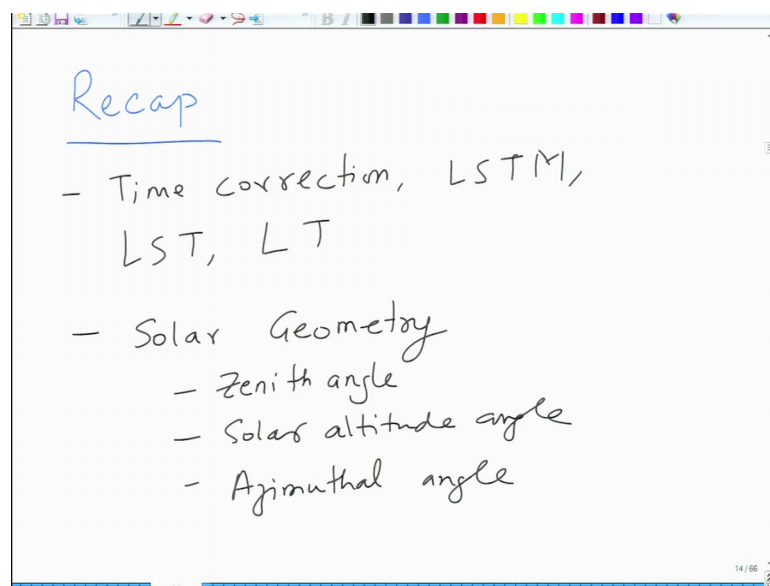


Solar Photovoltaics: Principles, Technologies and Materials
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Lecture - 06
Solar Radiation Measurements

So, welcome to this lecture number-6 of Solar Photovoltaics course Principles Technologies and Materials. So, we will just do a quick recap of lecture number 5.

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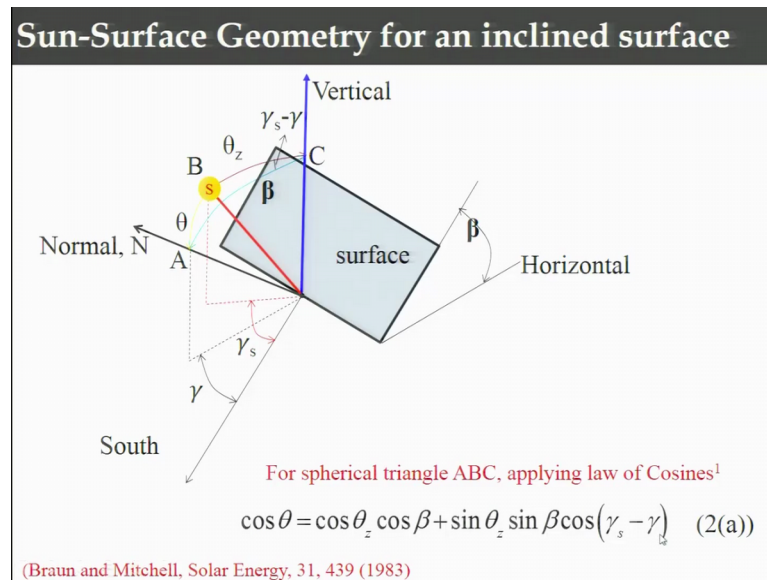


In the previous lecture, we looked at essentially methods to correct for time. So, we looked at time correction, concept of LSTM local solar time, local time; so, basically how to correct for actual solar rule and the one which is predicted by your watches. So, and these are nothing, but geometrical corrections based on the location where you are the longitude, latitude, because the whole country is by clock is in one time zone, whereas the actual time at a given location may be different from what is given in you in your watch and that is because of geometrical corrections in because the line.

For example, the longitude of Kanpur is different from longitude in Calcutta. So, obviously, sun would actually rise earlier in Calcutta than Kanpur. So, although Calcutta and Kanpur, the 12 o clock in clocks will be at the same time, but the noon will happen at the different time so you need to correct for these discrepancies.

And we also looked at we also initial we also got initiated into solar geometry. So, we looked at things like zenith angle, we looked at solar altitude angle, we looked at various azimuthal angles and so on and so forth.

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So, we were we when we finished we were just looking at the geometrical relationship for a inclined body, so let me now switch over to the PPT. So, we were looking at this kind of geometry, where a surface that you want to use is inclined to the horizontal. And this makes an angle beta with respect to the horizontal. And the arrow pointing this direction is the south arrow and so south in this direction, and north obviously would be opposite of that. And this is the vertical to the horizontal and this is the sun.

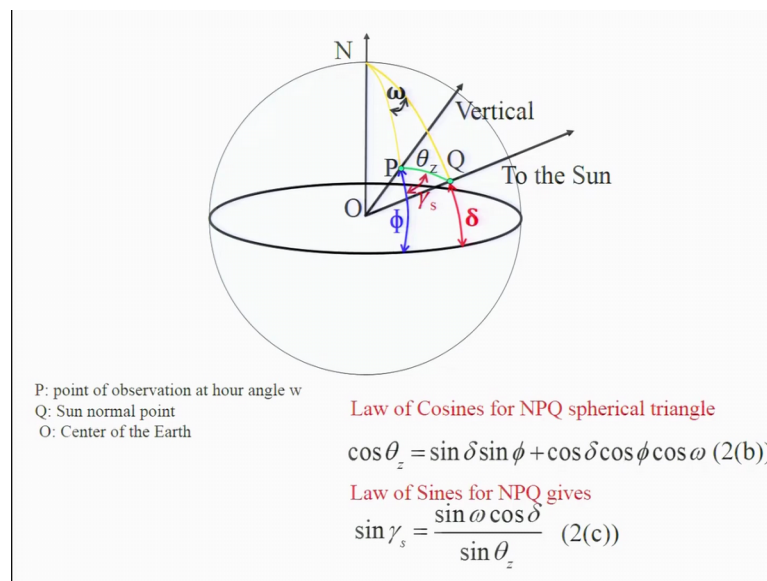
So, sun ray is coming at certain angle to the surface. So, sun ray comes at certain angle to the horizontal, but since the surface that beta angle with respect to horizontal you need to make that correction in the angle for sun ray on the horizontal surface, so that beta have to be subtracted from the total overall angle. And then so this is the angle between the vertical and the sun which is the zenith angle, then we have normal to the surface, so not the there is a difference between the vertical and the normal to the surface.

Vertical is vertical to the horizontal whereas normal to the surface, N is the normal to the surface. So, which means the angle between normal and vertical is going to be beta right, because the angle between the surface and horizontal is beta. So, these two angles are going to be beta. And then you can also define some other angles the angle between sun

ray and the normal is theta. Angle between the projection of sun ray on the horizontal and its angle with the south is called as gamma; s, solar azimuthal angle the angle of surfaces normal project its projection on the horizontal and its angle with the south is called as gamma.

So, based on variety of these angles you can define this sole triangle ABC. And by the equivalence of in the geometry you can see that angle between BC and AB will be gamma s minus gamma, because this angle is gamma s minus gamma so that angle will become gamma s minus gamma. So, if you do now, so we will not get into details of trigonometry, but if you apply the law of cosine, you will get cos theta relation as cos theta is equal to cos theta z cos beta plus sin theta z sin beta into cos gamma s minus cos minus gamma.

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Now, you can represent the whole thing in a different way in this kind of with respect to earth being is a sphere, and sun being somewhere around it; so, which is sort of a legitimate design. And again using the equal law of the cosine, you can determine cos theta z will be equal to sin theta sin phi plus cos theta cos phi cos omega.

So, you can see that in the previous one we had relation for cos theta now it is a relation for cos theta z it is a zenith angle. And law of sin s will again give you relation, so the idea is to get two expressions where you can you require a minimum number of angles to

make predictions. So, law of sines will give you $\sin \omega \gamma$ which is the solar azimuthal angle in terms of ω , δ and θ_z .

You see some of these angles are easy to work out. For examples, zenith angle, it can be found out easily. And δ is the declination angle and ω is the hour angle. So, these three angles are easy to decipher, whereas solar angle azimuthal angle is not decipher. So, you would like to replace the quantities which are not given easily by the quantities which are available to us, so that is why these three expressions are come into being.

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Solar Radiation Geometry

For a vertical surface, $\beta=90^\circ$

$$\cos \theta = \sin \phi \cos \delta \cos \gamma \cos \omega - \cos \phi \sin \delta \cos \gamma \sin \beta + \cos \delta \sin \gamma \sin \omega \dots \dots \dots (3)$$

For a horizontal surface, $\beta=0^\circ$

$$\cos \theta = \sin \phi \sin \delta + \cos \phi \cos \delta \cos \omega \dots \dots \dots (4)$$

In this case, the angle θ is zenith angle θ_z

Now, you just simplify these expressions; so, for a vertical surface with β is equal to 90 degree. This simplifies to $\cos \theta$ simplifies to $\sin \phi \sin \delta \cos \gamma \cos \omega \cos \phi \cos \delta \cos \gamma \sin \beta$ and another term in including $\cos \delta \sin \gamma$ and $\sin \omega$. So, you can see here ϕ is the position dependent term; δ is the declination angle which is day dependent term. γ is the angle of surface normal with respect to north south, so that you may have to define; ω is the hour angle.

So, these three these this angle, so ϕ , δ and ω are easily known, whereas γ you would know because of orientation of surface ok, so that also could be known. Similarly, for a horizontal surface, this even simplifies further, because then β becomes equal to 90 degree sorry 0 degree; so, all the $\cos \cos \sin \beta$ terms become sort

of 0; so, as a result now this cos theta is only sin phi sin delta plus cos phi cos delta cos omega. So, here everything is easily determinable, phi is the position dependent term, delta is the declination angle, phi is again position dependent, delta is declination angle and omega is the hour angle.

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Solar Radiation Geometry

For a surface facing south, $\gamma=0^\circ$

$$\begin{aligned} \cos \theta &= \sin \phi (\sin \delta \cos \beta + \cos \delta \cos \omega \sin \beta) \\ &\quad + \cos \phi (\cos \delta \cos \omega \cos \beta - \sin \delta \sin \beta) \\ &= \sin \delta \sin(\phi - \beta) + \cos \delta \cos \omega \cos(\phi - \beta) \dots (5) \end{aligned}$$

For a vertical surface due south, $\beta=90^\circ, \gamma = 0^\circ$

$$\cos \theta = \sin \phi \cos \delta \cos \omega - \cos \phi \sin \delta \dots (6)$$

So, this is how you can do for various things. You can have a, for you can simply over for a surface which faces south. For a surface which faces south, the projection of normal cosine sin should the south line. So, as a result gamma becomes equal to 0. Again this equation gets simplified to cos theta is equal to sin delta sin phi minus beta plus cos delta cos omega cos phi minus beta. And beta is the angle of inclination, phi is position dependent term, delta is the dependent term and omega is time dependent term.

You can also further simplify for a vertical surface due south. So, in this case beta is 90, gamma is 0. So, this again gets simplified cos theta term; so, basically the ideas to determine cos theta. What was cos theta? Theta is the angle between the sun beam and the so, if you go back to previous picture, theta is the angle between the sunbeam and the normal to the surface ok. So, basically this is what we are interested in determining.

So, if you have inclined surface which does not phase south then it gets complicated, but if you have if you make simplifications like surface facing south or surface being horizontal, surface being vertical these becomes little bit simpler. So, these are approximations one can make.

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Solar Radiation Geometry

We can also express the angle of incidence θ in terms of zenith angle θ_z , slope β , surface azimuthal angle γ , and solar azimuthal angle γ_s as following:

$$\cos \theta = \cos \theta_z \cos \beta + \sin \theta_z \sin \beta \cos(\gamma_s - \gamma) \dots \dots \dots (7)$$

Solar azimuthal angle γ_s is obtained as following:

$$\cos \gamma_s = (\cos \theta_z \sin \phi - \sin \delta) / \sin \theta_z \sin \phi \dots \dots \dots (8)$$

However, there is nothing these is you can also determine for a surface which is at certain angle. So, in that case you need to know delta gamma.

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Sunrise, Sunset, Day Length

For a horizontal surface, we can find out the hour angle ω_s corresponding to sunrise or sunset by substituting $\theta_z=90^\circ$ in eqn (4) i.e.

$$\cos \omega_s = -\tan \phi \tan \delta \quad \text{OR}$$

$$\omega_s = \cos^{-1}(-\tan \phi \tan \delta) \dots \dots \dots (9)$$

= (+ve for sunrise and -ve for sunset)

Maximum Day Length

$$S_{\max} = \frac{2}{15} \cos^{-1}(-\tan \phi \tan \delta) \dots \dots \dots (10)$$

So, we can also define two more few more things sunrise, sunset and day length. So, for a horizontal surface, one can find out what is the hour angle corresponding to sunrise, sunset. And for this you determine theta z to be equal to 90 degree in the in the previous equation. So, cos omega s is equal to minus tan phi tan delta or omega s can be written as

cos inverse minus of tan phi tan delta. And this value is positive for sunrise and negative for sunset.

So, since omega s is positive for sunrise negative for sunset, day length can be found by omega s minus of minus omega s. So, basically this becomes 2 omega s. So, if you look at the whole equation, day length is S max is equal to 2 divided by 15. So, 15 is nothing but you know three 60 degrees in 24 hours. This 15 is it is in hours basically. So, 2 if you look at the whole thing 15 into S max is equal to 2 into cos inverse minus tan phi tan delta; 2 into cos inverse minus tan phi tan delta is omega s.

So, this is 2 of omega s equal to 15 into S max, 15 is coming because of cal because you want to calculated in hours. If you did not want to calculate it in hours you can eliminate 15. So, maximum day length is 2 divided by 15. So, 2 omega s divided by 15 essentially and you substitute omega s from the previous equation. So, all of this is valid for northern hemisphere. If you need to go for southern hemisphere, you need to make appropriate corrections in the equation which has simple.

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Sunrise, Sunset, Day Length

Between March 21 and September 21, since the Sun moves to North of E-W.

$$\omega_s = \cos^{-1}(-\tan(\phi - \beta)\tan\delta) \dots\dots\dots(11)$$

So, between so for a inclined surface, so this is for a horizontal surface. But for a inclined surface between March 21 and September 21, sun so you can see as the sun moves sun is. So, you are going from sun goes from east to west, but in winter its more southish, in the summer its more northish. It is sun is mostly top in the summer. So, it moves to the north of east-west as a result between 21st in a September 21 the equation

gets modified as if for inclined surface omega s is equal to cos inverse minus of tan phi minus beta into tan delta. So, you need to consider the beta thing into account for this period.

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Sun Rise and Sun Set

June 21st and December 21st

$\gamma = 0^{\circ}, \beta = 10^{\circ}$

19° 07' N }
72° 57' E } Mumbai

So, for example, so let us let us see for certain position sun rise and sun set. So, between so you can say a for June 21st and December 21st, let us say gamma is equal to 0, which means surfaces facing due south, and beta is equal to 10 degree. And let us consider Mumbai whose location is 19 degree 7 minutes north, and 72 degree 57 minutes east ok. So, phi is given as 19 07.

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$$\begin{aligned}\phi &= 19^{\circ}07' = 19.12^{\circ} \\ \text{For June} \\ \beta &= 10^{\circ} \\ \delta &= 23.45 \sin \left[\frac{360}{365} (n + 254) \right] \\ \delta &= 23.45^{\circ} \\ \omega_{st} &= \cos^{-1} \left[-\tan(19.12^{\circ} - 10^{\circ}) \tan(23.45^{\circ}) \right] \\ \omega_{st} &= \underline{\underline{\pm 94^{\circ}}} \quad S = \frac{2}{15} \text{ WS}\end{aligned}$$

So, phi is 19 07 which is 19.12 degree. For June, beta is equal to 10 degree. You can find out delta, delta is 23.45 sin of 360 by 365 into n plus 254.

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$$\begin{aligned}\text{Dec} \\ \omega_s &= \cos^{-1} \left[\tan(19.12^{\circ}) \tan(-23.45^{\circ}) \right] \\ \omega_s &= \underline{\underline{\pm 81.4^{\circ}}} \text{ --- smaller} \\ &\quad \text{day} \\ &\quad \text{length}\end{aligned}$$

And then we have this so declination angle if you put in the value it will turn out to be. So, this will be your delta value. Then omega can be calculated as cos inverse minus of tan for inclined surface phi minus beta. So, this is phi, this is beta tan of 23.45. And so as a result omega is minus plus minus 94 degree for sun rise and sun set. So, this can be converted to day length.

And for December you can make the similar calculation. For December it would be $\cos^{-1} \tan 19.12^\circ$; [FL] in that you can reduce you can eliminate the beta. So, beta goes off and \tan of minus 23.45. So, this comes to be plus minus 81.4. So, you can now look at the wide day length, obviously, can see that 2ω will be larger in case of June than in case of December. So, you can see that your day length will be higher.

So, if you write here, if you write here, s will be equal to 2 divided by 15ω s. So, you can see that this will be larger in this case. Whereas, if you go to next one this is a smaller, as a result smaller day length is obtained for December. So, these are simple calculations you can do for where ever you are.

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Local Apparant Time

$$LAT = \text{Standard Time} \pm 4(\lambda_{\text{standard}} - \lambda_{\text{actual}})$$

+ Equation of time correction

λ : longitude

Now, let us look at another parameter which is called as local apparent time which is called as which is basically standard time plus minus 4 into lambda standard minus lambda actual. And lambda is nothing but the longitude plus equation of time correction that we looked at earlier ok. So, local apparent time is equal to standard time plus minus 4 into lambda standard minus lambda actual plus equation of time correction.

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Mumbai (19° 7' N, 72° 51' E)

IST 14:30 h 1st July
Indian ST $\lambda_{st} = 82.5^\circ$ E

Equation of time correction = - 4 min

LAT = 14:30 h - 4 (82.5 - 72.85) + (- 4 min)
LAT = 14:30 - 38.6 min - 4 min
LAT = 13 h 47 min

And so if you now look at Mumbai again, Mumbai is longitude latitudes are given. Let us says its, IST 14 hours 30 minutes on first of July and Indian standard lambda is 82.5 degree east. So, if you look at equation of time correction, it is minus 4 minutes. So, a standard time is given according to this, because you this is your India let us say not very good map, but right. So, Mumbai is somewhere here. Latitude of longitude the geometrical parameters of Mumbai are different with respect to GMT plus GMT plus 5 5 5.30 right.

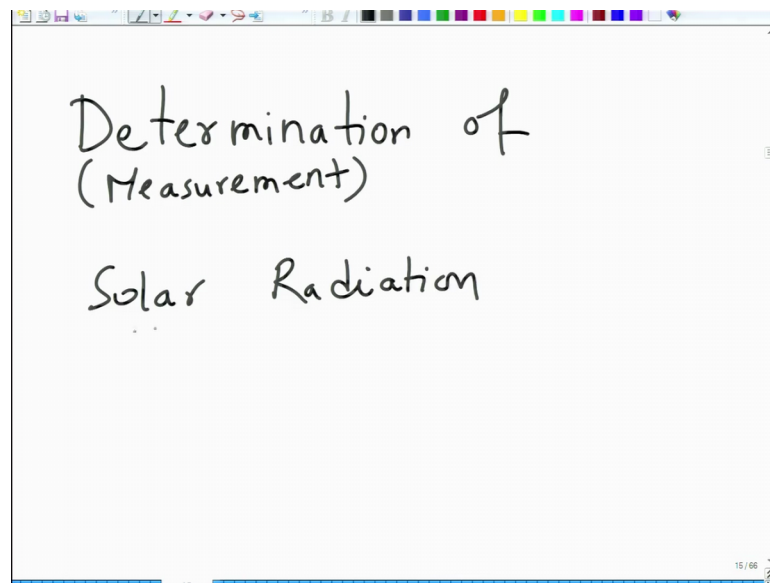
Now, this GMT for 5.30 will correspond to certain lambda value ok, because longitude of 5.30 would be some from the middle of India which is about Nagpur. So, this would be your standard lambda. So, this is lambda standard. Whereas, Mumbai is here this is lambda Mumbai right. So, there is a difference here. So, equation of time correction, if you go to previous equation in the previous lecture, it will be turn out to be minus 4 minutes. As a result local apparent time will be 14.30 hours minus 4 into 82.5 standard lambda minus the actual lambda which is 72.85 plus minus of 4 minutes.

And if you work this out, it comes out to be 13 hours 47 minutes. So, your the clock shows the time of 14.30 hours, but actual time in Mumbai is 13.47 hours. Similarly, if you do the same calculation for a Arunachal Pradesh the actual time will come will be ahead right. So, if you look at 14.30 hours time, it will become 15.30 for example, in

case of Arunachal Pradesh. So, this is how time corrections have to be made for calculate in the actual time.

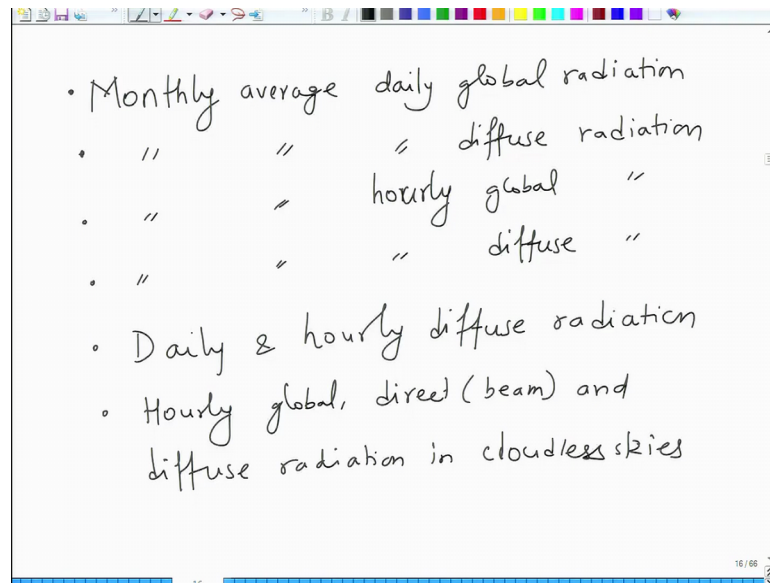
So, this is basically what we have discussed so far is related to the time corrections and geometries and so how to calculate angle of solar radiation with respect to a surface that is what we have done. And we have looked at a time corrections which will help us in calculating the radiation at appropriate time. So, these are the two things you need the direction and the time.

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Now, let us look at how to calculate the now what we will do is that we will do determination of, not determination actually it should be measurement ok, measurement of solar radiation. So, solar radiation can be defined in various fashion. And lot of these most of these methods of determining solar radiation at a given location or a given day given time are mostly empirical in nature. So, we will not look at all the models to the positive of time, we will only look at a few of them.

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So, the way you define solar radiation measurement there are methods of there are ways in which different people have done. So, for example, first method to decide solar radiation is monthly average daily global radiation. Now, here the trick is you have to measure direct radiation, you have to measure diffuse radiation, and then it can be average over a month, it can be average over a day so on and so forth.

There are various models for various definitions. So, monthly average daily global radiation, monthly average daily diffuse radiation. And monthly average hourly global radiation, then we have monthly average hourly diffuse radiation. And then we have daily and hourly diffuse radiation, and then we have hourly global direct which is also called as beam radiation and diffuse radiation in cloudless skies.

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Monthly average daily global radiation

$$\frac{\bar{H}_g}{\bar{H}_c} = a + b \left(\frac{\bar{S}}{S_{max}} \right)$$

monthly av^r of daily global radiation on a horizontal surface at a given location ($\frac{kJ}{m^2 \cdot day}$)

\bar{H}_c on a clear day

\bar{S} = monthly av^r of sunshine hrs per day (h)

S_{max} = monthly av^r maximum possible sunshine hrs (h)

So, let us first look at monthly average daily global radiation. So, in this case, the first attempt was made by somebody called as Angstrom. He said \bar{H}_g is divided by \bar{H}_c which is a plus b into \bar{S} divided by S_{max} . Now, what are these quantities? Now, \bar{H}_g is basically monthly average of monthly average of daily global radiation on a horizontal surface at a given location. And this is in kilo joule per metre square per day ok. Similarly, \bar{H}_c is monthly average of daily global radiation on a horizontal surface at the same location on a clear day.

So, the so essentially \bar{H}_g , it is equal to \bar{H}_c on a clear day ok. This is on a general day; this is on a clear day absolutely clear day again the same thing. \bar{S} is equal to S_{max} on a clear day. \bar{S} is defined as monthly average, monthly average of sunshine hours per day at the location ok. So, this is in hours. And then we have S_{max} , you can guess what it would be, it would be monthly average of maximum possible sunshine hours at a given location that is there on the horizontal surface [FL].

So, monthly average maximum possible sunshine hours at the same location on a horizontal surface; and then a and b are the constants which are empirical constants used for data fitting. So, this is mostly empirical. And you can again you can now there were later some changes which were made for example, this \bar{H}_g was \bar{H}_c as it was not very easy to calculate \bar{H}_c which is maximum average of daily global radiation on a horizontal surface on a clear day, it is not be easy to mention.

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\bar{H}_c replaced with H_o

H_o - monthly avg of extraterrestrial radiation which would fall on a horizontal

Pune = $\bar{S}/\bar{S}_{max} = 0.25-0.49$

	a	b
Pune	0.3	0.51
Bangalore	0.18	0.64
Jodhpur	0.33	0.46
Delhi	0.25	0.57

Solar Energy, 22 (407), 1979

So, H_c was later replaced with H_o . So, you can say H_c replaced with another quantity H_o . And what is H_o ? Monthly average of extraterrestrial radiation which would fall on a horizontal surface. So, many of these quantities are changed because previous quantities were not easy to obtain as a result changes are made. So, essentially you can do the calculations and work out various values.

For example, for Pune in India, the value of \bar{S} to \bar{S}_{max} was \bar{S}_{max} was about 0.25 to 0.49 with a and b value being a being 0.3 and b being 0.51. You can do for various other locations a and b values for example, place like Bangalore, Bangalore would be about 0.18, 0.64.

If you look at a place like Jodhpur, Jodhpur will give you a value of 0.33 and 0.46. And if you look at something like Delhi, Delhi would be 0.25 and 0.57. So, these data you can obtain in literature. So, there is a paper in solar energy 22, 407, 1979. So, this is the volume number; this is the page number; this is the year number, and this is the name of the journal. Now, so this is what we defined here was, this was the monthly average daily global radiation.

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The image shows a handwritten derivation of the monthly average extra-terrestrial radiation equation. The equation is written on a whiteboard with a toolbar at the top. The derivation starts with the following equation:

$$H_0 = \frac{12}{\pi} \cdot I_{sc} \left[1 + 0.033 \cos \frac{2\pi n}{365} \right] \int_{-\omega_s}^{+\omega_s} (\sin \phi \sin \delta + \cos \phi \cos \delta \cos \omega) d\omega$$

The second line shows the result of the integration, with a downward arrow pointing from the first term of the bracketed expression in the first line to the first term of the second line:

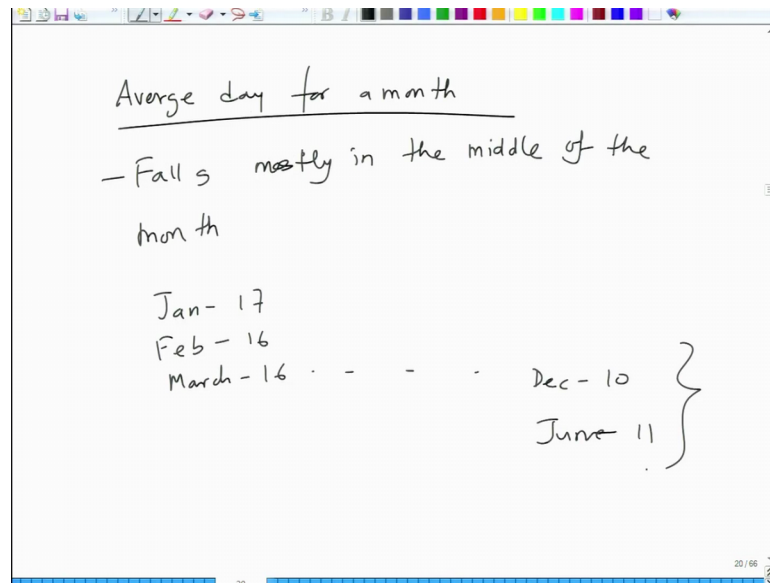
$$= \frac{24}{\pi} \cdot I_{sc} \left[\omega_s \sin \phi \sin \delta + \cos \phi \cos \delta \cdot \sin \omega_s \right]$$

So, how do you work out? Now, H naught this H naught is the monthly the average of extra terrestrial radiation that would fall on the on a horizontal surface. H naught is given by this equation, 12 divided by phi into I s c which is the solar constant into 1 plus 0.033 cos of 2 pi n divided by 365, and then you integrate it over whole day.

So, this is essentially cos theta term integrated. So, sin phi sin delta plus cos phi cos delta into cos omega over d over whole time; so, the cos phi term integrated over the whole day and that that is what you will obtained for a given location. And this would turned out to be omega s sin phi sin delta plus cos phi cos delta into sin of omega s, this is what this term will turn out to be.

And, if you do this will be this will become 24 by phi into I s c into the term that you have here and this term 24. And this can be simplified by I mean for a given month it was found by scientist that you can find average day for a month.

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So, if you want to find out the monthly average you can just choose that particular day. So, for example, for so you can say average day for a month and this average day falls mostly in the middle of the month, it is not exactly middle, it changes. So, for example, for January it is 17; for February it 16; for March it is of course, this has come after empirical data fitting ok. So, it is not just you take 15th of January 15th of Feb. The so calculations are made for the whole month measurements are made for the whole month and then average out the values and see which day corresponds to the average of it. So, this is what various values would be like.

Whereas for December for example, it becomes 10; and for June, it will zone for June it is 11. And June, December show a bit of deviation because June and December are months where you have longest day and longest night. As a result they have bit of deviations in these two months, but other months show fairly the average days fairly in the vicinity of 15th of every month.

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Baroda - March $a = 0.28, b = 0.48$

16th $\rightarrow H_0 = ?$

$n = 75$

$$\delta = 23.45 \sin \left[\frac{360}{365} (75 + 284) \right] = -2.42^\circ$$

$$\omega_s = \cos^{-1} (-\tan \phi \tan \delta)$$

$$= 89.02^\circ \equiv 1.554 \text{ Rad}$$

$$S_{\max} = \frac{2}{15} (89.02) = 11.87 \text{ hvs}$$

$$H_0 = \frac{2\pi}{4} \cdot I_{sc} \left(= 1.367 \frac{\text{kW}}{\text{m}^2} \right) \times 3600 \left(1 + 0.033 \cdot \cos \frac{360}{365} \cdot 75 \right)$$

$$= 34206 \cdot \left\{ 1.554 \cdot \sin 22^\circ \cdot \sin(-2.42^\circ) + \cos 22^\circ \cdot \cos(-2.42^\circ) \right\}$$

21/08

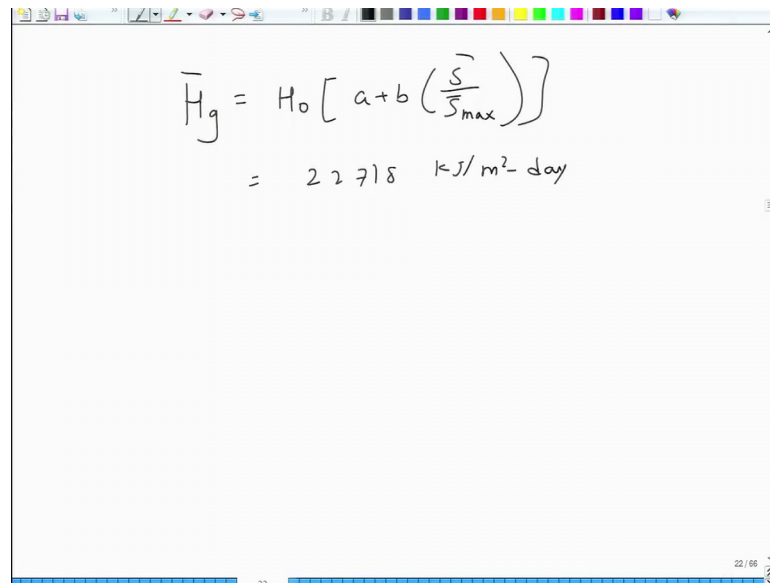
So, you if you want to calculate the monthly average radiation let us say in Baroda, Baroda in March. So, for Baroda is 0.28, and b is 0.48. The average day is 16th ok. On 16th, I can calculate was its H naught; so, H naught for 16th needs to be calculated and this works 16th works out to n is equal to 75 75th day of the year.

So, delta is 23.45 into sin of 22 pi divided by 365 you can say 360 divided by 365 into 75 plus 284, this will give you angle of minus 2.42 degree. Omega s since it is before 21st of March this is cos inverse minus of tan phi and delta. And this will be nearly 89.02 degree which is equivalent to 1.554 radian.

So, I can find out S max which is 2 by 15 into omega s. So, this is 2 by 15 into 89.02. And this turns out to be 11.87 hours all right. H naught can be found by 24 by pi into I sc which is equal to 1.367 kilo watt per metre square into 3600 ok, 3600 is a correction you can see it is for hour into seconds ok, and then you have 1.033 cos of 360 by 365 into 75 which is n value, and this is multiplied by omega s that is 1.554 into sin of 22 sin of 22 will. So, if you look at the equation, sin phi which is the latitude.

So, sin of 22 which is the latitude for Baroda into sin of minus 2.42 which is delta plus cos of phi which is cos 22 into cos of delta which is minus 2.42 degree into cos of omega x, which is eighty nine point sorry sin of omega s which is 89.02 degree. And if you do the calculation this will turn out to be 34206 kilo joule per metre square per day.

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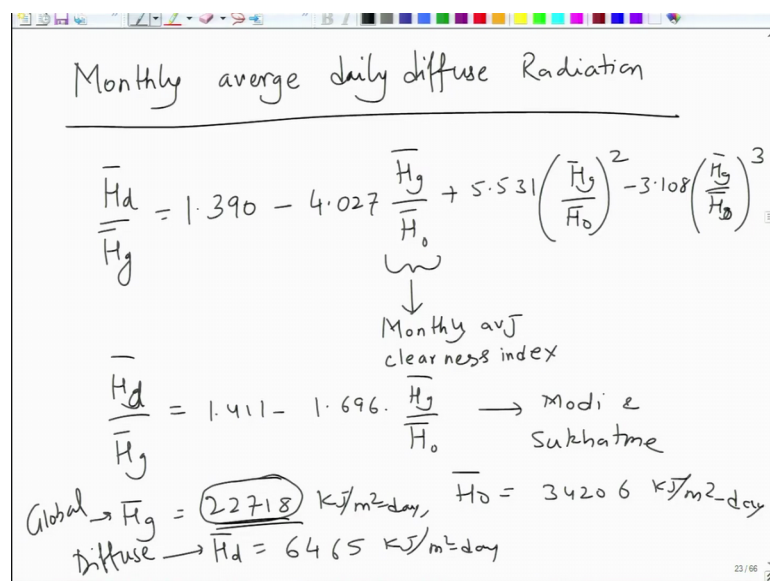


$$\bar{H}_g = H_0 \left[a + b \left(\frac{\bar{S}}{\bar{S}_{max}} \right) \right]$$

$$= 22718 \text{ kJ/m}^2\text{-day}$$

So, if you now make the calculation of \bar{H}_g which is the daily global average daily global radiation which is H_0 into $a + b \bar{S} / \bar{S}_{max}$ this will be 22718 kilo joule per metre square. The daily global radiation for a given location in Baroda in the month of March is 22718 kilo joule per metre square per day. So, I hope you can understand the calculation. It is a fairly simple calculation that we have seen here.

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Monthly average daily diffuse Radiation

$$\frac{\bar{H}_d}{\bar{H}_g} = 1.390 - 4.027 \frac{\bar{H}_g}{H_0} + 5.531 \left(\frac{\bar{H}_g}{H_0} \right)^2 - 3.108 \left(\frac{\bar{H}_g}{H_0} \right)^3$$

\downarrow
 Monthly av^J
 clearness index

$$\frac{\bar{H}_d}{\bar{H}_g} = 1.411 - 1.696 \cdot \frac{\bar{H}_g}{H_0} \rightarrow \text{Modi \& Sukhatme}$$

Global $\rightarrow \bar{H}_g = 22718 \text{ kJ/m}^2\text{-day}$, $H_0 = 34206 \text{ kJ/m}^2\text{-day}$
 Diffuse $\rightarrow \bar{H}_d = 6465 \text{ kJ/m}^2\text{-day}$

So, you can also calculate the monthly average diffuse daily diffuse radiation. So, this is again so H_d divided by H_g again empirical equation H_d is equal to $1.390 - 4.027 H_g$ divided by H_0 plus $5.531 H_g$ divided by H_0 square minus $3.108 H_g$ divided by H_0 over cube. So, this is the daily diffuse radiation, and this is the daily global radiation; monthly average daily diffused radiation, monthly average daily. So, it is again a fitted amount fitted equation. And this parameter H_g divided by H_0 is called as monthly average clearness index basically it makes sense.

So, if higher the H_g is more this ratio is going to be which means that day is more clear right. When the day is more clear, your global radiation is going to be higher at number. And when this parameters higher, as a result your diffuse radiation also tends to be smaller in amount. This equation has been modified for India. For India you can use a little bit modified equation H_d divided by H_g . This is the $1.411 - 1.696$ into H_g divided by H_0 . This is done by Modi and Sukhatme.

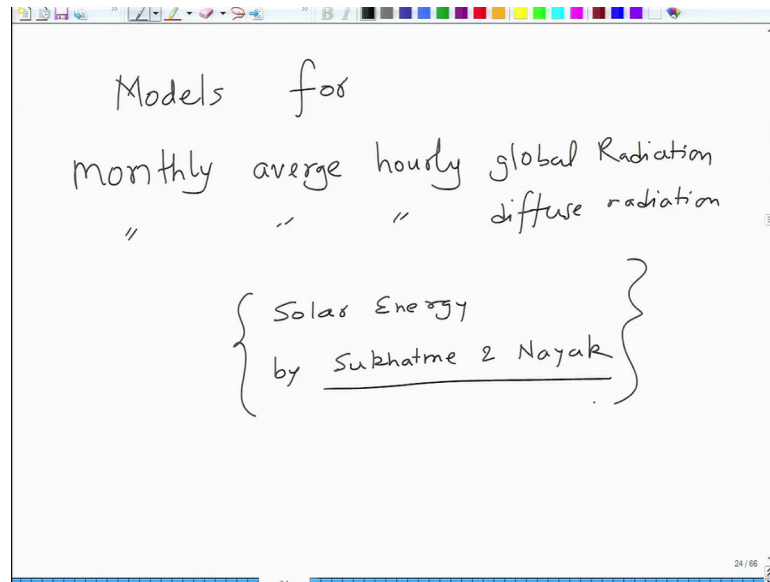
So, based on the values that you obtain for H_g and H_0 for a given day, you can calculate what the diffuse radiation is going to be ok. So, I mean from the previous equation, you can just make the calculations. So, if your H_g is 22.718 kilo joule per metre square per day, and your H_0 was 3220, 34206 kilo joule per metre square per day. You can calculate what your H_d is going to be H_d is going to be 6465 kilo joule per metre square per day.

So, obviously, if you increase the value of H_g , your H_d will come down and right. So, this is what and direct radiation is nothing but H_g minus H_d . So, this is total radiation global. So, this is global; this is diffuse. So, your direct or beam radiation is global minus diffuse. So, 22718 minus 6475 will be the direct radiation.

So, idea is in most cases to so I mean it is not in your hands, but if we have higher amount of beam radiation, this number will go up as compared to diffuse radiation on a clear day. So, similarly there are models for monthly average hourly global radiation, monthly average hourly diffuse radiations, and I will not get into details of those. So, we can say month. So, models for monthly average hourly global radiation, and monthly average hourly diffuse radiation.

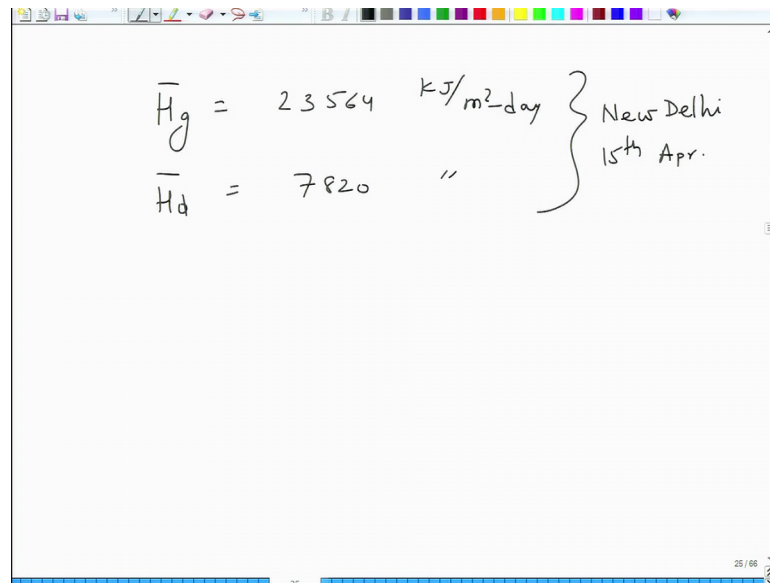
So, we cannot cover all of these in this course. So, I would request that you go to this book by I do not remember the exact topic as of now. But if you look at the first lecture, in the first lecture I have provided the book by Sukhatme and Naik.

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I think it is solar energy or solar thermal storage something like the name of the title is, but anyway you can find it out it is a book by Sukhatme and Naik. The first or second chapter of that book first few chapters of that book discuss these models for a daily average and daily diffuse radiation for given locations in India. So, it is a very nice calculation.

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The image shows a whiteboard with handwritten text. The text is as follows:

$$\begin{aligned} \bar{H}_g &= 23564 \text{ kJ/m}^2\text{-day} \\ \bar{H}_d &= 7820 \text{ " } \end{aligned} \left. \vphantom{\begin{aligned} \bar{H}_g \\ \bar{H}_d \end{aligned}} \right\} \begin{array}{l} \text{New Delhi} \\ 15^{\text{th}} \text{ Apr.} \end{array}$$

The whiteboard also features a toolbar at the top with various drawing tools and a status bar at the bottom right showing '25 / 66'.

So, if you so let me just give you the values for example, the values of if you do on hourly basis, the \bar{H}_g turns out to be 23564 kilo joule per metre square per day. And \bar{H}_d will be 7820 kilo joule per metre square per day. This is for example, for New Delhi on the April 15th, 15th April for a horizontal surface.

So, you can so again there are empirical equations in which you need to provide the data again you need to calculate what the declination angle is going to be, what the value of hour angle ω_s is going to be, what is the angle that is what is the day length that is going to be, similarly you need to calculate what is the extra terrestrial that is. So, equations are fairly similar, it is just that they are they have different empirical fitting constants. So, as a result they give you slightly different values. So, you can go to this book by Sukhatme and Naik, and read more about these models which provide these values.

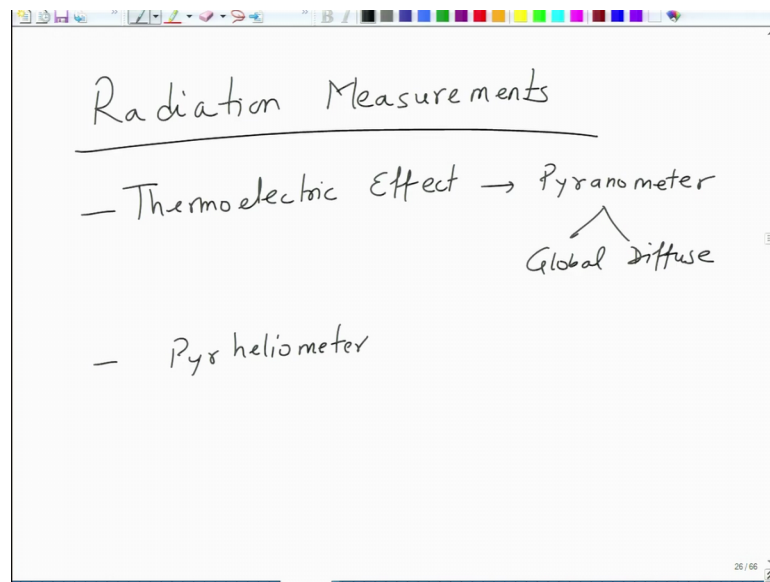
So, this sort of gives you an idea of how do you determine so this is for a horizontal surface most of these calculations. So, if you want to, so if you know that your radiation is coming at certain angle. So, you know what is the global radiation, you know what is the diffuse radiation from this you can find out the direct radiation. Now, you know direct radiation comes directly. So, for a horizontal surface, it is fine, but for a incline surface you will have to take $\cos \theta$ of or whatever the angle that the normal and the vertical that they make with each other. So, if it is $\cos \beta$, you will have to

modify that with $\cos \beta$ so that much amount of drop in the direct radiation that will happen for a incline surface. But the diffuse will remain same, diffuse does not have angular dependence as a result diffuse will remains fairly the same.

So, what will happen is that your global radiation for a incline surface will change as compared to that for a horizontal surface. Of course, these values are time dependent as well because different times will give you different. So, there will be times at which inclines surface will give you higher radiation, so that is why surfaces are kept inclined because they tend to take out the average value for the day.

Horizontal value will get horizontal surface will get maximum radiation only for the when the sun is at zenith. So, that is why you will see every solar panel is inclined to the surface at certain angle to average over the whole day in terms of receiving maximum solar radiation or average value of solar radiation which is nothing but a one 1.5 g. So, there are models in the same book for tilted surfaces also and so on and so forth that you can read in the books.

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So, how do you do the radiation measurement? Radiation measurement is done by it is done by basically the first is based on thermoelectric effect. And for this we you use equipment called as pyranometer. And this can measure both global and diffuse. And the second one is called as pyrheliometer ok. These are the two equipments which are used for measurement of radiation which are useful.

So, this is what a brief discussion on solar radiation, solar geometry, and solar radiation measurement was. So, this is this is essential to know how the solar radiation is measured for a given surface at a given location.

In the next class, in the in the next lecture onwards, we will move on to the fundamentals of semiconductors which are essential to know to understand the pn junction characteristics which are p-n junction is nothing but a solar cell architecture. So, and since p-n junction is made of p and n-type semiconductor, we need to know how the carriers move after the radiation absorbed within a solar cell. So, we will discuss that in the next class.

Thank you.