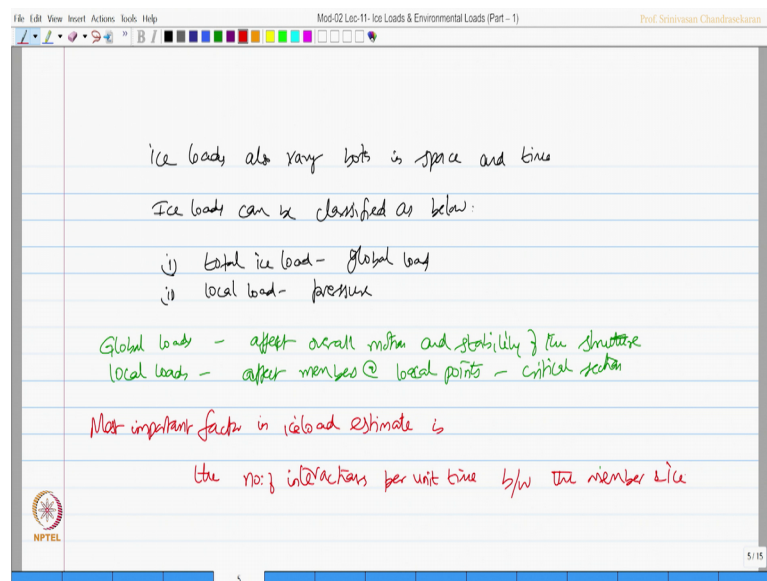
Let us move on to the next important load which is ice load.

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Ice loads are generally dominant in arctic region. Prediction of ice loads has a lot of uncertainties. Ice actually exists in different forms like level ice, broken ice, ridges and icebergs, ice can result in various effects. Ice loads can cause various effects on members; it can cause creep, can cause buckling, it can cause spalling and the failure can also be due to crushing; these are all different kinds of failures which can be caused by ice on members.

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The image shows a screenshot of a presentation slide with handwritten text. The text is as follows:

Ice loads also vary both in space and time

Ice loads can be classified as below:

- (i) total ice load - global load
- (ii) local load - pressure

Global loads - affect overall motion and stability of the structure
Local loads - affect members @ local points - critical section

Most important factor in ice load estimate is
the no. of interactions per unit time b/w the member & ice

The slide also features a standard software interface at the top with a menu bar (File, Edit, View, Insert, Actions, Tools, Help) and a toolbar. The title bar reads 'Mod-02 Lec-11- Ice Loads & Environmental Loads (Part - 1)' and the presenter's name 'Prof. Srinivasan Chandrasekaran' is visible in the top right corner. An NPTEL logo is present in the bottom left corner, and the slide number '5/15' is in the bottom right corner.

More interestingly ice loads also vary both in space and time.

So, ice loads can be classified as below one, total ice load otherwise called as global load to local load otherwise called as pressure. Interestingly the global loads affect overall motion and stability of the structure whereas, the local loads affect members at local points all it is a critical sections. So, the most important factor in ice load estimate is the number of interactions between the member and ice.

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Current international codes include equations for estimating ice load as static ice loads

- Ice loads also depend on shape of the structure

ice loads on conical structures are lesser than cylindrical structures (Sanderson, 1988)

main reason for this reduction

well-designed conical geometry can alter the failure mode of the structure, caused by ice from crushing to bending

Interestingly the current international codes include equations for estimating ice load as static ice loads, it is important to know that ice loads also depend on shape of the structure which it is encountering; study show that ice loads on conical structures like pyramids or lesser than cylindrical structures.

So, that is given by a good reference Sanderson 1988 the main reason for this reduction is due to the fact that, the well designed conical geometry can alter the failure mode of the structure caused by ice from crushing to bending that is the reason.

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Ice force spectrum on a narrow conical structure

$$S^{\ddagger}(f) = \frac{A F_0^2 \bar{T}^{-5}}{f^{\alpha}} \exp\left\{-\frac{B}{\bar{T}^{\alpha} f^{\beta}}\right\} \quad (1)$$

A and B are constants $A = 10$, $B = 5.47$

$\bar{T} = \frac{L_b}{v}$ - ice period

L_b = ice breaking length = (kh) h : ratio of ice thickness to ice breaking length (4.051)

F_0 = force amplitude on the member

f : frequency $\alpha = 0.64$

v : velocity $\beta = 0.64$

So, ice given again by ice force spectrum on a narrow conical structure, this is given by the following equation $A F \bar{v}^2 T \bar{v}^{-\alpha} f^{-\beta}$ or exponential minus B by T bar alpha and f beta equation 1. Double equation A and B are constants whose values are A is 10 and B is taken as 5.47, T bar is L_b / v which is called ice period L_b is called ice breaking length typically it is between 4 to 10. $F \bar{v}^0$ is called force amplitude on the structural member, the ice breaking length is given by $k L_c$ where k is the ratio of ice thickness to ice length, where this lies between 4 to 10 not this value; f is the frequency is the variable in the spectrum and v is the ice velocity the constants alpha is 0.64 beta is 0.64.

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The image shows a digital whiteboard with the following handwritten content:

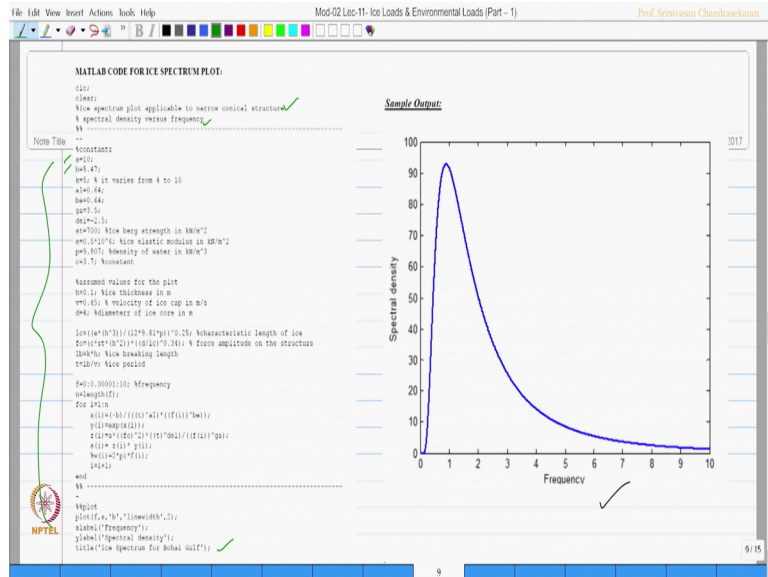
$$F_0 = C \sigma_f h^2 \left(\frac{D}{L_c} \right)^{0.34} \quad (2)$$

$C = \text{constant} = 3.7$
 σ_f : ice breaking strength (0.7 MPa)
 h : ice thickness
 D : dia of ice cone
 L_c : characteristic length = $\left(\frac{E h^3}{12 g \rho_w} \right)^{0.25}$
 $\gamma = 3.5$
 $\delta = 2.5$
 E : ice elastic modulus (0.5 GPa)
 ρ_w : density of sea water

And F_0 is given by $C \sigma_f h^2 D / L_c$ to the power 0.34 where C is again a constant which is 3.7 σ_f is ice breaking strength which is 0.7 mega Pascal, h is the ice thickness D is the diameter of the ice cone and L_c is the characteristic length.

So, the equations the power γ and δ respectively 3.5 and 2.5 the characteristic length L_c is further given by $E h^3 / 12 g \rho_w$ raised the power 0.25, where E is ice elastic modulus which is given by 0.5 Giga Pascal and ρ_w is density of seawater the typical I spectrum which can be plotted its looked into the figure here.

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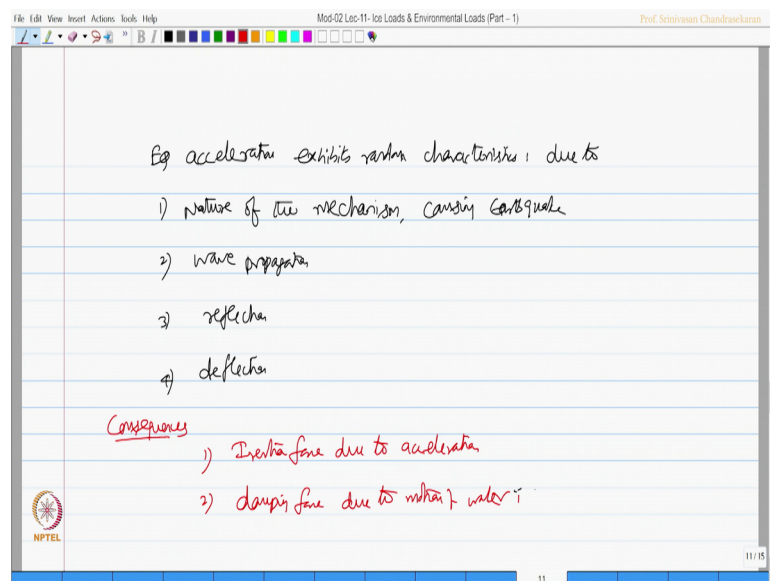


And we have given the program to plot by spectrum on a narrow conical structure, the plot shows the spectral density versus frequency, the constants as I said are already given in the equation a 10, b 5.47 and other constants are named as per the programming variables as alpha beta gamma and delta. Now, the plot is shown on the right hand side whereas, the coding required to plot the spectrum is given on the left hand side of the screen. So, you can use this coding directly to get the ice spectrum for Bohai gulf as you see here.

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The next kind of loading is a earthquake load, we understand that offshore structures which are stiff and connected that is fixed to the seabed, will undergo all will experience earthquake loads directly. However, compliant structures like TLP will also experience earthquake loads let us see how. This is a superstructure of the TLP connected to the seabed using tendons the seabed experiences earthquake loads, earthquake loads cause ground displacement that is displacement of the seabed this induces change in T_0 , this change in T_0 alters buoyancy and weight and stiffness in the TLP therefore, the earthquake loads have indirect effect here on **compliant** structures.

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We all know from the literature that earthquake acceleration exhibits random characteristic, this is due to nature of the mechanism causing earthquake, it can be due to wave propagation, it can be also due to reflection and further can be due to deflection. What are the consequences of earthquakes on offshore structures; one it can cause inertia force due to the acceleration, it can result in a damping force due to motion of water particle.

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Compliant structures - like TLP. (T_0) - varies
- causes dynamic tension variation

$$\Delta T = \frac{AE}{L} \{ x(t) - x_g(t) \}$$

$x(t)$: instantaneous response vector of TLP
 $x_g(t)$: ground displacement vector

$x_{1g}(t)$: horizontal ground displacement
 $x_{3g}(t)$: vertical ground displacement

Ground motion - simulated by Kanai-Tajimi ρ

The slide also features a list of ground displacement components in a curly brace: $x_{1g}(t)$, 0, $x_{3g}(t)$, 0, 0, 0.

So, as I said in **compliant** structures like TLP the T_0 varies, this causes dynamic tension variation. So, this variation is given by a factor of the axial stiffness which is x_t minus x_g of t , where x_t is the instantaneous response vector of TLP, on x_g of t is ground displacement vector one can quickly look at this vector it is going to have the effect in such degree no effect in sway Hitler effect in heave degree no effect in roll pitch and yaw.

So, I should say now that the x_1 of g is actually horizontal ground displacement and x_3 of g is vertical ground displacement. So, earthquake causes displacement and the ground motion which is caused by earthquakes is simulated by Kanai Tajimi ground spectrum.

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one-sided psd is given by

$$S_{\ddot{y}_g \ddot{y}_g(\omega) = \left\{ \frac{\omega_g^4 + 4\zeta_g^2 \omega_g^2 \omega^2}{(\omega_g^2 - \omega^2)^2 + 4\zeta_g^2 \omega_g^2 \omega^2} \right\} S_0 \quad (2)$$

where S_0 - intensity of excitation = $\frac{2\zeta_g \sigma_g^2}{\pi \omega_g (1 + 4\zeta_g^2)} \quad (3)$

ω_g : Natural freq of ground motion
 ζ_g : damping of the ground motion
 σ_g^2 : Variance of the ground accelerations

Important parameters of K-T spectrum
 ② parameter spectrum

The one sided power spectral density function is given by $S_{\ddot{y}_g \ddot{y}_g}$ of ω is ω is ω to the power 4 plus 4 zeta g square, ω square ω square by ω square ω square minus ω square the whole square plus 4 zeta g square, ω square ω square off S_0 , where S_0 is called intensity of excitation which is given by $2\zeta_g \sigma_g^2$ by $\pi \omega_g (1 + 4\zeta_g^2)$, ω_g is natural frequency of the ground motion, ζ_g is damping of the ground motion and σ_g^2 is variance of the ground motion.

So, these three are important parameters of Kanai-Tajimi spectrum.

So, Kanai-Tajimi spectrum is a three parameter spectrum, what will be the consequence of this?

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Consequence of ϵ_p on compliant structures (TLP)

- Causes dynamic tension variation (T_0) - 65%
causing pullout
- It affects rigid d.o.f (like heave) - dangerous
 - safety of the platform
- loss of functional value of the platform

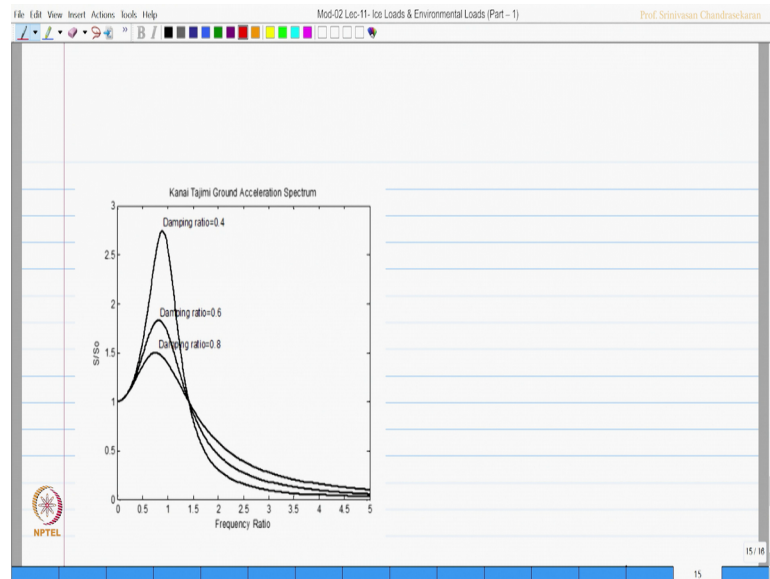
- Srinivasan Chandrasekaran . 2015 . Advanced Marine structures CRC press

- Srinivasan Chandrasekaran . 2017 . Dynamic analysis and design of offshore structures Ed-II, Springer, Singapore

The consequence of this on let us say **compliant** structures like TLP could be, it results in dynamic tension variation in T_0 and this variation can be as high as 65 percent causing **pullout**. It affects rigid degrees of freedom like heave which is quite dangerous because it can challenge the safety of the platform. This ultimately also results in loss of functional value of the platform.

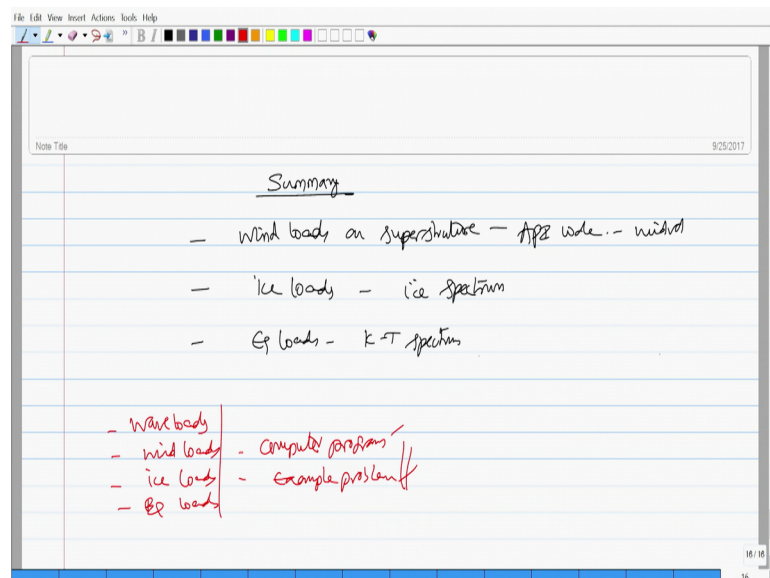
So, detailed results can be seen from the following textbooks: advanced marine structures authored by me published by CRC press; there is one more book which also discusses the behavior again authored by me dynamic analysis and design of offshore structures addition to **Springer** Singapore.

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So, friends for different damping ratio the typical Kanai Tajimi ground spectrum looks like this as you see on the screen now.

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Let us see the summary what we learned in this lecture we did one more numerical to understand the wind loads on superstructure of the platform, we have used API code to compute the wind velocity, we have learnt how to estimate ice loads we have seen ice spectrum, we have also learnt how to calculate earthquake loads we have learnt Kanai Tajimi spectrum. So, far we have learnt wave loads, wind loads, ice loads earthquake

loads including the computer program to calculate them solving example problem to understand.

I hope you follow these lectures and you will be able to write these programs on your own and check the results and compare the answers what we have in this screen here.

Thank you very much.