

Dynamics of Ocean Structures
Prof. Srinivasan Chandrasekaran
Department of Ocean Engineering
Indian Institute of Technology, Madras

Lecture – 29
Fluid Structure Interaction

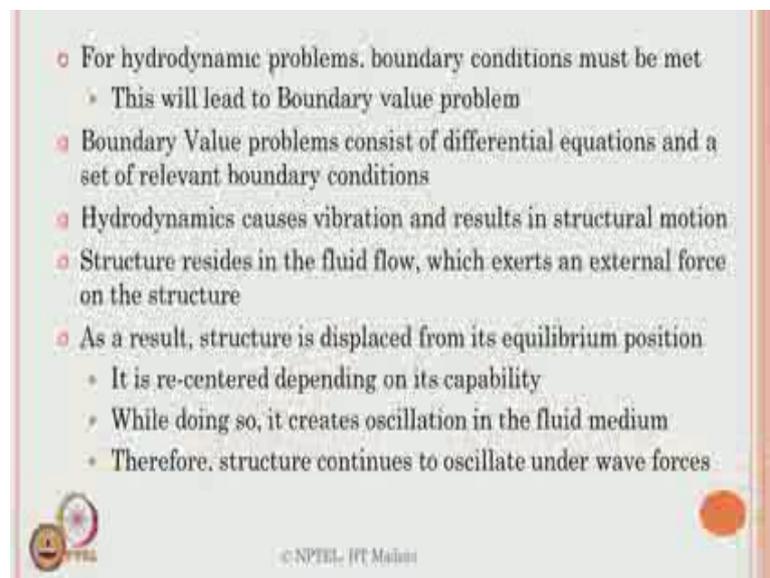
So, this is the module 2 lecture which we will talk about FSI fluid structure interaction. Then we will deal with the dynamics of detailed dynamic analysis of offshore structures. We will take up examples of different platforms and will handle both the LHS and RHS of the equation of motion. That is, we will derive the mass matrix stiffness matrix and damping matrices of the given system. We will also talk about how to estimate f of t of course you cannot solve this x of t because it needs lot of iterations. So, we will use numerical solutions for this, and you will show the results from the research proper directly. Before we get into understand how to do a dynamic analysis of offshore platforms directly.

Let us try to talk about in the design perspective, what will be the influence on fluid structure interaction. So, actually if you look at the first module lectures, where we are talking about different kinds of forces acting on structural systems. We have already said the wave force is one of the important contributors, for shore platforms, which is irregular and prescribed and random dynamic loading acting on the structure. There are many theories available in the literature define they what about the water body kinematics sees for salivation which varies with velocity current presence etcetera.

So, we can use different ideal equations, to find out the velocity and acceleration, of the water particle. Then we will also try to know how to get the forces, lateral forces expected on the structural member by these wave interaction. But now I will talk about the design perspective on fluid structure interaction. Where we will say what are those important contributors when in a fluid flow a structure member remains in a fluid rigid. So, what will be the interference effects on structural member on the fluid flow we all know that as long as there is no obstruction, by any member, on any fluid or any domain, no force is excited. For example, wind blows from left to right on this hall and there is no obstruction to the wind flow wind that will not exert any force.

Wind or any lateral force will be excited, on the member only when there is obstruction caused to the fluid flow. So, let us talk about what is that obstruction caused by the presence of member. If the member is vertical, if the member is horizontal, if the member is large diameter, if the member is fixed at the bottom member is floating what would be the interference effects of this. And how design perspective is important in fluid structure interaction. Because it is important to know, that what will be the forces arising from different position of the members, and a different category, if you really wanted to know f of t in equation of motion.

(Refer Slide Time: 02:47)



So, it is very clear to understand basically, for a hydrodynamic problem, we all know that boundary conditions must be met. If you look at the boundary condition implementations on a hydrodynamic problem, it will ultimately land up to what we call b v p is which is classified as boundary value problems.

Now, BVP consisting of differential equations, and of course, a set of relevant boundary conditions, which has got to be a met, to solve the boundary value problems. Now we are bothered about this laid, or this point onwards. Hydrodynamics actually causes vibration. The moment it causes vibration, it will result in a structural motion. The moment structures starts moving in the regime of fluid flow, there is external action acting on the

member. Now this structure will be displaced whether a structure is fixed, whether structure is floating, complaint there is always at displacement on the structural member which is the result of the external force, acting on this member, which arises essentially from the vibration caused by hydrodynamic effects.

Now, we are not bothered about the boundary value effects. Because the boundary value effects will only modify, the characteristic of hydrodynamic forces. What we are both bothered here is, what is the influence of the structural displacement on the fluid domain. We are important we are looking only this part of it the moment is a structure displaced from it is equilibrium position. We all know for a given design, the structure will always try to re centered it itself. What does not mean is when the structure is displaced from it is equilibrium position, where the natural tendency in a design the structure, will try to come back to it is normal position.

Now, it cannot happen because, the structure can regain it is normal position only in the absence of external loads. Now the external loads in offshore systems are continuously present. There is no absence case considered therefore, re centering will always be an oscillatory motion. This oscillation will again cause a secondary force in the medium itself. Now there are 2 forces oscillated here. One the external force caused by the fluid flow on the member plus the result of the fluid flow, which is causing displacement in the member, which invokes equilibrium movement on the member, by re centering capability, which induce the secondary motion, which call oscillation. So, there are displacements, or causing vibrations, and oscillations. There are 2 important categories of aspects dynamic present, in FSI therefore, ultimately the structural member will continue to oscillate, under the action of wave forces.

(Refer Slide Time: 05:17)

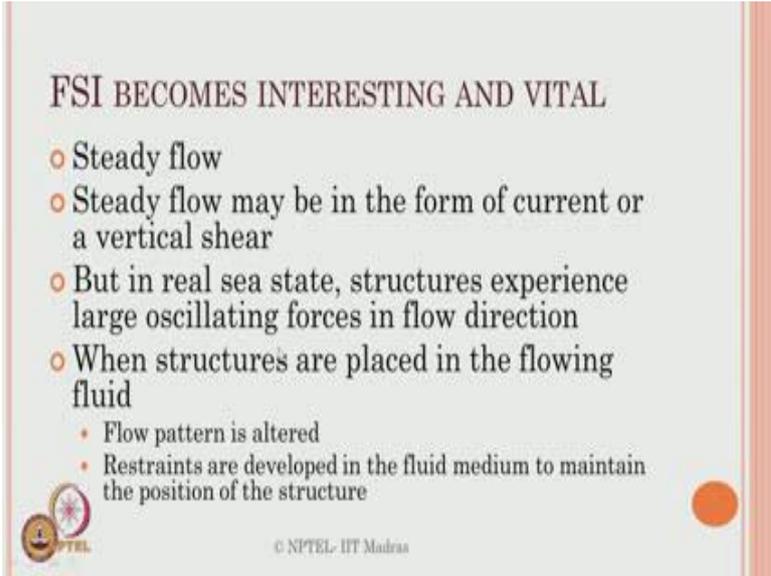
- Fluid structure interaction plays an important role for structures placed in the path of flowing fluid
 - Presence of structure alters fluid flow field in its vicinity
 - Degree of compliance offered by the structure adds further complexity due to the reaction it offers to the excited force
 - Even though structures remain flexible (for example TLP) in certain degrees-of-freedom, dynamics become important
- It is not their deformation capacity that is looked upon in this context

Having said this, we must understand that, fluid structure interaction plays a very important role for structures placed in the path of flowing fluid. The presence of structure, significantly alters this flow field, in its vicinity. That is very important. Now depending upon the diameter of the member versus, the wave length effect, what we call d by λ effect etcetera. The significant alteration of the structure, in the fluid field may not be present. So, what we mean to say is, the structural presence is felt only with in vicinity. So, in the closed regime, it is present. On the other hand if you are got 2 members placed at a large distance or spaced as a large distance, the cascading effect of one on the another, caused by the fluid medium may not be influential. So, spacing d by λ or the diameter versus wave length, all are important factors, now to understand that what would be the influence on the presence, of structure in the fluid medium.

Adding to it, the degree of compliance offered in the structure because the degree of compliance is nothing, but the support conditions given to the system, by the external boundaries. For example, it can be floating and anchor to the sea bed. It can be completely floating and controlled by a DPS system it can be rigidly fixed to the sea bed etcetera. So, what is the boundary effect you are giving to the structural system, to avoid the degree of compliance, or to induce the degree of compliance, to a structural system, adds further complexity? Because this will create additional reaction forces, to the

excited force, now even though the structures remained flexible for example, in TLP in certain degrees of freedom, dynamics still become important. Because it is not the deformation capacity that is looked upon it is actually the vibration caused by the medium is looked upon.

(Refer Slide Time: 07:08)



FSI BECOMES INTERESTING AND VITAL

- Steady flow
- Steady flow may be in the form of current or a vertical shear
- But in real sea state, structures experience large oscillating forces in flow direction
- When structures are placed in the flowing fluid
 - Flow pattern is altered
 - Restraints are developed in the fluid medium to maintain the position of the structure

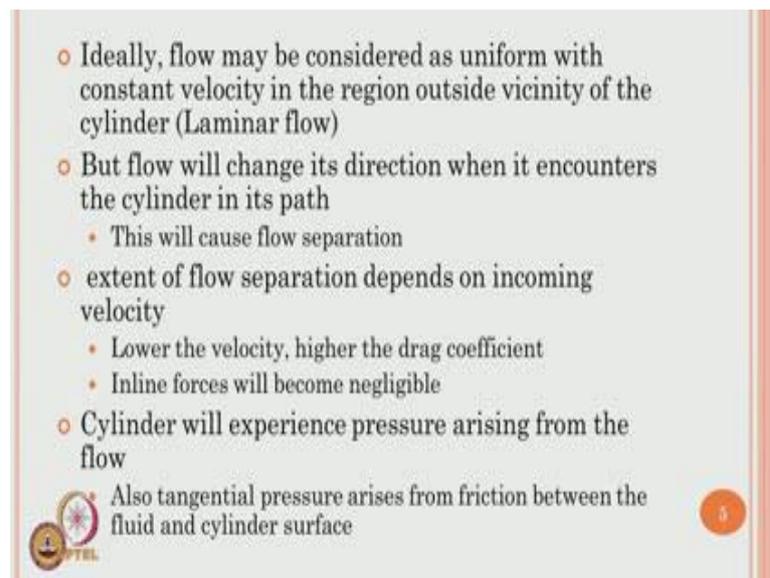
© NITEL- IIT Madras

Therefore, fluid structure interaction becomes interesting and becomes vital for structures placed in the fluid medium, because it alters the steady flow steady flow may be in the form of current, or a vertical shear, because it induces vertical shear. It induce the displaced or differential pressure gradient, that is upstream and downstream side, which we will see the next slide, but in the real state structures experience large oscillating forces in the flow direction. Now there are 2 ways here. One is structures experience forces in the direction of flow medium one is in the transverse direction.

Now, when the structures are placed in the flowing fluid flow pattern is significantly altered, restraints are developed in the fluid medium to maintain the position of the structure. Because the moment you try to push the structure may start exerting it is boundary value limitations to the fluid medium itself.

So, that will cause an additional reaction, which will induce force on the medium back and depending upon who is the winner either the structure is effected or the fluid medium is altered.

(Refer Slide Time: 08:12)



- Ideally, flow may be considered as uniform with constant velocity in the region outside vicinity of the cylinder (Laminar flow)
- But flow will change its direction when it encounters the cylinder in its path
 - This will cause flow separation
- extent of flow separation depends on incoming velocity
 - Lower the velocity, higher the drag coefficient
 - Inline forces will become negligible
- Cylinder will experience pressure arising from the flow

Also tangential pressure arises from friction between the fluid and cylinder surface

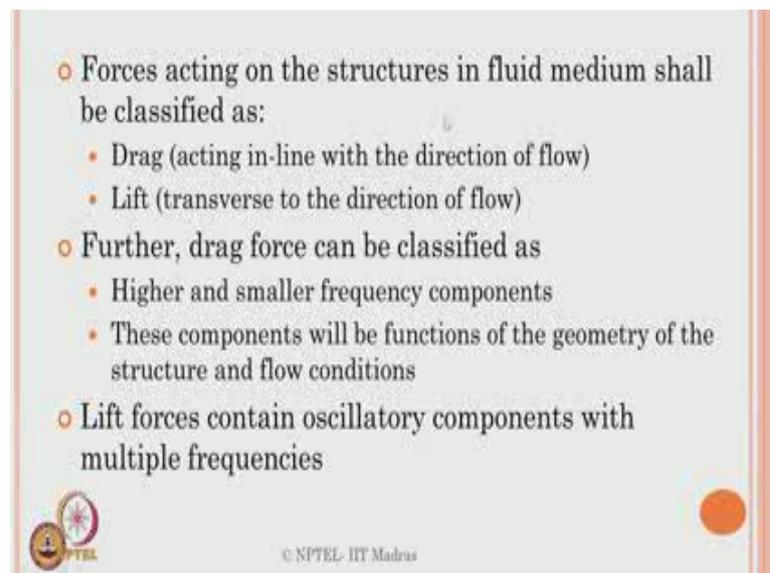
Ideally, flow may be considered as uniform, with constant velocity in the region outside the vicinity. Which we call technically in hydrodynamics as laminar flow, but flow with the change it is direction, when it encounters the cylinder in it is path. This will cause what is call flow separation. Now the extent of flow separation in a given system strictly depends on incoming velocity. Therefore, water body in a kinematics becomes very important. We will talk about this equation slightly later, in the end of the lecture. So, water body in kinematics, becomes very important because the extent of flow separation depends on that. One may ask me a question, what would be the influence on flow separation on the force exerted on the structure.

Once the flow is separated, then they will act as an independent medium there is an interaction between the flow lines. So, the extent of flow separation depends on incoming velocity lower, the velocity higher the drag coefficient. Now the drag coefficient which is called a c_d which is very important item, which is now identically argued upon in the research friend, which you call as drag crisis. I will talk about that

slightly later in the next slide. So, drag coefficient is enhanced. Inline forces will therefore, become negligible. Now cylinder will experience pressure which arises from this flow at one end and therefore, it also increases or creates tangential pressure which arises from friction between the fluid medium and the cylinder surface.

Now, the point of interest is here the cylinder surface, does not remain always smooth because of the marine growth deposits on the member. The moment the cylinder surface becomes rougher, it attracts more and more forces and therefore, the drag the initial coefficients keep on changing. Therefore, there is always the constant interaction between the structures even though the structure does not move. Now please understand the structure is or the member is fixed to the bottom. It offers reaction. This interaction interfaces the fluid medium. And that alters of the fluid flow actually. So, if you keep a member, may be fixed or floating, it will alter the fluid medium. The moment the fluid medium is altered it exerts forces. And it is a continuous process. And adding to this complexity the member is also moving, in terms of compliant systems, we are more secondary vibrations introduced a system which we call as oscillatory motion.

(Refer Slide Time: 10:23)



- Forces acting on the structures in fluid medium shall be classified as:
 - Drag (acting in-line with the direction of flow)
 - Lift (transverse to the direction of flow)
- Further, drag force can be classified as
 - Higher and smaller frequency components
 - These components will be functions of the geometry of the structure and flow conditions
- Lift forces contain oscillatory components with multiple frequencies

© NPTEL-IIT Madras

Therefore forces acting on the structures in the fluid medium shall be classified as 2 one is a drag and the lift forces. Drag is what we call in line force acting in the direction of

flow. Lift is the transverse to the direction of flow. There are 2 ways here the flow will be characterizing the flows us on the member. Further the drag force can be classified as, higher and smaller frequency components, which we call as premium bringing responses later, in the later part of experiment TLP for dynamic analysis. Therefore, both the frequency components are important higher as well as smaller. These components will be of course, functions of the geometry of the given system and the flow condition. Now here the design becomes important.

If you really wanted to make design interceptive force comparability, in that case the geometry of the system places a very important. So, since the drag force is component of the functions of the geometry, which is the design interception in the force calculations. If the geometry of the system is very large, if we invoked additional forces because of it is size or the design itself. Now interestingly, you will understand in any classical structural design, forces are estimated on the members. And the members are designed for the given forces. Whereas here you see the geometry induces forces on the system itself. Because of it is interaction with the media. Now lift forces which are transverse to the direction of flow, contain oscillatory components, with multiple frequencies, which also important. Now you have a member which is vibrated, or which is vibrating, or which is displaced in the direction of flow because of the drag effect. Which is also be vibrating, with multiple frequencies, in the direction normal to the direction of flow this is transverse motion.

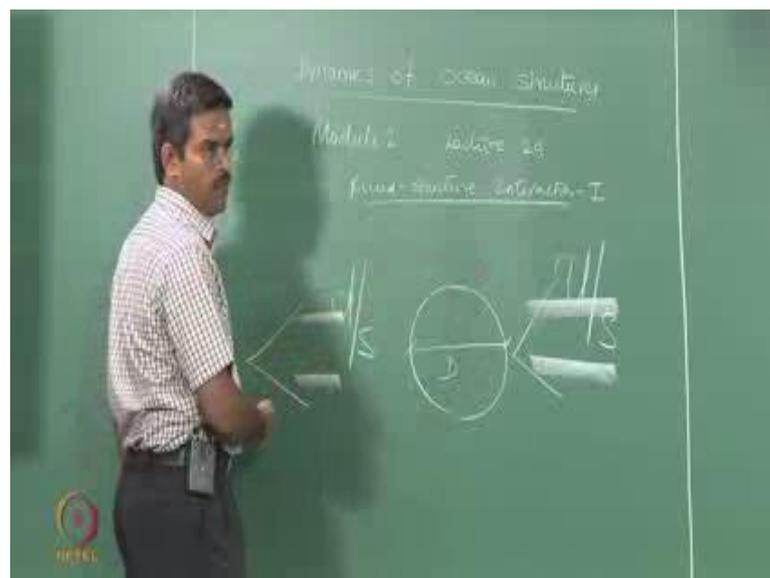
(Refer Slide Time: 12:09)

- On the downstream side,
 - Flow will return to its unaltered condition
 - This is due to fluid viscosity and damping
- Region of altered flow, directly behind the structure is called **WAKE REGION**
- ***This will cause asymmetric pressure distribution in the inline direction***
- ***Results in net horizontal force in inline direction***
- In the Wake regions,
 - There will be one-to-one relationship between the extent of wake region and restraint loads
 - Means that fluid-structure interaction in wake region is determinant
 - Frequency content of wake region is same as that of restraint loads

© NPTEL- IIT Madras

So, now the system or the member is interactive in both the components. Now, let us see what happens in the downstream side. One can understand or ask a question what we mean by a downstream side - let say I have a member.

(Refer Slide Time: 12:19)

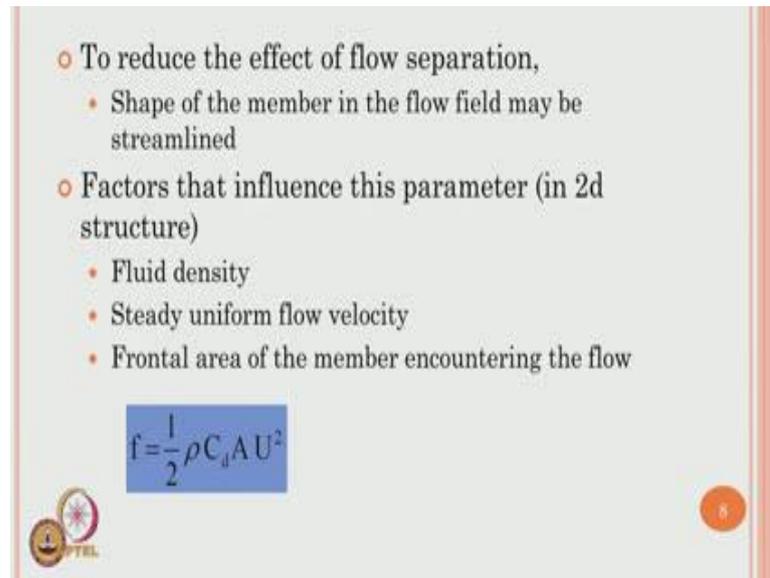


Let say we have the cylindrical member, maybe of a specific diameter d ; the wave is approaching the system, in it is direction. And the wave leaves the platform or the member in this manner. Here hypothetically considering a unidirectional wave of course, we know that the direction of wave is not in unidirectional, it is multidirectional hypothetical if a laminar flow, let say it is a unidirectional wave. We call this has upstream side this has downstream side, for a unidirectional flow.

Now, on the downstream side, flow will return to it is unaltered condition because it leaves the member and then becomes unaltered after specific distance. This is due to the fluid viscosity. And a damping effect present in the media. Now the region of altered flow directly behind the structure is what we call as wake region. This is very important because this will cause asymmetric pressure distribution, in the inline direction of forces. This results in net horizontal force in inline direction. In the wake regions, there will be one to one relationship between the extent of wake region and restraint loads which means that fluid structure interaction in the wake region, is becoming determinant we can calculate this very in the closed form solution.

Frequency content, of the wake region is said same as that of the restraint loads. So, on the other hand you see here, the frequency content of the force component remains and assimilates a similar value as that of the restraint loads. It means you will see that, the wake region invoked forces, or in resonance with that of the restraint loads. So, this induces though in a multiple frequency, a kind of an additional force on the wake region which is on the downstream side only for a specific sector. Beyond which the flow becomes unaltered back again. So, it is not only the flow direction important. In line is not only the transverse direction. It is also the downstream side sectors this disturbing the flow medium which causes forces on the member.

(Refer Slide Time: 14:21)



○ To reduce the effect of flow separation,

- Shape of the member in the flow field may be streamlined

○ Factors that influence this parameter (in 2d structure)

- Fluid density
- Steady uniform flow velocity
- Frontal area of the member encountering the flow

$$f = \frac{1}{2} \rho C_d A U^2$$

The slide also features a logo in the bottom left corner and a red circle with the number '8' in the bottom right corner.

Now, one can ask me a question. I want to reduce the effect of flow separation. What should I do to reduce the effect, of flow separation in design people use to adopt shape of the member is one of the important parameter, to streamlined flow. Now one asks me a question what are the factors which influences this parameter in a 2 dimensional frame. Fluid density, steady uniform flow velocity, and the frontal area of the member encountering the flow, which is given by this equation where rho of courses sea water density, series the drag coefficient, a is the frontal area of the member, and use the uniform steady uniform flow velocity.

(Refer Slide Time: 14:59)

FLOW REGIMES IN UNIFORM FLOW
Axis of cylinder normal to flow direction
Flow is without turbulence and boundary effects

Flow region	Re range	Flow condition	Forces on cylinder
Laminar & steady	0-40	No separation of flow	Drag forces occurring in the direction of flow
Sub-critical	40 – 5E05	Broken stream lines	Lift forces depends on Strouhal number Steady drag force+ smaller oscillating drag forces at double the frequency of lift force
Super-critical	5E05 – 7E05	Ill-defined vortices	Drag forces decrease rapidly Lift and drag forces will be seen at higher frequencies
Trans-critical	> 7E05	Vortices will be persistent Turbulent flow due to randomness in fluid viscosity	Similar to sub-critical range

 © NPTEL- IIT Madras

If you look at the flow regimes in uniform flow; let us consider axis of cylinder normal to the flow direction. Flow is without turbulence and boundary effects. Now when you talk about this hydro dynamics, people generally look at one important parameter, which we call as Reynolds number which is indicated as re here. Depending upon the range of the Reynolds number one classifies the flow conditions, and assimilates what are the kinds of forces which can come on the strain cylinder. For example, if the flow region remains laminar and steady, for which the verification is the Reynolds number should lie between 0 and 40, the flow condition shows there is no separation of flow.

If there is no separation of flow, the drag forces occurring in the direction of flow will be a predominant force, acting on a cylinder. On the other hand if the flow becomes sub critical. Which can be verified with Reynolds number ranging from 40 to 5×10^5 you will see that there are broken streamline generated in the flow field which induces lift forces. Which also of course, depends on Strouhal's number a steady drag force, plus small oscillating drag forces at double the frequency, of lift force will be now acting on the structure.

When the flow becomes super critical, where the Reynolds number ranges from 5×10^5 to 7×10^5 . Then it will develop what we call ill defined vertices now drag

forces decrease rapidly in the situation. Lift and drag forces will be seen at higher frequencies now. Now there is an extreme shift of the frequency, from the direction of regular to that of small frequency to that of double of the frequency of lift force to that of the higher frequency. Now one can see here depending upon the flow field, and flow condition, you will see that all components of the drag forces in lower and higher frequencies, and double the frequency are also present in the given system. If the flow becomes further trans critical where the Reynolds number exceeds 7×10^5 , in that case vertices will be present. The flow will come turbulent due to randomness in fluid viscosity, which results in sub critical range as that of you see here.

So, the lift forces we again created. So, depending upon the flow field mannerism, losses or induced in the member, when the member interferes with the flow field.

(Refer Slide Time: 17:10)

DRAG CRISIS

- At critical flow ($Re > 2E05$), drag coefficient decreases significantly.
- This also causes the WAKE to become narrow
- Also there is a decrease in pressure gradient
 - results in sharp drop in the drag coefficient
- This is called as DRAG CRISIS
- Drag Crisis is less for rough cylinders
 - Best way to remove drag crisis is allow roughness
- But greater the roughness, earlier is the separation of flow
- This will result in pressure difference between the U/S and D/S forces on the member
- Since the pressure distribution will not be symmetric about flow direction, this will generate additional forces in transverse direction (f_t)

$$f_d = \frac{1}{2} \rho C_d A U^2$$

There is something called drag crisis in the literature which is very important for drag dominant structures in offshore platforms. At critical flow for example, the Reynolds number exceeds 2×10^5 , then the drag coefficient decreases phenomenally. This also causes a wake to become very narrow.

When the wake becomes narrow this causes a decrease in pressure gradient. This decrease in pressure gradient, will results in sharp dropped in the drag coefficient. This is what we called as drag crisis. Now crisis is less for of course, rough cylinders therefore, as for the design people induced roughness in the cylinder surface. That is way you will say there are perforated members, or there are stampered members, or there are stripes placed on the members, which will induce surface roughness, which will decrease or the drag coefficient in the given system. Which is one of the design methodology for doing this, but greater the roughness the separation of the flow is earlier, when the flow get separated you will have the lift forces induce in the system automatically. So, one benefit creates one more demerit in the given system. So, this will result in pressure difference between upstream and downstream force in the member.

Since the pressure distribution is not symmetric about the flow direction, this will now generate additional forces what we call lift forces, which is given by the equation on the slide now. Where c_l it is a lift coefficient and of course, a rho and u or as same as defined in the previous slide

(Refer Slide Time: 18:38)

FORCES IN OSCILLATING CYLINDERS

- Inline force (per unit length) is the drag force (f_D)
- Inertia force on the cylinder is (f_I) $f_D = \frac{1}{2} \rho C_D D |u| u$
- Total force = $f_D + f_I + (\text{mass} \times \text{acc})$ $f_I = \frac{\pi}{4} D^2 \rho C_m \ddot{x}$

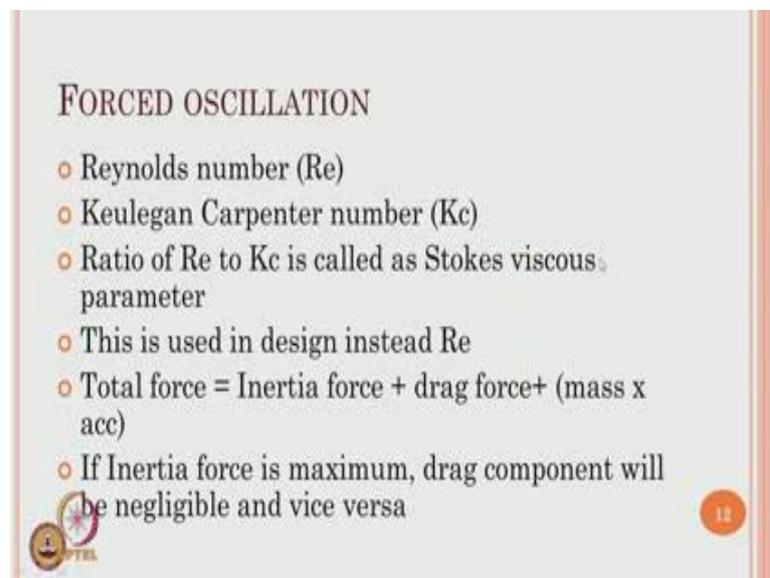
11

Now when you talk about oscillating cylinders, which I am not fix to the sea bed, there are 3 kinds of force generated one is what we call inline forces, what otherwise we call

as drag force given by the equation available here. Other is the inertia force and the cylinder given by the equation available here again f_I and f_D . Now the total force in a given system the right hand side of the equation of motion, the summation of the drag force per unit length of the system, plus inertia force per unit length of the system, plus of course, the mass of the platform into acceleration of the structural system itself.

Now, there are 2 components here. Please understand f_D and f_I have of course, the velocity and oscillation components which arise from the flow field and this acceleration components from the structural system because structure is now oscillating. So, there are 2 components inherently represent in the system. One because the structural motion itself, one because of the oscillatory motion induced, by the interference of the system on the flow field. So, now, it is very interesting to know all of us that, the f_D is dimension protected by having one of the system modular here. So, that it can also cause reverse effects.

(Refer Slide Time: 19:48)



FORCED OSCILLATION

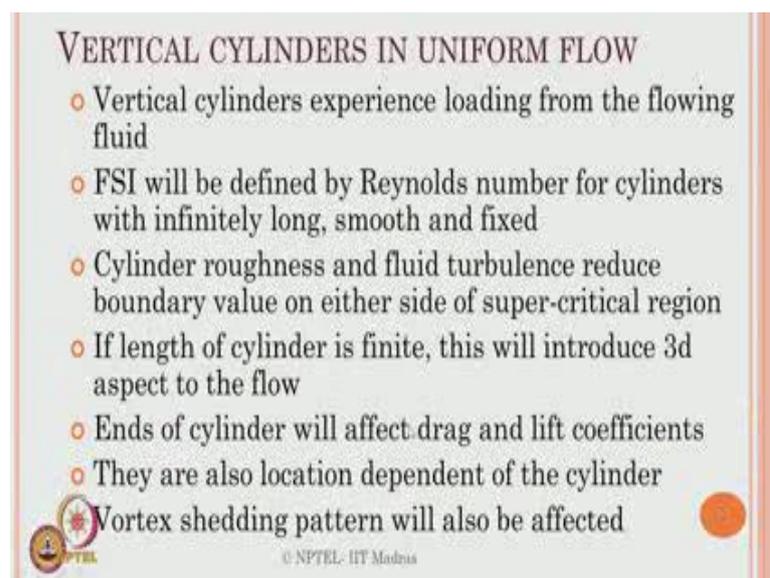
- Reynolds number (Re)
- Keulegan Carpenter number (Kc)
- Ratio of Re to Kc is called as Stokes viscous parameter
- This is used in design instead Re
- Total force = Inertia force + drag force + (mass x acc)
- If Inertia force is maximum, drag component will be negligible and vice versa

Now, we will talk about what we call forced oscillation which slowly depends on Reynolds number, and Keulegan carpenter number. But interestingly in design of offshore structures, people need the looks at this number independently, if you look at the

ratio of this number. Which you call Stokes viscous parameter. Which is ratio of re to kc this is actually used in the design in subsequent Reynolds number.

Now, the total force as you saw in the last slide, if the inertia force is arising from the system, plus drag force arising from the system, plus mass into acceleration, of the system itself. So, these 2 are from the medium. This is from the structural component. Of course, when the structural component does not move, this component becomes inefficient of course; this will be linearly present in the given system. Therefore, the right hand side of equation of motion, in the given dynamic system offshore structures will never be set to zero, if inertia of force is maximum interestingly, drag component will be negligible, and because vice versa that is what you seen in the research in the literature.

(Refer Slide Time: 20:47)



VERTICAL CYLINDERS IN UNIFORM FLOW

- Vertical cylinders experience loading from the flowing fluid
- FSI will be defined by Reynolds number for cylinders with infinitely long, smooth and fixed
- Cylinder roughness and fluid turbulence reduce boundary value on either side of super-critical region
- If length of cylinder is finite, this will introduce 3d aspect to the flow
- Ends of cylinder will affect drag and lift coefficients
- They are also location dependent of the cylinder
- Vortex shedding pattern will also be affected

© NPTEL- IIT Madras

Now, let us talk about vertical cylinders in uniform flow. Vertical cylinders experience different kind of loading, from the flow in fluid. Fluid structure interaction will be different by Reynolds number for cylinders, with infinitely long smooth, and fixed at the bottom. The cylinder roughness and fluid turbulence reduce boundary value on either side of the sub critical region. If of course, the length of cylinder is finite, this will introduce 3 dimensional aspects, to the flow field. Ends of the cylinder will of course, significant affect on the drag and lift coefficients. Because your considered to be

covered, in the original design. They are also location dependent of the cylinder. Therefore, the coordinate of the cylinder, or the coordinate of the cg of the cylinder, with respect to that of it is a boundary, because the important role to estimate these kinds of forces on the given system. Vortex shedding pattern will also be altered, depending upon the flow field surrounding the vertical cylinder.

(Refer Slide Time: 21:45)

REDUCED VELOCITY RANGE

Flow region	Reduced velocity	Vortex shedding	Types of vibration caused
I	1.7 to 2.3	Symmetric shedding	In-line oscillation only
II	2.8 to 3.2	Alternate shedding of vortices	Predominantly in-line vibrations Some transverse vibrations are also seen
III	4.5 to 8.0	Alternate shedding of vortices	Predominantly transverse vibration In-line vibrations are seen at frequency twice as that of the transverse vibration This is called <i>figure eight motion</i>

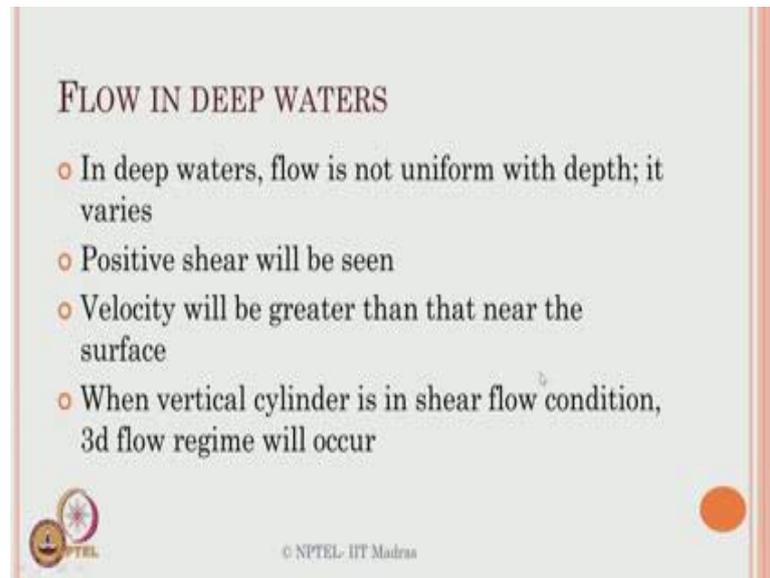
Hampshire, J.A. and Walker, D.H. 1987. Vortex excited response of large scale cylinders in shear flow. Proc. Sixth OMAE, Houston, TX, 2:139-143.
© NPTEL- IIT Madras

Like in the case of horizontal cylinders, reduced velocity can also be seen for different ranges, for different flow regions categorize cd 1 2 and 3, has given by Hampshire's and walker in 1987. The reduced velocity ranges from 1.7 to that of 8.0 which causes vortex shedding effect in the case of 1.7 to 2.3, where the flow regime is calculated as classical value 1 as given by Hampshire's and walker. The vortex shedding becomes symmetric, which will result in inline oscillations only. Please understand we will talk about design of a given system, we must understand what frequency we must approach, for calculating the response of the system.

So, when your flow region is only, with the reduced velocity of 1 to 1.7 to 2.3 which causes symmetric shedding, it will result only in inline oscillation. Where as in flow region 3, where the reduced velocity can go as high as 8.0 it causes alternate shedding of vertices which you will cause transverse vibration. And inline vibrations are seen at

frequency twice that of the transverse vibration which will result in what we called figure 8 motion of the structural system. So, here the stability of the system will be challenged.

(Refer Slide Time: 22:57)

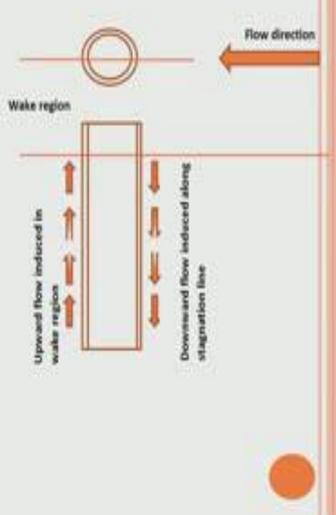


When we move on to shallow medium to deep waters, then the flow field slightly gets altered. In deep waters the flow is not uniform with the depth. It varies. We all know that because a water body is velocity in acceleration, keeps on challenging with respect to depth. It is maximum at the mean sea. And it is practically 0 when it goes through the sea bed.

Positive shear will be generated. Now interestingly shear is always a force, this try to divide the member in it is characterical strength. So, positive shear will be seen. I will show you the next slide how the shear is generated. Velocity will become greater than the near the surface, when the vertical cylinder is in shear flow condition, a 3d flow regime will now occur.

(Refer Slide Time: 23:36)

- Under positive shear, wake region experiences vertical upward flow
- Variation in stagnation pressure causes downward flow along the length
- The flow is SHEARED from upstream to downstream
- There is downward flow on the U/S side and upward on the D/S side

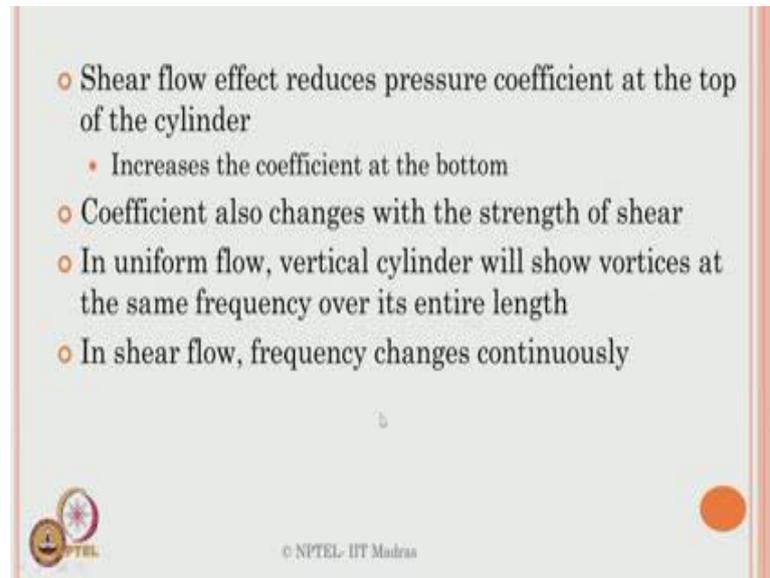


The diagram illustrates a cylinder in a shear flow field. The flow direction is indicated by a large arrow pointing to the left. A horizontal line represents the stagnation line. The wake region is shown as a rectangular area below the stagnation line. Vertical arrows indicate the induced flow directions: upward flow in the wake region and downward flow along the stagnation line. The flow is sheared from upstream to downstream.

© NPTEL- IIT Madras

Now, let us quickly see under positive shear the wake region. We all know the wake region is the flow pass the cylinder. If this is my cylinder, placed in the flow region if this is this my elevation, and this is my flow direction. We all know the wake region is on the flow pass cylinder here. Under positive shear the wake region experiences vertical upward flow. It will try to lift the member you see here. There is a downward flow induce along the stagnation line in the upstream side. Where as in the downstream side it is going to create an upward induce flow in the wake region.

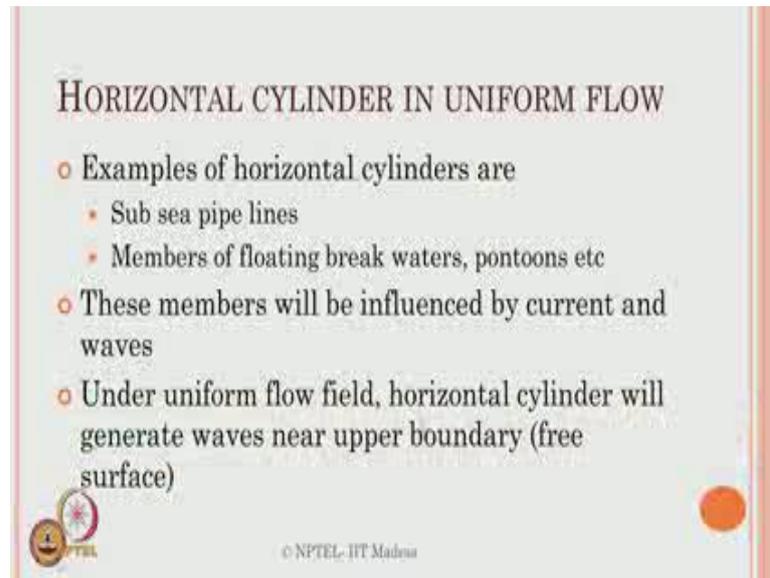
(Refer Slide Time: 24:27)



This will result in, what we call as the sheared motion between the upstream and downstream. There is down flow downward flow on the upstream side, and upward from the downstream side which will cause a shear effect on the given member in the wake region. This shear flow effect reduces the pressure coefficient at the top of the cylinder. And of course, increases the coefficient at the bottom. Usually it is vice versa, where this effect is absent coefficient also changes, with the strength of the shear value. In uniform flow the vertical cylinder will show vortices at the same frequency, over its entire length. It means the entire member will now become critical.

In shear flow frequencies changes continuously therefore, it can enter and exit the resonance domain of the member very frequently which results in what we call fatigue damage to the members.

(Refer Slide Time: 25:04)



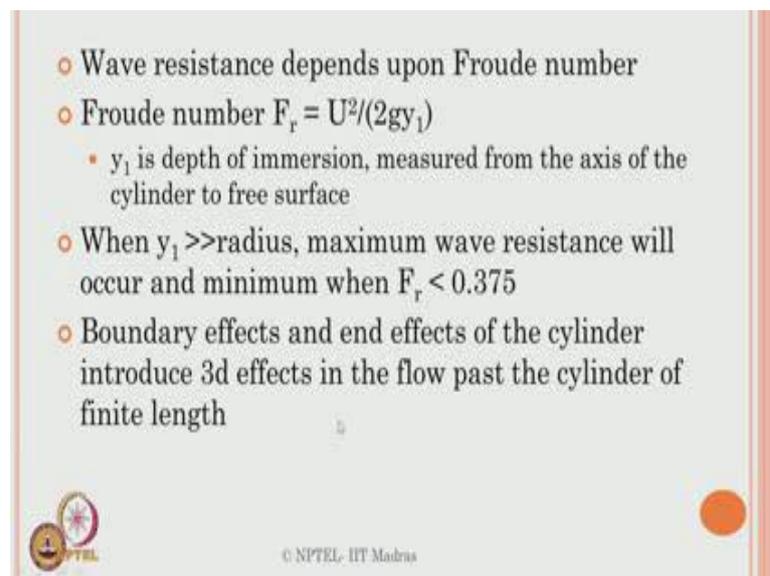
HORIZONTAL CYLINDER IN UNIFORM FLOW

- Examples of horizontal cylinders are
 - Sub sea pipe lines
 - Members of floating break waters, pontoons etc
- These members will be influenced by current and waves
- Under uniform flow field, horizontal cylinder will generate waves near upper boundary (free surface)

© NPTEL- IIT Madras

When we now place the cylinder horizontally for example, pontoon members in uniform flow, like subsea pipe lines pontoon members of floating break waters etcetera, in such cases these members will be influenced by the current and the waves together. Under uniform flow field horizontal cylinder will generate waves near the upper boundary, what we call as free surface effects.

(Refer Slide Time: 25:27)



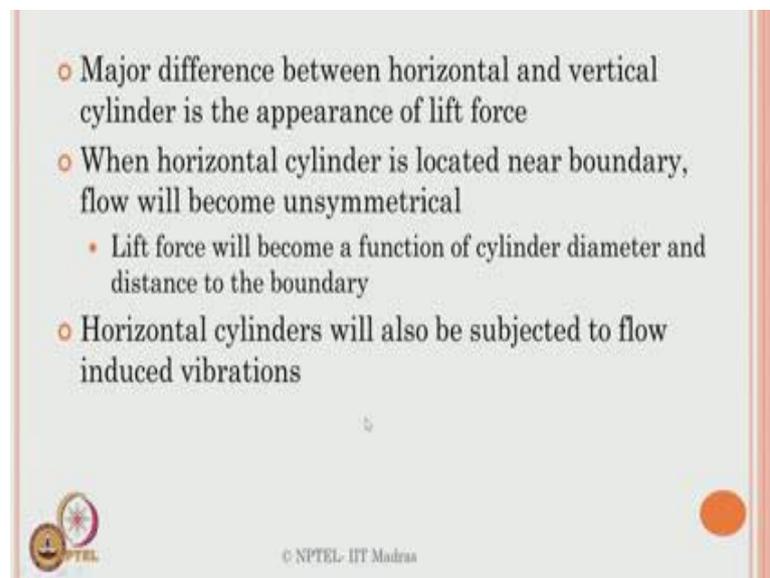
- Wave resistance depends upon Froude number
- Froude number $F_r = U^2/(2gy_1)$
 - y_1 is depth of immersion, measured from the axis of the cylinder to free surface
- When $y_1 \gg$ radius, maximum wave resistance will occur and minimum when $F_r < 0.375$
- Boundary effects and end effects of the cylinder introduce 3d effects in the flow past the cylinder of finite length

© NPTEL- IIT Madras

In such situation wave resistance, purely depends on the Froude's number as given in the equation here. Where y one is the depth of immersion of the member, measured from the axis of the cylinder, to the free surface. When this member or this value exceeds the radius of the member, the maximum wave resistance will occur and the minimum, when $f r$ is less than 0.375 as see in the literature.

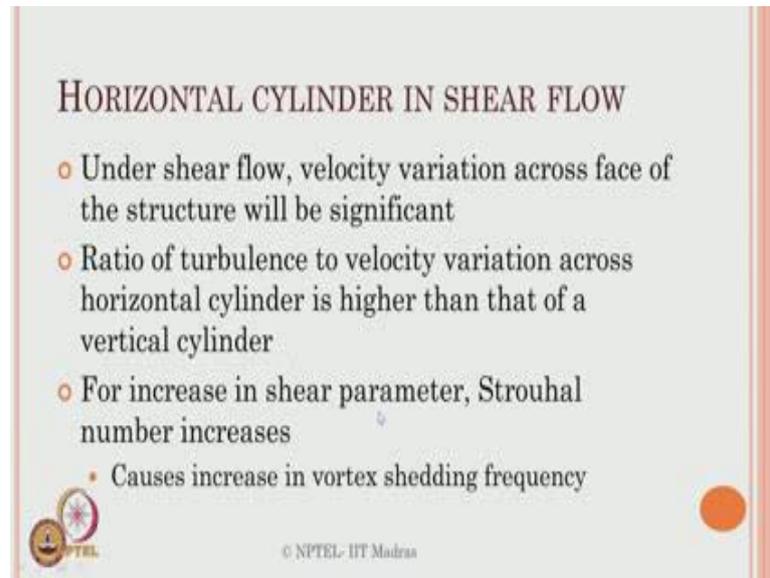
Now, the boundary effects and end effects of the cylinder introduce 3d effects in the flow past the cylinder, in the entire length of the member.

(Refer Slide Time: 25:59)



Which result in major difference between the horizontal and vertical cylinder is the appearance of lift force. When the horizontal cylinder is located near the boundary flow will become unsymmetric. Lift forces will become a function of cylinder diameter, and distance to that of the boundary from the axis of the member horizontal cylinders will also be subjected to flow induced vibrations which will cause secondary oscillation to the given system.

(Refer Slide Time: 26:23)



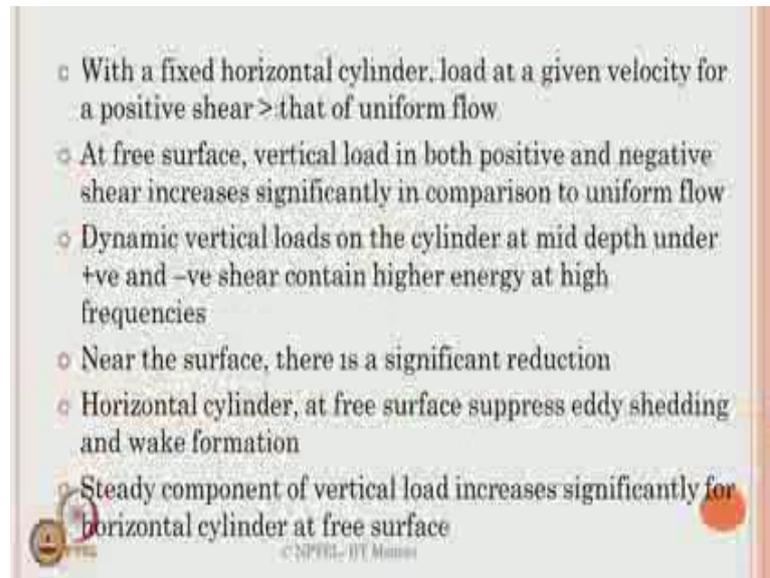
HORIZONTAL CYLINDER IN SHEAR FLOW

- Under shear flow, velocity variation across face of the structure will be significant
- Ratio of turbulence to velocity variation across horizontal cylinder is higher than that of a vertical cylinder
- For increase in shear parameter, Strouhal number increases
 - Causes increase in vortex shedding frequency

 © NPTEL- IIT Madras 

Horizontal cylinders, like vertical are also subjected to shear flow. Under shear flow the velocity variation across face of the structure will become significant. Ratio of turbulence to velocity variation across the cylinder is higher, than that of a vertical cylinder. So, therefore, now you see in a given system, like a TLP where the column members and pontoon members, one kind of member is having different kinds of shear flow compared to the other. It means the member has got disagreement in the pressure variation the upstream and downstream side whether the member is oriented vertically, or horizontally. For increase in shear parameter stochastic number therefore, increases.

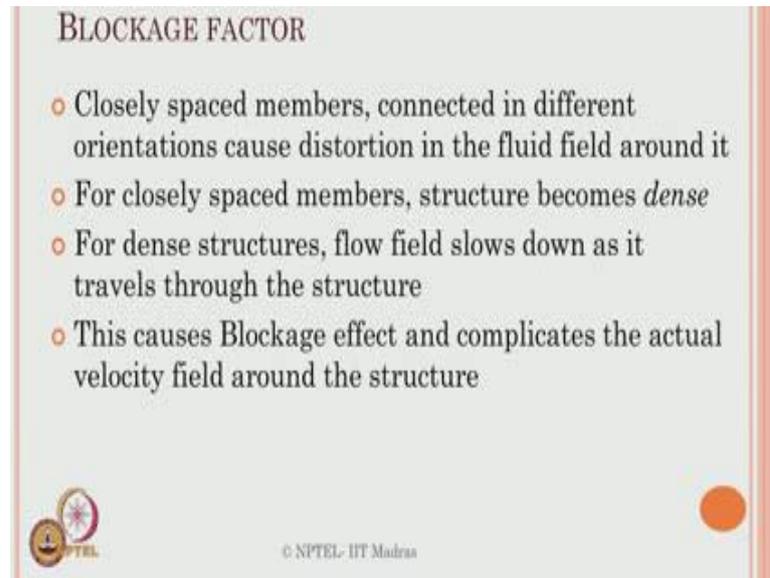
(Refer Slide Time: 27:12)



Now, when the stochastic number increases, this results in water shaded frequency, which will cause secondary vibration to the horizontal members. With a fixed horizontal cylinder, load at a given velocity for a positive shear, is generally seen more for a uniform flow. At a free surface the vertical load in both positive and negative shear increases significantly, in comparison to the uniform flow. The dynamic vertical loads on the cylinder at mid depth under positive and negative shear contain higher energy, at high frequencies. So, therefore, near the surface, this effect is significantly reduced. Horizontal cylinder therefore, at free surface suppresses eddy shedding effects, and wake formation is not seen for members, on the free surface. The steady component of the vertical load increases significantly, for the horizontal cylinder at free surface.

So, there are 2 types of components. One is the vertical component which is called the lift component, or is the horizontal component in and force called drag component. So, depending upon the orientation of the member, how do we place the member by one from the free surface effect, you will have the difference in these kind of floats are also created in the given member.

(Refer Slide Time: 28:10)



BLOCKAGE FACTOR

- Closely spaced members, connected in different orientations cause distortion in the fluid field around it
- For closely spaced members, structure becomes *dense*
- For dense structures, flow field slows down as it travels through the structure
- This causes Blockage effect and complicates the actual velocity field around the structure

© NPTEL- IIT Madras

More interestingly, we also something called blockage factor. Now with this blockage factor become significant when I got closely spaced members. When the closely spaced members connected in different orientation, this causes distortion in the fluid field around it. For closely spaced members the structure is considered to be dense for a dense structures literature, flow filed slows down as it travels through the structure. When the flow field slows down this is what we call as blockage effect. This complicates the actual velocity field around the structure. Velocity is reduced by the flows increases.

(Refer Slide Time: 28:44)

- Load on the structure increases due to this blockage

$$C_{BF} = \left[1 + \frac{\sum (C_D A)_i}{4A} \right]^{-1}$$

- Drag force is summed for each member in the dense structure
- In case of group of vertical cylinders present in the flow field, blockage factor is

$$C_{BF} = 0.25S/D \text{ (for } 0 < S/D < 4.0)$$
$$= 1.0 \text{ for } S/D = 4.0$$

Where S is c/c distance of the cylinder and D is diameter



© NPTEL- IIT Madras

Now, let us coming back to the point or the load on the structure increases due to this blockage effect which is given by this equation where C_{BF} is given by the blockage factor. Which is given by this equation are in case of group of vertical cylinders present in the flow filed you can also calculate C_{BF} using this relationship where s is a center distance of the cylinder, and where d is the diameter of the cylinder.

(Refer Slide Time: 29:11)

WAVE-STRUCTURE INTERACTION

- When waves past cylinder, it causes oscillating in-line force on the cylinder
- In addition, free surface also changes in case of a submerged cylinder
- Large structures placed in wave field alters incident waves in its vicinity
- If dimension of structure is large compared to wave length, flow remains attached to the structure



© NPTEL- IIT Madras

When we talk about wave structure interaction, is very important to know that, when the waves pass the cylinder it causes oscillating inline forces on the cylinder. In addition to that the free surface also changes in case of a submerged cylinder, because of the variables buoyancy or variables submergence effects, large structures place in wave field alters incident waves in its vicinity itself. The dimension of the structure is too large compared to the wave length, flow remains attached to the structure.

So, the flow remains attached means, when the flow is from left to right it has tendency to take back the structural along the same direction. Therefore, the resonance after the structure will go null and wide.

(Refer Slide Time: 29:51)



Of course the important components present in the structure in this lecture or given by these references are you see here which include some of the important components as we discussed in the design perspective given by me and Bhattacharya.

(Refer Slide Time: 29:58)

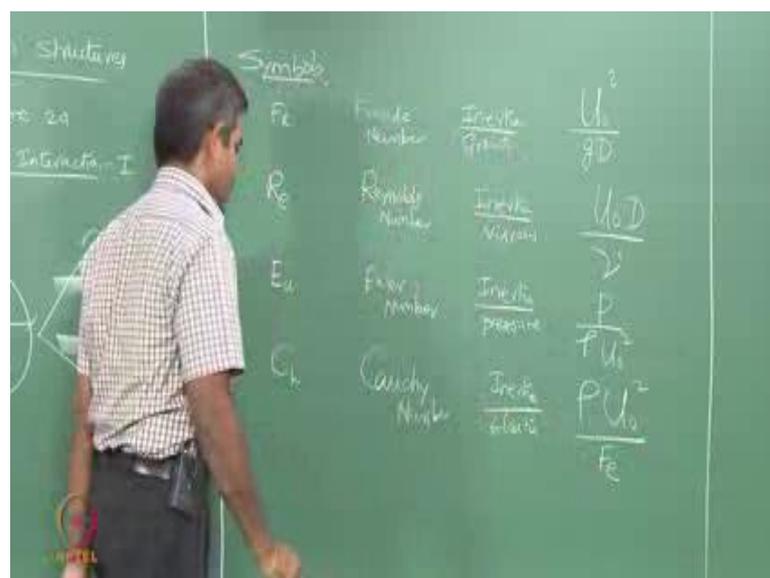
REFERENCES

- Patel, M. H., 1989. Dynamics of offshore structures: Butterworths, London.
- Sadehi, K. 1989. Design and analysis of Marine structures: Khajeh Nasirroddin Tsi University of Technology, Tehran, Iran.
- Sarpkaya, T. and Isaacson, M. 1981. Mechanics of Wave Forces on Offshore Structures: Van Nostrand Reinhold.
- Srinivasan Chandrasekaran and Subrata Kumar Bhattacharyya. 2012. Analysis and Design of Offshore Structures with illustrated examples. Human Resource Development Center for Offshore and Plant Engineering (HOPE Center), Changwon National University Press, Republic of Korea ISBN: 978-89-963915-5-5.
- Srinivasan Chandrasekaran. 2015. Dynamic analysis and design of offshore structures, Springer
- Srinivasan Chandasekaran. 2015. Advanced Marine Structures, CRC Press, Florida (in Press)

© NPTEL- IIT Madras

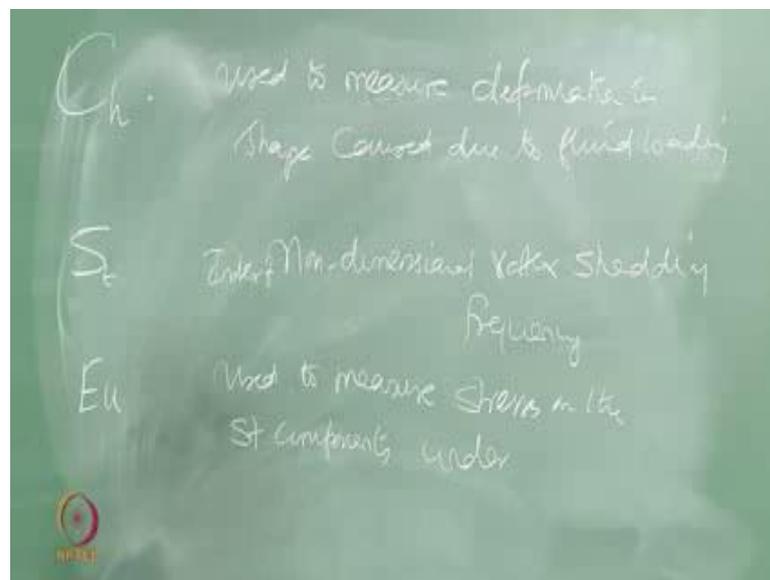
Given by me in 2 of the recent books in Springer and CRC press which will be now coming up, now, adding to having a summary of the forces ,will act on the cylinder will give us to important non dimensional numbers, and some of the important effects of this forces in the summary as a table now.

(Refer Slide Time: 30:23)



So, let us talk about some of the important symbols, and forces used in terms of relationships. Let us say Froude's number which is given by Fr which is ratio of inertia to gravity, the equation of course, of Fr we all know that u^2/gd , of course, the Reynolds number, given by Re you already seen in force the Reynolds number in a given system is the ratio of inertia to viscous force, given by the relationship $u d/\nu$ I will talk about these concepts slightly later. Next is important is an Euler number, given by Eu ratio of inertia to pressure.

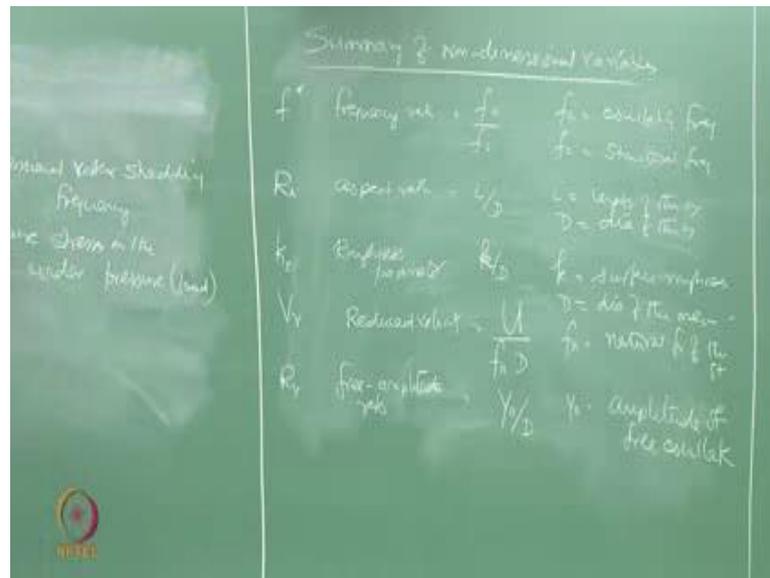
(Refer Slide Time: 32:29)



Cauchy number Ch inertia of to elastic Keulegan carpenter number $k c$. Drag to inertia, Strouhals number, given by St by u naught, where d diameter of the member, u naught flow velocity, out of this. Let us talk about these 3 numbers which are important for us. One is the Cauchy's number, or is Strouhals number. Euler's number talk about Cauchy's number, it is used to measure deformation in shape caused due to fluid in.

Strouhals number see index of non dimensional. Vortex shedding frequency Euler's number use to measure stresses on the structural components, under pressure load. In dynamic analysis of offshore platforms you normally come across, lot of non dimensional variants. Let us look at the summary of non dimensional variables.

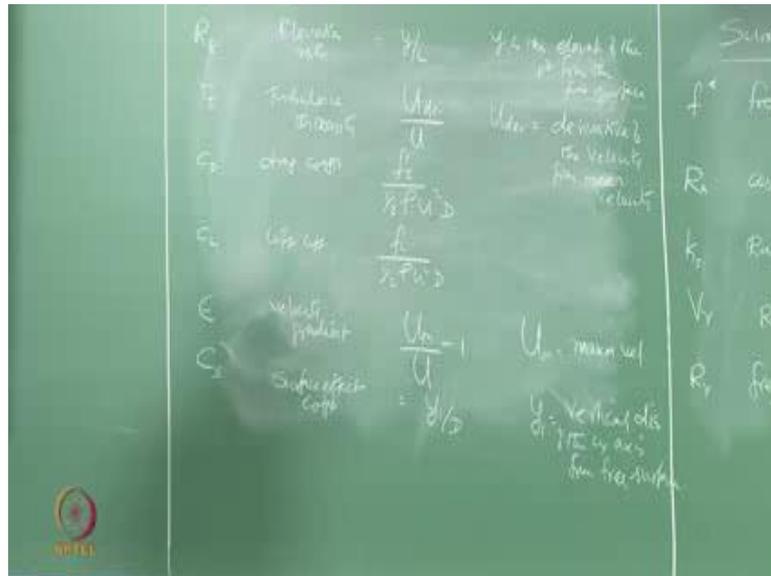
(Refer Slide Time: 35:58)



Which is important for us to understand because they will have it is an important role to play, frequency ratio, is actually oscillating frequency, to structural frequency. Or it is called aspect ratio which is the design parameter, which is R_a , which is L over, D L length of the cylinder if D dia of it is a geometric parameter. The other one is roughness parameter, which is given as k_s is given by k by D I think is small k plus male k is called surface roughness. And of course, D is the diameter. Of the something called reduced velocity which we talked about in the presentation recently which we call as v which is given by u by f and D . Where f_n is a natural frequency of the structure R_y called free amplitude ratio, which is given by Y naught by D . Amplitude of free oscillation you are; obviously, see in most of the cases in these non dimensional variables are connecting the behavior of the flow field to that of the diameter.

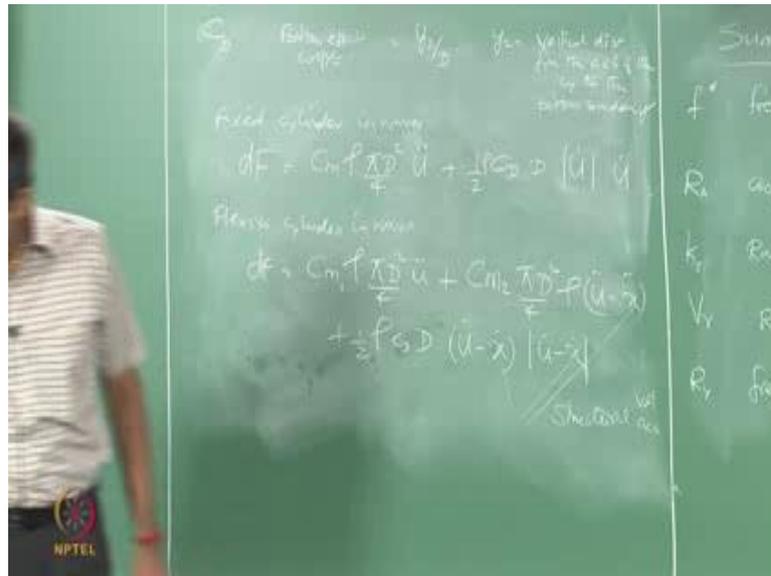
Let say they are called design parameters also, because most of them connecting the diameter, you see elevation ratio.

(Refer Slide Time: 39:31)



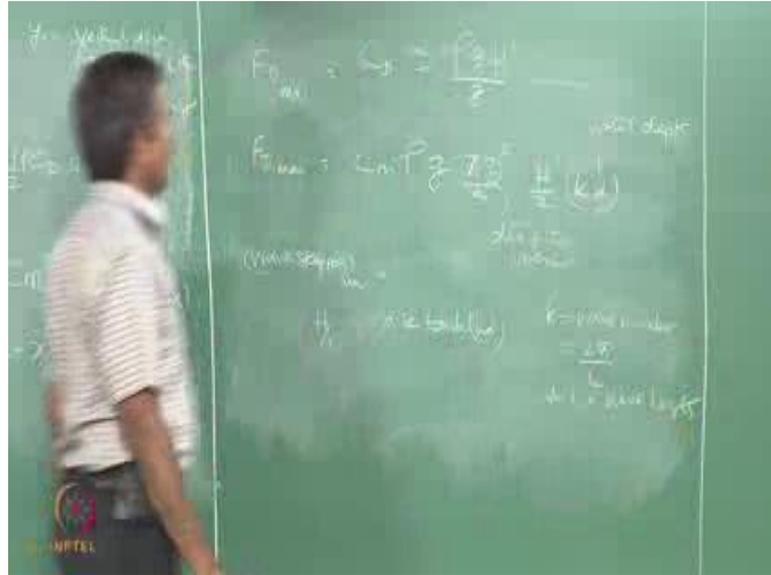
Which is re of course, this way confused a Reynolds number - y by l where y is the elevation of the point from the free surface. Turbulence intensity, u develops by u by u , where u developed is a derivative of the velocity, from μ velocity. Drag coefficient f_d by half flow u square d we already saw the equation earlier. Lift coefficient f_l by half ρ u square d . Velocity gradient indicated by ϵ , which is u_m by u minus one where u_m is a maximum velocity. Surface effect coefficient which is given as C_s it is given by y l by d , where y l is the vertical distance of the cylinder axis from the free surface.

(Refer Slide Time: 42:51)



Bottom effect coefficient c_b which is given by y^2 by d where y is the vertical distance from the cylinder axis to the bottom boundary. This was a summary of this lecture. For fixed cylinder in waves will develop for experienced forces which are given by $d f$ the elemental force on unit increment length of the member. $C_m \rho \pi d^2$ square by 4. Flexible cylinders in waves will experience forces where the term v or let us say x . Please make it to x the term x relates to structural components may be velocity and acceleration respectively whereas the term u refers to water particle. Now design one as interested to know what is the maximum force coming on the member $f D_{max}$ which is $c_d d$ relate.

(Refer Slide Time: 45:57)



Similarly, inertia of force maximum expressed by the member, the small d indicates water depth of course, the capital d indicates diameter of the member. Maximum wave stiffness it is given by h by l . $0.14 \tan$ hyperbolic kb now of course, k is a wave number. Which is given by 2π by l where, l is the wave length and so on. So, this will be a thumb rule for you just glossary of terms looking at different non dimensional variables, which are often seen in the right hand side of the equation motion we are solved we for the different kinds of forces. People used these terminologies or one must know how to compute them, and what is the influence on different kinds of numbers the variations and the participation when a fluid medium, is interfered by a member depending upon it is orientation. Vertical horizontal fixed floating etcetera. Just now we have seen in this lecture. So, this lecture summarizes the fluid structure and wave structure interaction, in terms of brief understanding, how the forces can be estimated on the members.

Thank you.