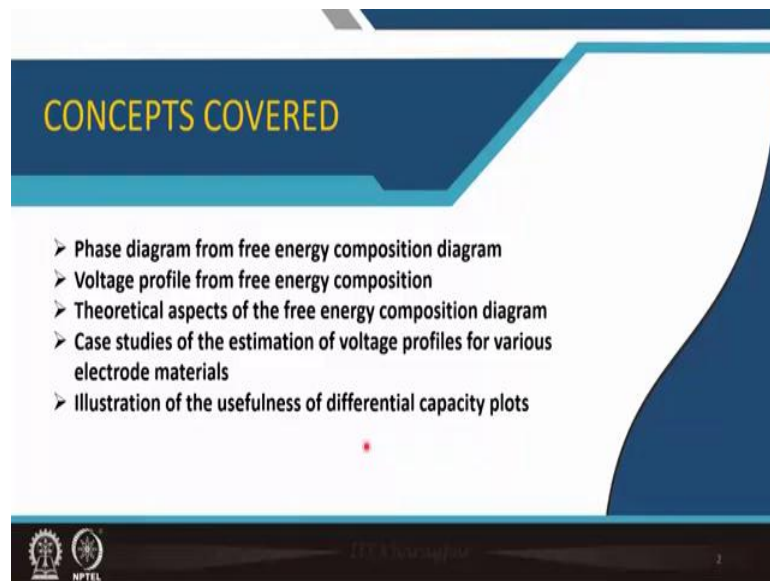


**Electrochemical Energy Storage**  
**Prof. Subhasish Basu Majumder**  
**Department of Materials Science Centre**  
**Indian Institute of Technology, Kharagpur**

**Module - 03**  
**Lithium batteries**  
**Lecture - 13**  
**Differences of Voltage Profiles between Intercalation Materials, Alloys, and Conversion Materials**

Welcome to my course, Electrochemical Storage. And, this is module number 3 on Lithium Batteries and this is lecture 13. So, here I will show, what is the genesis of various types of voltage profile between different types of electrode material? So, far we have talked about intercalation material, alloy conversion materials. So, do you get similar type of pattern voltage versus lithium composition or you get different types of pattern and what are the genesis of that?

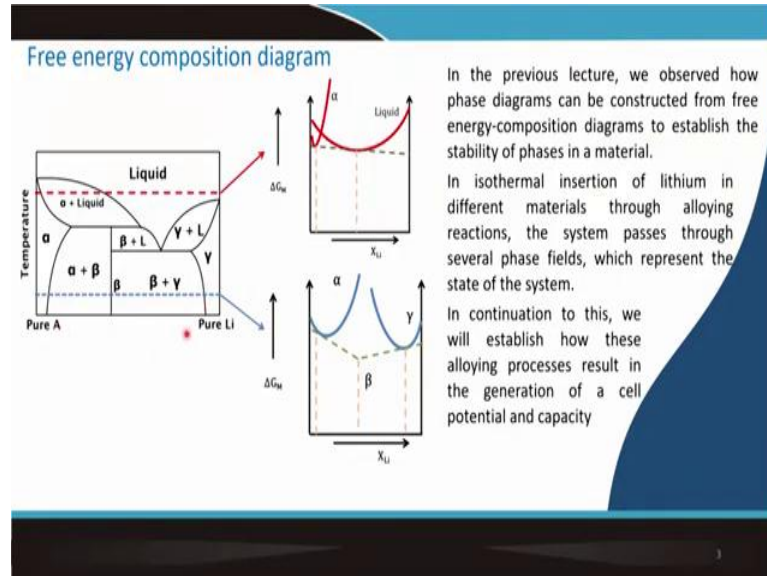
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So, we will again talk about the phase diagram from the free energy composition how they are related. Then, we will estimate the voltage profile from free energy composition diagram, then we will explain the theoretical aspects of the free energy composition diagram, then we will have certain case studies for the estimation of voltage profile for various electrode materials.

And, finally, the differential capacity plot, which I showed in one of the my earlier lectures differential capacity plot the illustration of their usefulness, that I will cover.

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So, we will start with again the free energy composition diagram and the phase diagram of a binary component system, one is a pure component which is defined as A, and another side is pure lithium. So, sometimes in some of my slide instead of A I put X and the right hand side is always lithium. So, lithium content increases here and it forms various types of solid solution and mixture of solid solution.

So, if you go by this particular red line, then you end up with the free energy versus lithium diagram like this, which already I explained. And, if you go by this blue line then this kind of free energy versus composition diagram one can easily identify. So, in the previous lecture we observed how this phase diagram can be constructed from this free energy composition diagrams, we explained the genesis of this.

In isothermal in intersection of lithium in different materials through alloying reactions, the system passes through several phase field as you can see which represent the state of the system. So, in continuation to this we will now establish, how this alloying process, result in the generation of cell potential and capacity?

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**Relationship between voltage profile and free energy-composition diagram**

In the earlier lecture, we saw how lithium can alloy with a pure element X to form Li-X binary alloys, wherein the lithium is distributed homogeneously in the alloy. This type of alloying reaction is called solid-solution alloying reaction, wherein the reaction is a single phase reaction.

Free energy change due to mixing of a component with another to form a solution =  $G_i$  (in solution) -  $G_i^0$  (pure) =  $RT \ln(a_i)$   
 Suppose  $n_x$  moles of X is mixed with  $n_{Li}$  moles of lithium to form binary Li-X alloy,  
 Free energy before mixing =  $n_x G_x^0 + n_{Li} G_{Li}^0$   
 Free energy after mixing =  $n_x G_x + n_{Li} G_{Li}$   
 Free Energy change due to mixing =  $n_x (G_x - G_x^0) + n_{Li} (G_{Li} - G_{Li}^0)$   
 =  $n_x \Delta G_x + n_{Li} \Delta G_{Li}$

So, in earlier lecture, we saw how lithium can alloy with pure element X. So, as I told in here, I have defined the left part as X to form a lithium X binary alloys, wherein the lithium distributed homogeneously in the alloy. So, remember the diagram that I showed where lithium and this X component and sometimes I define as a. So, they are homogeneously distributed.

This type of alloying reaction is called a solid solution alloying reactions, wherein this reaction is a single phase reaction. So, the free energy change due to mixing of the component with another to form a solution. So, I can have this  $G_i$  in solution minus this  $G_i$  in pure case and that is equated with  $RT \ln$  into the activity. So, you suppose that  $n_x$  mole of this X component is mixed with  $n_{Li}$  moles of lithium to form this binary alloy. So, I am defining this composition.

So, the free energy before mixing you can write with this equation, where  $n_x$  and  $G_x$  and  $n_{Li}$  and  $G_{Li}$  is already defined. And, after mixing this is  $n_x G_x + n_{Li} G_{Li}$ , so, this is after mixing. So, free energy change due to mixing is just this minus this. So, we will work out with  $n_x \Delta G_x + n_{Li} \Delta G_{Li}$  simple calculations.

$$\text{Free energy before mixing} = n_x G_x^0 + n_{Li} G_{Li}^0$$

$$\text{Free energy after mixing} = n_x G_x + n_{Li} G_{Li}$$

$$\text{Free Energy change due to mixing} = n_x (G_x - G_x^0) + n_{Li} (G_{Li} - G_{Li}^0)$$

$$= n_x \Delta G_x + n_{Li} \Delta G_{Li}$$

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Molar free energy change of mix =  $X_x RT \ln(a_x) + X_{Li} RT \ln(a_{Li})$

If we consider an ideal solution, where  $a = X$  (activity coefficient = 1),  
then  $\Delta G_M^{id} = RT (X_x \ln(X_x) + X_{Li} \ln(X_{Li}))$

In the figure shown above, we can plot the free energy of mixing against composition and obtain the following curve: (You can try to plot this function in Excel or any other graphing software)

Molar free energy of mixing for Li =  $\Delta G_{Li} = \Delta G_M^{id} + X_x \frac{\partial \Delta G_M^{id}}{\partial X_{Li}} = \mu_{Li}^{\infty}$  (this relation is derived later)

From the construction in the previous slide, we can see that  $\mu_{Li}^{\infty}$  is the intercept which the tangent drawn at a composition  $X_{Li}$  makes with the line  $X_{Li} = 1$ .

Now, molar free energy change of the mix. So, that is n mole and divided by the total mole. So, that is the molar fraction. So, that  $RT \ln a_i$  sorry  $a_x$  plus mole fraction of Li  $RT \ln$  activity of Li. So, if you consider an ideal solution, where this activity coefficient is 1, then this free energy mixing is  $RT$  into  $X_x \ln X_x$  plus  $X_{Li} \ln X_{Li}$ .

$$\text{Molar free energy change of mix} = X_x RT \ln(a_x) + X_{Li} RT \ln(a_{Li})$$

If we consider an ideal solution, where  $a = X$  (activity coefficient = 1),

$$\text{then } \Delta G_M^{id} = RT (X_x \ln(X_x) + X_{Li} \ln(X_{Li}))$$

So, the figure that is shown here, we can plot the free energy of mixing against the composition of lithium usually with the lithium composition it is shown. And, you can get the plot of the free energy of mixing against the composition.

So, I will ask you to try this plot try to plot this function in excel or origin or any other graphical software to actually see that you are getting this kind of shape. So, one can also estimate, that this molar free energy of mixing for lithium, this is the free energy change of the mixing in the ideal case plus  $X_X$ , then del of this del  $G_M$  ideal by del  $X_{Li}$ .

$$\text{Molar free energy of mixing for Li} = \Delta G_{Li} = \Delta G_M^{id} + X_X \frac{\partial \Delta G_M^{id}}{\partial X_{Li}} = \mu_{Li}^{\infty}$$

And, this is nothing, but the chemical potential of lithium. So, this relation I have derived it for you initially I thought that you can derive it yourself, but later I thought that let us derive it. So, this is shown as this tangent, you can see that at this particular composition if you take and you draw a tangent here, then this molar chemical potential of lithium and this  $X$  component you can easily identify.

So, for the construction in the previous slide, we can see that this is the intercept which is the tangent drawn at a composition makes with the line  $X_{Li}$  equal to 1. So, with this if you draw the tangent, which is passing through this lithium composition you get the chemical potential for lithium.

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$G$  (molar free energy after mixing) =  $X_X G_X + X_{Li} G_{Li}$

$dG = X_X dG_X + X_{Li} dG_{Li} + G_X dX_X + G_{Li} dX_{Li}$

From Gibbs Duhem Eqn.  $X_X dG_X + X_{Li} dG_{Li} = 0$  Hence  $dG = G_X dX_X + G_{Li} dX_{Li}$

Now  $1 - X_{Li} = X_X$ ; hence  $dX_X = -dX_{Li}$   $dG = G_X (-dX_{Li}) + G_{Li} dX_{Li}$

$dG = (G_{Li} - G_X) dX_{Li}$  Therefore,  $G_{Li} = G_X + \frac{\partial G}{\partial X_{Li}}$

Multiplying both sides by  $X_X$ ,  $X_X G_{Li} = X_X G_X + X_X \frac{\partial G}{\partial X_{Li}}$  Adding  $X_{Li} G_{Li}$  both sides

$X_{Li} G_{Li} + X_X G_{Li} = X_{Li} G_{Li} + X_X G_X + X_X \frac{\partial G}{\partial X_{Li}}$

$G_{Li}(x) = G_{mix} + X_X \frac{\partial G}{\partial X_{Li}}$   $\Delta G_{Li} = \Delta G_{mix} + X_X \frac{\Delta \Delta G_{mix}}{\Delta X_{Li}}$  This is  $\mu_{Li}^{\infty}$

So, let us try to solve this. So,  $G$  is the molar free energy after mixing so, you can write this relation and again this will all be subscript, this will all be subscript, then differentiate this relation.

$$G \text{ (molar free energy after mixing)} = X_x G_x + X_{Li} G_{Li}$$

$$dG = X_x dG_x + X_{Li} dG_{Li} + G_x dX_x + G_{Li} dX_{Li}$$

Now earlier I proved the Gibbs Duhem equation. So, this part the rate part is Gibbs Duhem equation and that is equal to 0. So, you have dG equal to this plus this.

$$X_x dG_x + X_{Li} dG_{Li} = 0$$

$$dG = G_x dX_x + G_{Li} dX_{Li}$$

Now, from the consideration that X mole of lithium and X mole of X, that is basically the total mixture. So, this relation is valid. So, I can always differentiate this and then you put the value of dX<sub>x</sub> here, replace it with minus dX<sub>Li</sub>. So, your dG is free energy of lithium minus free energy of x component into dX<sub>Li</sub>

$$dG = (G_{Li} - G_x)dX_{Li}$$

$$G_{Li} = G_x + \frac{\partial G}{\partial X_{Li}}$$

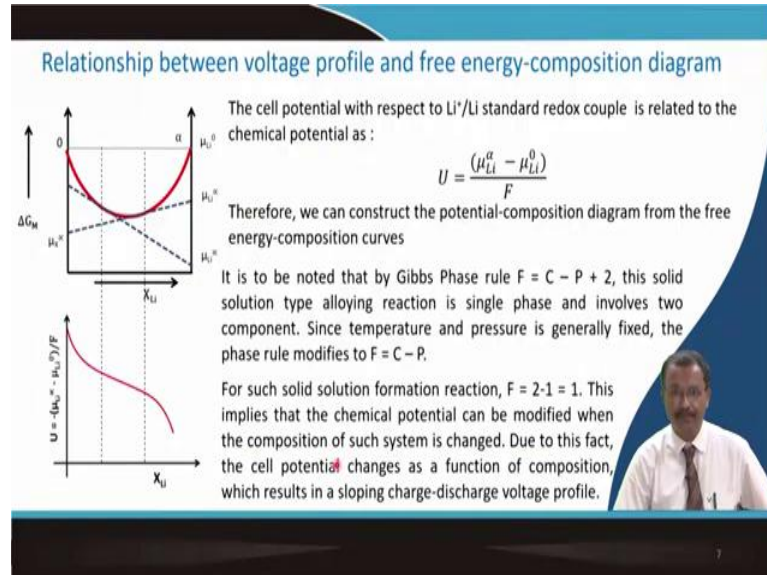
So, therefore, your G<sub>Li</sub> is G<sub>x</sub> plus the partial differentiation of del G with respect to del x lithium. So, in this equation if you multiply both side with X<sub>x</sub>, then we get X<sub>x</sub> of G<sub>Li</sub> and here also X<sub>x</sub> of G<sub>x</sub> and X<sub>x</sub> of del G by del X<sub>Li</sub>. Then, you add this term X<sub>Li</sub> G<sub>Li</sub> in both side.

$$X_{Li}G_{Li} + X_x G_{Li} = X_{Li}G_{Li} + X_x G_x + X_x \frac{\partial G}{\partial X_{Li}}$$

So, you get this relation. So, that leads you to G<sub>Li</sub> of x is G<sub>mix</sub> plus X<sub>x</sub> of del G by del X<sub>Li</sub>. So, differentiation of this will give you this relation, which is nothing, but the tangent and that gives the chemical potential for lithium in the solid solution phase.

$$G_{Li} = G_{mix} + X_x \frac{\partial G_{mix}}{\partial X_{Li}}$$

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So, the cell potential with respect to lithium redox couple is standard redox couple is related to chemical potential and this already we have talked about several times this relation. So, your lithium is here for this particular composition if you take, then draw a tangent here. And, for pure lithium it is in this state, in this state.

$$U = \frac{(\mu_{Li}^{\alpha} - \mu_{Li}^0)}{F}$$

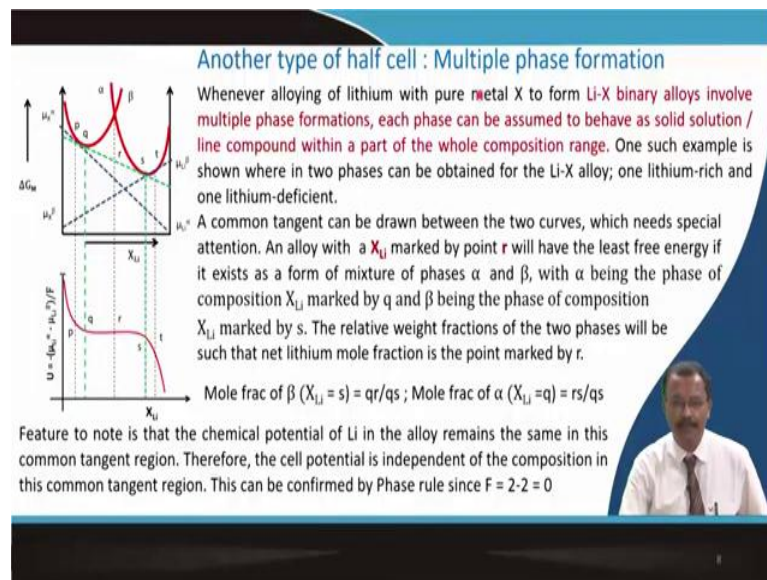
So, the difference you can get, this difference you can get. And, similarly if you take this composition, here your lithium potential is here and this one is here again. So, this value if you take the lithium potential value with respect to this two composition, then the voltage certainly will get affected.

So, we can see it diagrammatically here. So, here the difference is this and this. So, this difference is relatively small as compared to this difference, which is much larger. So, when lithium composition is low, then it is in this side the higher potential side, when it is relatively higher, then the potential drops down.

So, it get it gets a s type of curve. So, you can apply that Gibbs phase rule which says the degree of freedom is number of component minus phase plus 2. So, this is solid solution type alloying reaction in single phase and involves two component. Since the temperature and pressure is generally constant, then the phase rule modifies to degree of freedom is nothing, but C minus P.

So, here the component is 2 and phase is 1. So, only 1 degree of freedom is there so; that means, it implies that the chemical potential can be modified, when the composition of this system is changed. Due to this fact the cell potential change as a function of composition which results this sloping charge discharge profile. So, this is as simple as that.

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Now, another type of half cell where you use lithium and in particular alloy, which is having multiphase formation. So, two different phase formation you can see. So, whenever alloying of lithium with pure metal X to form Li X type of binary alloy, that involved multiple phase formation, you remember the phase diagram you have alpha, then alpha plus beta and beta. So, there are several phases. So, each phase can assume to behave like a solid solution or a line compound within the part of the whole composition range, you remember the phase diagram which I showed earlier.

So, one such example is shown here in two phase can be obtained in lithium X alloy; one is lithium rich and another one is lithium deficient. Pictographically that also I have



shown in one of my earlier slides, you remember with small circles colored in different one is red and another one was green. So, when you draw a common tangent between 2 curves which needs some kind of special attention.

So, an alloy with X Li marked by the point r. So, that is in between here. That will have the least free energy, if it exists as a form of mixture of two phases marked as alpha and beta from the phase diagram. With being alpha is the phase of composition X Li marked by q so, this part. And, beta is a phase of composition X Li marked by s so, this. So, the relative weight fraction of this two phase is such that, the lithium mole fraction is the point which is marked by r, that is from the standard phase diagram and applying the lever rule in it.

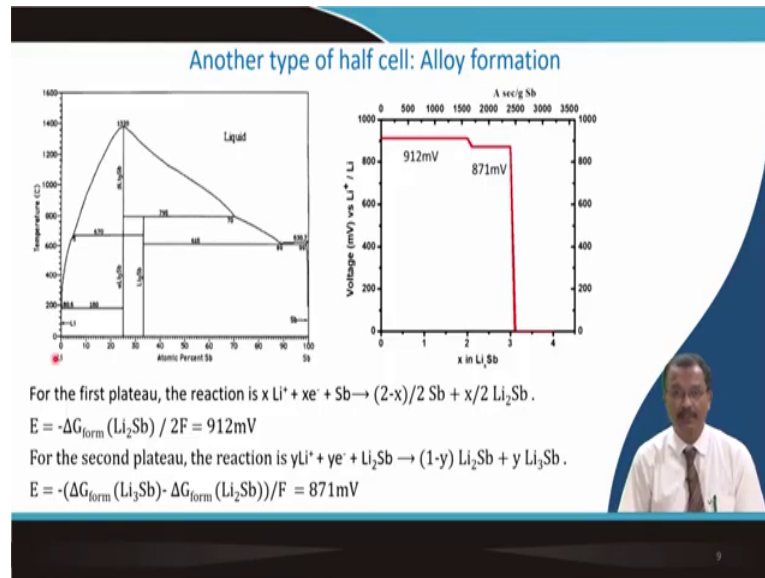
So, the mole fraction of beta is given by  $qr$  this divided by the whole  $qs$ . And, mole fraction of alpha which is in this side, that given by  $rs$  divided by the whole  $qs$ . Now, the feature that is worth noting is that the chemical potential of lithium in the alloys, remains the same in the common tangent right.

So, the chemical potential will remain same here along with the common tangent. Therefore, the cell potential will not be dramatically affected. So, the cell potential is independent of this composition. So, in the common tangent region you can see, that the cell potential will remain constant and if you apply phase rule here also.

So, component and phase this  $2 - 2$  is equal to 0 so; that means, you cannot change anything. So, the with the composition of lithium your voltage will remain same, but when you have the single phase solid solution and as I showed earlier, you will have this kind of drop.

So, this is typical for multiphase for the alloy which forms a multiphase. And, therefore, you can correlate the free energy composition diagram with the voltage, that is resulting from it.

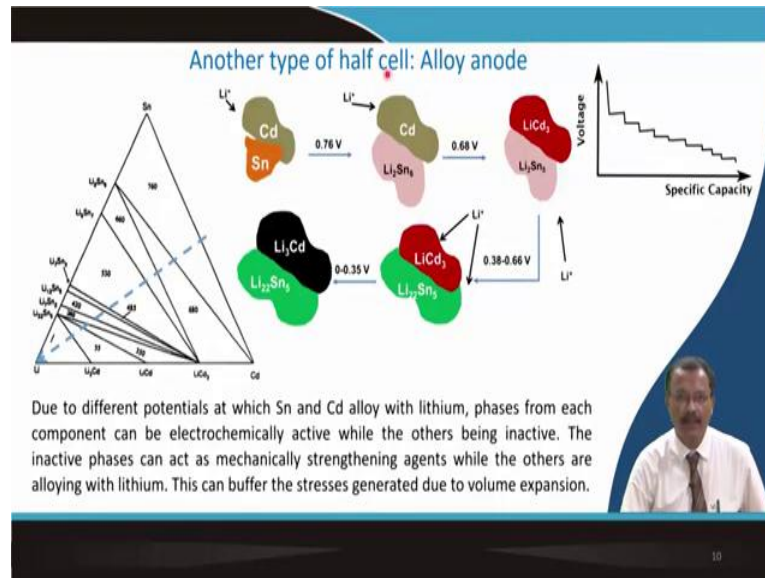
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So, another type of half cell where this alloy formation take place, this also I have defined in antimony and lithium case. So, here the first plateau, the reaction is lithium reacts with antimony to form  $\text{Li}_2\text{Sb}$  which is given by this line. And, the value of E that is minus del G formation of  $\text{Li}_2\text{Sb}$  by 2F, because 2 electrons are involved. And, this is can be calculated I will show it, that it will be about 912 milli volt around that. And, for the second plateau whatever you are getting again it is a two phase mixture this is given by this relation.

So, the formation free energy is for  $\text{Li}_3\text{Sb}$  minus formation of  $\text{Li}_2\text{Sb}$ . So, that is this 2 component  $\text{Li}_2\text{Sb}$  and  $\text{Li}_3\text{Sb}$ . So, the voltage is 871 milli volt and this kind of step profile you will get in this type of alloy.

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Another example can be shown where it is a ternary kind of phase system. So, this is already I have explained how it forms. So, if you have lithium alloying across this line, then for tin cadmium this binary alloy lithium will progressively form various types of alloying initially it will start to form with this cadmium will remain like this. And, then another voltage which you can calculate back this two will form.

And, then this two phases will form which is apparent from this phase diagram and for this type of multiple alloying reaction for this solid solution this inter metallics, you will get this kind of step profile. So, due to different potential at which tin and cadmium alloy with lithium phase's form from each component can be electrochemically active while others are being inactive.

The inactive phase can act as a mechanically strengthening agent as I have told that when lithium comes in, then the volume expansion can be buffered by this metallic element. While the other phase that alloy with lithium. So, the presence of this metal eventually at this stage at least, it can reduce the volume expansion and buffer the stress which is generated.

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**Lithium-graphite alloy formation**

In alloy systems, the simplest model of forming a solution is the ideal solution model wherein  $\Delta G_M^{id} = X_A RT \ln(X_A) + X_B RT \ln(X_B)$

However in real solutions, the free energy is never equal to the ideal case due to variations in activity with composition. Another popular solution model is the **Regular Solution Model**, wherein  $\Delta G_m^{reg} = \Delta G_M^{id} + G_{XS}$  with  $G_{XS} = \Omega X_A X_B$

Such a free energy change term also results in two phase reactions, which is prevalent in case of graphite.

$\Omega$  represents a sort of penalty term for mixing that depends on components involved.

In such regular solutions, the activity coefficient is related as :  $\ln \gamma_X = CX_B^2$  and  $\ln \gamma_B = CX_A^2$

In case of lithium graphite alloy formation the simplest model that forming a solution that is the ideal solution that I described this relation this is a bit modified. So, in real solution the free energy is never equal to the ideal case due to the variation in the activity with the composition.

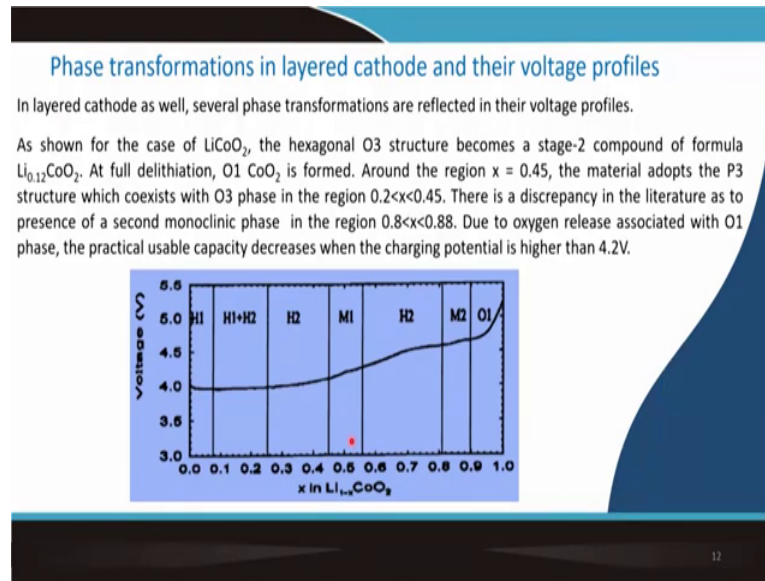
So, when carbon and lithium they form this kind of alloy, then it is not considered as a ideal solution. So, one can use another popular solution model, which is termed as regular solution model, where along with this you have another term which is added. And, this is actually defined by omega into molar fraction of X and lithium X in this case is carbon.

$$\Delta G_m^{reg} = \Delta G_M^{id} + G_{XS} \text{ with } G_{XS} = \Omega X_C X_{Li}$$

So, such free energy change is also results a two phase reaction, which is prevalent in case of graphite as well. So, delta that eventually some kind of penalty term for mixing, that depends on the component which is involved. So, here also the step type of reaction that takes place and as I told the value of S in the last lecture starting from 432 and 1, and this alloying takes place. And, progressively the voltage step kind of voltage profile that you get, the lowest 1 is here.

So, in such regular solution the activity coefficient that can be defined by this relation, I will try to frame a assignment problem to better illustrate this. So,  $\ln \gamma_X$  this is  $\frac{CX}{Li}$  whole square and  $\ln \gamma_{Li}$  is  $\frac{CX}{A}$  whole square. So, this will be illustrated in the assignment problem set. So, the voltage correspond to this is actually you can see in this view graph as well.

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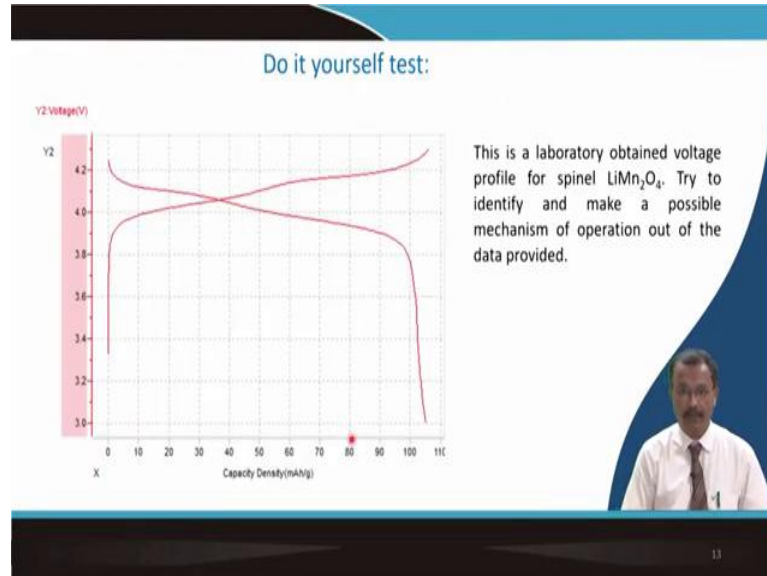
So, phase transformation already I defined in case of lithium cobalt oxide several phase transformation that is possible. So, in case lithium cobalt oxide hexagonal O3 structure becomes a stage-2 compound with formula of typical formula of Li 0.12 Cobalt Oxide. At full delithiation, O1 type of cobalt oxide formed. Around the region x equal to 0.45 the material adopts a P3 structure.

All these I have explained in my last lecture, which coexist with O3 phase in this region when the lithium content is in between 0.45 to 0.2. Although there is a discrepancy in the literature, the presence of a second monoclinic phase in the region typically here. So, here oxygen start to release and that is associated with O1 phase, the practicable usable capacity when charging potential is higher than 4.2, then this oxygen evolution cannot be avoided.

So, we will limit the lithium extraction from lithium cobalt oxide, because of this structural complicity up to 0.5 up to 5.5 lithium. So, according to the Faraday law, if you estimate the capacity we will find this estimated capacity of lithium cobalt oxide is

pretty large, but actually it is halved because you are not able to extract the whole lithium out of it.

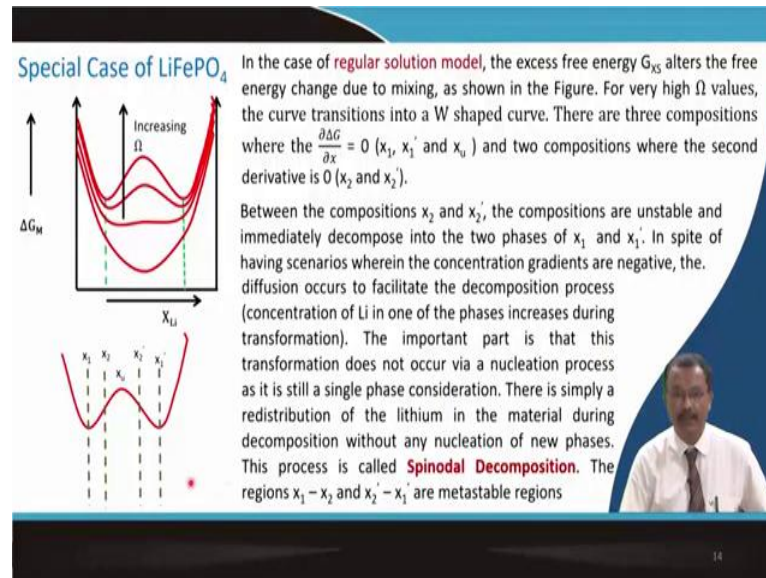
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So, I have given a typical charge discharge profile of lithium manganese oxide a well known spinel. So, you can try to identify based on the lecture that we had so far we are discussing, you can try to identify and make a possible mechanism of operations. So, what is happening during charging up to this? What is happening in this plateau and during discharge what is happening here, and what is also happening here and what is happening here?

So, based on the discussion I leave it on you to provide an explanation and come up with your answer.

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A special case is lithium iron phosphate where this regular solution model is prevalent then the ideal solution model. We talked about the excess free energy term this alters the free energy change due to mixing so, as shown in the figure. So, this term when this omega term increases, then from regular this type of bold type of free energy diagram as you increase this delta term, you see that slowly it goes to a 2 minima condition.

So, for very high omega value, the curve transition to a W type of curve. So, there are three composition where this partial derivative of free energy with x is 0; one is x 1 another one is x 1 dash and here another one is x 1 and the third one is x of lithium which is here. So, these three cases you have this partial derivative is 0, and, two compositions, where the second derivative is 0. So, this two composition this x 2 and this x 2 dash, which is in between this slope, it is 0.

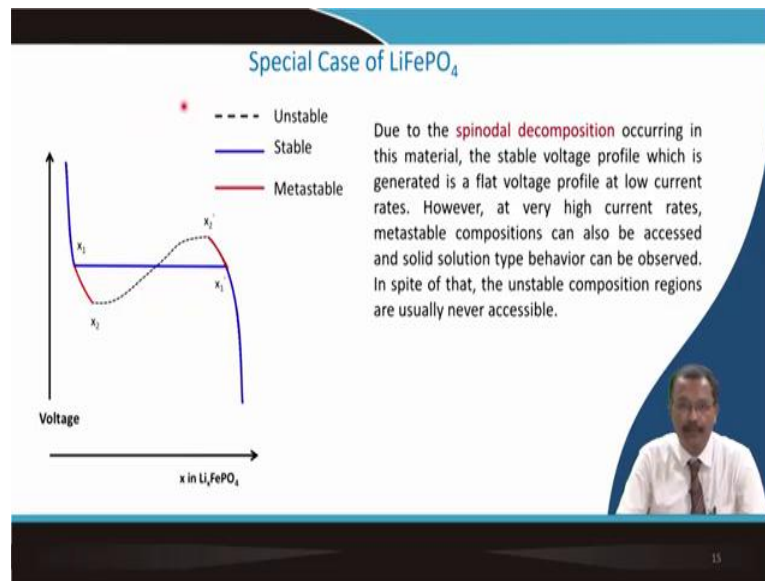
So, between the composition of x 2 and x 2 dash this composition are unstable and immediately decomposes into x 1 and x 1 dash phase. So, in spite of having the scenario, where in the concentration gradient is negative, the diffusion occurs to facilitate, the decomposition process. So, the composition or rather concentration of lithium in one of the phase increase during this transformation.

The important part is that the transformation does not occur via a nucleation process. So, that is very important, as it is still a single phase consideration. So, there is a I remember in case of the alloy we talked about say antimony and tin. So, this nucleates and then

grows, but this is not a two phase system. So, there is simply a redistribution of lithium in the material during the decomposition, without any nucleation of a new phase. So, this particular process that is known as spinodal decomposition, which some of the metallurgists may be familiar of.

And, the region  $x_1$  to  $x_2$  and  $x_2$  dash  $x_2$  dash to  $x_1$ , they are actually meta stable regions.

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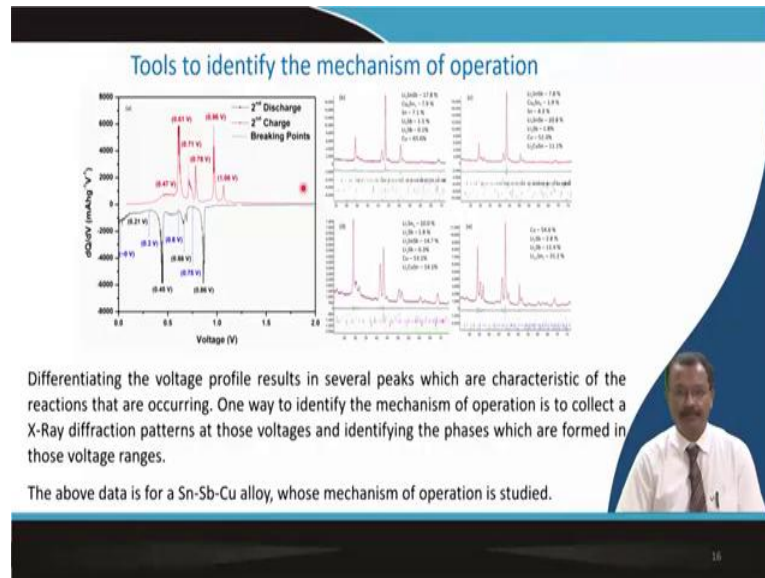


So, now if you have the voltage profile due to this spinodal decomposition, the stable voltage profile is generated whatever is generated is this flat voltage profile. And, this is occurring at a relatively lower current of discharge. However, when a very high current rates are applied, then this metastable region, that can also be accessed and solid solution type behavior you can see where this sloping profile you can see here right. In spite of that the unstable composition regions; usually they are never accessed except for a very high current probably it will look like this.

But, like the two phase type of alloy always you get a flat profile like this one, not the one that has been shown here except for a very high current. So, the mechanism of the this two things are very different, but the profile is more or less similar in nature.



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Now, once you get the discharge profile like, the 1 like this and this. In order to better understand this profile what we do, we do a differential capacity plot, where we plot the  $dQ/Dv$ , where  $Q$  is the charge the capacity with respect to voltage. And, plot it with the respective voltage to get this kind of  $dQ/Dv$  curve. So, particularly for the step reaction for alloy materials, we do this thing. And, wherever the oxidation and reduction takes place, this is this gives a very sharp because there is a change in slope.

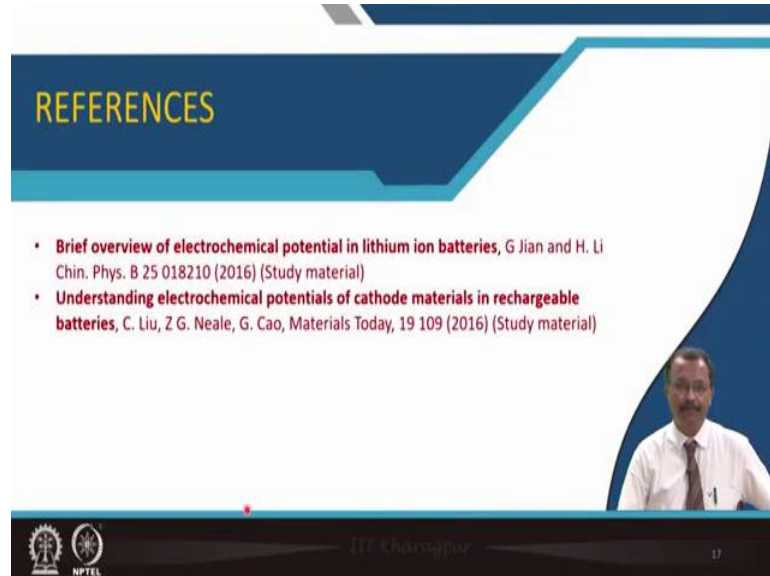
So, there is a very sharp peak oxidation and reduction peak, that is observed. And, schematically it is shown for various compositions through the X-Ray diffraction studies. And each of this particular phase is identified, whether indeed during oxidation and reduction this kind of alloys are forming you can stop your measurement right at that point and then this electrode you can do the X-Ray diffraction to identify the phase. And, then indeed whether it is forming or not that can be identified and at which voltage it is forming that also can be identified.

So, this is a very useful technique of differentiating the voltage profile they result several peaks which are characteristics of the reaction that is occurring. So, one way to identify the mechanism of operation is to collect the X-Ray diffraction pattern at those voltages to identify this phase, which are formed in those voltage ranges.

So, this above data, this data is our own data on a system tin antimony copper. So, tin and antimony they indeed form alloy with lithium and copper acts as a buffered layer.

So, the stress basically is buffered through the dislocation movement along the slip plane. So, that is I have cited as one of the examples.

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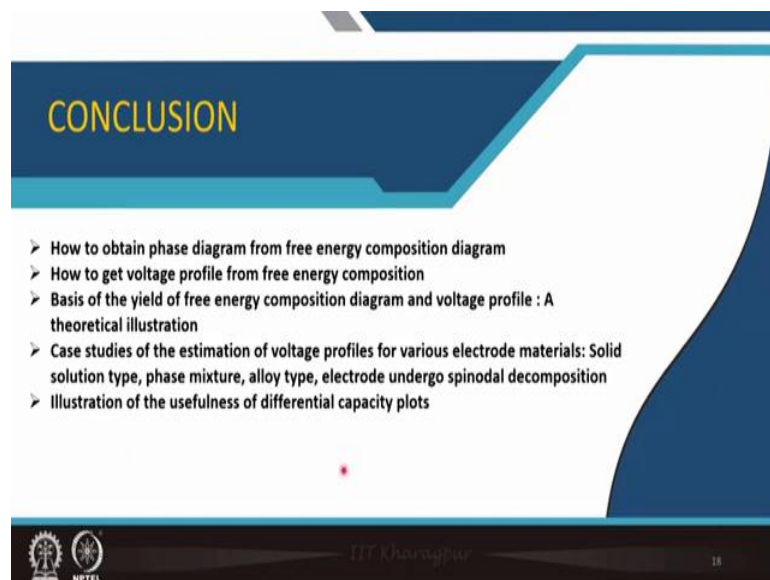
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So, again there are two important publications that is the study material for this part of the work. And, this these two papers will give you a more insight about the topic covered.

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**CONCLUSION**

- How to obtain phase diagram from free energy composition diagram
- How to get voltage profile from free energy composition
- Basis of the yield of free energy composition diagram and voltage profile : A theoretical illustration
- Case studies of the estimation of voltage profiles for various electrode materials: Solid solution type, phase mixture, alloy type, electrode undergo spinodal decomposition
- Illustration of the usefulness of differential capacity plots

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So, wherein this particular lecture I have demonstrated that how to obtain the phase diagram from free energy composition diagram, then how to get the voltage profile from

free energy composition? Then basis of the yield of free energy composition diagram and voltage profile; a theoretical illustration has been done. And, I will suggest you to do a line by line calculation, to estimate the straight line, the tangential line that gives you, the estimation of  $\mu$  of lithium.

And, then point by point analysis of the free energy; versus composition diagram to see the exact voltage profile in case of a single phase, or at least binary phase electrode material. And, then a case study of estimation of voltage profile of various electrode material, we will talk more on it during the case study the remaining 2 lectures, solid solution type, phase mixture type, alloy type, and the electrode which undergoes a spinodal decomposition.

And, finally, the illustration of the usefulness of differential capacity plot.

Thank you for your attention.