



expressed by this right. So you will see under what conditions this blade or diagram efficiency is maximum one thing is here that the ratio of  $U$  and inlet velocity because this is peripheral velocity this is inlet velocity.

Relative velocity is derived from this and this and all the velocities are derived from this and thus peripheral velocity the main thing is the peripheral velocity and the inlet velocity and there ratio is denoted by  $\text{row}$ . This blade efficiency will be maximum when this is having the maximum value this is having the minimum value right  $V_1$  is let us say it is constant.

We cannot have  $V_1$  minimum is 0 it because when there is no velocity at inlet mathematically then efficiency is going to be the infinite. In this case  $V_1$  is also constant will component from is dependent on inlet velocity will component  $VW$  is dependent on inlet velocity or relative velocity at inlet either of these and also yet  $U$  right. So we will say that  $VW$  first of all  $VW = V_1 \cos \alpha_1 + V_2 \cos \alpha_2$ .

Right or we can say subsequently  $VR_1 \cos \beta_1 + VR_2 \cos \beta_2$  we will take  $VR_1 \cos \beta_1$  out  $1 + VR_2$  by  $VR_1 \cos \beta_2$  by  $\cos \beta_1$ . Now these values of either there equal  $\beta_1$  or  $\beta_2$  are equal or their values are very close to each other under any case it is a constant right. And this  $VR_2$  by  $VR_1$  this is played velocity coefficient right so we can always say that  $VR_1 \cos \beta_1 = 1 +$  this is also constant so  $KB$  right.

Ideal case  $K = 1$  and  $B = 1$  now  $VR_1$  we do not have the value of  $VR_1$  because  $VR_1$  dependent is dependent on  $V_1$  the absolute at inlet. So relative velocity is depended on the absolute velocity so instead of taking  $VR_1$  so it cannot be blizzard we will take  $V_1 \cos \alpha_1 - U$ .  $V_1 \cos \alpha_1$  is in this direction that the component of absolute velocity -  $U$  will give us the  $VR_1 \cos \beta_1$  this component.

So this component of  $V_1$  in this direction minus peripheral velocity  $U$  will give this component so this is going to be the  $VW$  right now  $U$  multiplied by  $U$ . So this has to be multiplied by  $U$  and from here we can take  $U = \text{row } V_1$ . So  $VW = U = V_1 \cos \alpha_1 - \text{row } V_1 + KB \text{ row } V_1$  because  $U$  is again replaced by  $V_1$  and this  $U$  can also be replaced by  $\text{row } V_1$ .

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$$2VWU = 2P V_1 (V_1 \cos \alpha_1 - P V_1) (1 + KB)$$

$$= \frac{2VWU}{V_1^2} = 2 (P \cos \alpha_1 - P^2) (1 + KB)$$

$$\eta_b = f(P)$$

$$\frac{d\eta_b}{dP} = 2 (\cos \alpha_1 - 2P) (1 + KB) = 0$$

$$P = \cos \alpha_1 / 2$$

$$= u / V_1$$

Now if you further simplify this so  $2VWU$  is going to be  $2 \text{ row } V_1 V_1 \cos \alpha_1 - \text{row } V_1 + KB$  now this  $V_1$  and  $V_1$  this, this and multiplied by this will go here square is going to  $2 \text{ row } \cos \alpha_1 - \text{row}$  in square  $1 + KB$  is it ok? This row and this row is multiplied  $V_1$  is taken out this  $V_1$  and  $V_1$  are taken out multiplied by this one has gone here row has gone in.

So row  $\cos \alpha_1 - \text{row}$  is square  $1 + KB$  and this is nothing but blade efficiency. Now we have blade efficiency remember this is a constant this is a constant.  $\alpha_1$  is also constant this is the blade inlet angle and which is constant.

So sorry not blade so nozzle inlet angle it is a constant. So we can say that efficiency of the blade is a function of row earlier lecture we have also discussed then the output when we increase row output increase if you remember that graph. When we increase the value of  $U$  by  $V_1$  or the row then the efficiency increases and it is the maximum value and then it comes down right. And this sorry not efficiency work output increases and comes down and force decreases.

When we increases the value of  $U$  by  $V_1$  when  $U = V_1$  there is no force and when  $U = 0$  force is maximum. So now what we can do we can differentiate this equation for blade efficiency with respect to row.

So what we are going to get two row sorry  $\cos \alpha_1 - 2 \text{ row } 1 + KB$  right again if we differentiate  $D$  square and  $B$  by  $D \text{ row square}$  then we are going to get  $2 - 2, 1 + KB$  or  $= -4, 1$

+ KB K and B both are constant so it is going to have negative value. It means if we take this is equal to 0 and the solution will give the maximum value.

Now this is taken as 0 in that case  $\cos \alpha = 1$  by so the maximum efficiency or the highest efficiency the value of  $\cos \alpha$  has to be half of the  $\cos \alpha = 1$  ok and  $\cos \alpha$  is nothing but  $U$  upon  $V_1$ . Now with this value of  $\cos \alpha$  what is the value of efficiency? What is going to be the efficiency of the impulse turbine? In order to find that here we will put  $\cos \alpha = 1$  by 2.

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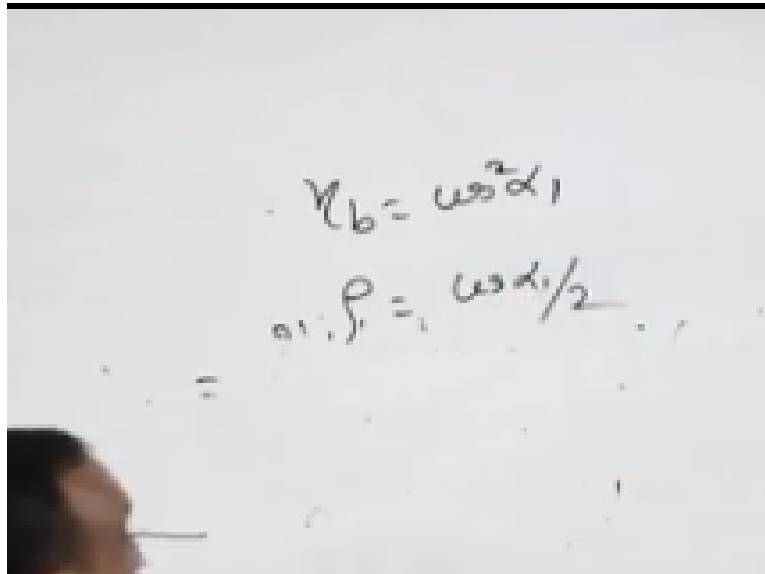
$$\begin{aligned}
 2VwK &= 2P V_1 (V_1 \cos \alpha_1 - P V_1) (1+KB) \\
 &= \frac{2VwK}{V_1^2} = 2 (P \cos \alpha_1 - P^2) (1+KB) \\
 \eta_b &= 2 \left( \frac{1}{2} \cos \alpha_1 \cos \alpha_1 - \left(\frac{1}{2} \cos \alpha_1\right)^2 \right) (1+KB) \\
 &= 2 \left( \frac{1}{2} \cos^2 \alpha_1 - \frac{1}{4} \cos^2 \alpha_1 \right) (1+KB) \\
 \eta_b &= 2 \left( \frac{1}{4} \cos^2 \alpha_1 \right) (1+KB) \\
 \eta_b &= \frac{1}{2} \cos^2 \alpha_1 (1+KB) = \frac{1}{2} \cos^2 \alpha_1 \times 2
 \end{aligned}$$

So efficiency of the blade = two times this is half  $\cos \alpha_1 \cos \alpha_1 - \text{half } \cos^2 \alpha_1$  whole square and then  $1 + KB$  right. And from this you will get two times half  $\cos^2 \alpha_1 - 1$  by 4  $\cos^2 \alpha_1 + KB$  if you further simplify it then you will get blade efficiency as two times 1 by 4  $\cos^2 \alpha_1 + KB$  right or efficiency blade efficiency is half  $\cos^2 \alpha_1 + KB$ .

Now K is an ideal case relative velocity this K is the ratio of relative velocity of steam which is leaving the blade and relative velocity of the steam which is entering the blade. So this is one if there are no friction losses B is blade angle normally the blade inlet angle and blade outlet angle the values are very close to each other they are not exactly same they can be exactly same also but in most of the cases they are very close to each other.

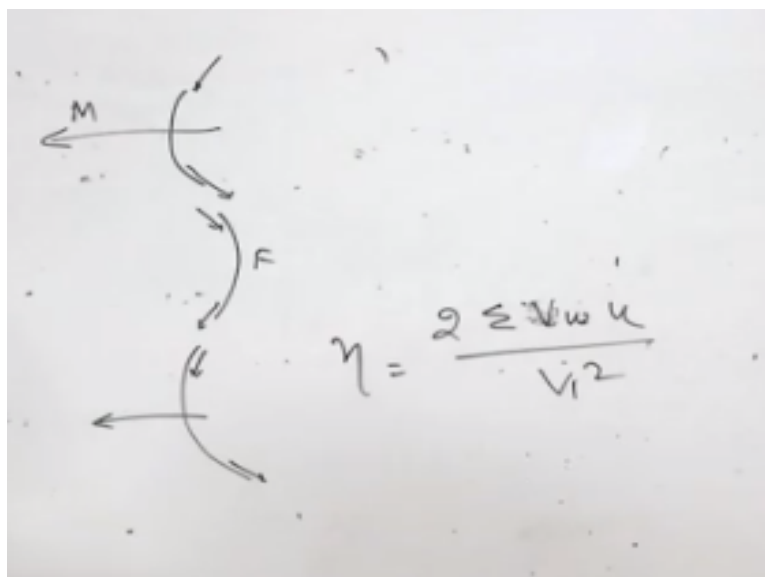
So this K and B we can consider for the sake of convenience we can consider them to be V to be 1. So K is 1, V is 1 + is 2 and then it becomes half cos is square alpha one multiplied by 2 and 2 will be cancelled out.

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We will get blade efficiency as cos square alpha1 right for speed ratio or U by V1 as for a speed ratio  $\rho = \cos \alpha_1$  right. Now we will talk a little about multi staging what happens in multi-staging? In multi-staging when this is analysis we have done for single staging in multi staging what is done suppose there is a multi-staging velocity component turbine.

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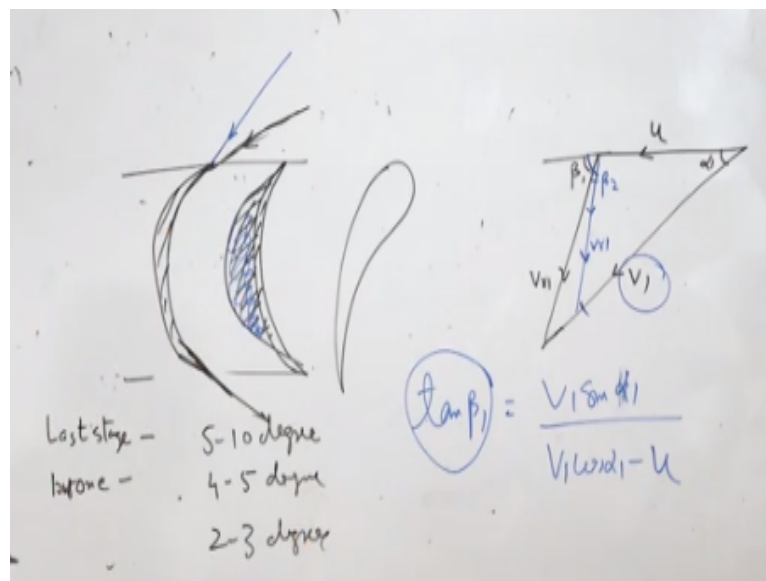
So simply ray diagram if i want to draw this is the moving blade steam is leaving then again there are guide veins steam is entering from here and leaving from here then again though

there is a moving blade and there is a fix blade and then again there is a moving blade right. Steam is entering from here and leaving from here and we can have N number of such stages.

And cumulative effect of these stages will be the net output of the turbine or the if we the concerned with efficiency then efficiency is going to be two sigma VW sorry  $V_w U$  by  $V_1$  square. So this is the sigma will component of each stage will add them and this will give the net output of the multistage in the extremes. Second thing is there are losses for the transmission from this stage to this stage.

The steam leaving the moving blade and entering in the next stage will have some losses in between all these issues will be taking up when we deal with the impulse reaction turbine ok. And after this we will go for selection of blade hmmm angles impulse turbine blade sorry impulse turbine blade sections.

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So for this selection in impulse turbine as you know there are blades made out of plates and there. Co plates like this. So initially this edge was base sharper i will draw bigger diagram i think that will be make things more clear. Initially the blades are like this when it started with the section of the blades of impulse turbine this edge was made sharper.

So that there is a smooth entry of the steam then the steam will glide over the surface and leave from this side later on this side also was made sharper. So the section of the blade became like this so both the ends were sharp and so there are number of plates in turbine

there are not a single blade there are number of blades. So what happens steam which is confined to this or which goes into this zone there is a lot of turbines this is a convex surface.

So turbulence takes place and this causes loss or decline in the efficiency of the turbine right in order to overcome this five types of plates were used. So this side what they need the extended side up to this point. So that there was no turbulence in the vicinity of the convex surface and the performance of the blades was improved and you saw the cases this also the exit this was also extended.

So that proper direction is given to this team which is going out of the blade but this profiling of the blade in impulse turbine blades definitely have the improvement in the performance of turbine. In reaction turbines there air flow type of plates these plates will discuss in detail when we will go for the reaction turbines. The choice of plate angles the inlet angle let us talk about inlet angle.

Now for inlet angle as you know that nozzle or nozzle angle is fixed it is outside the turbine this is peripheral velocity of the turbine this is absolute velocity with  $V$  is entering the turbine and here is the relative velocity  $V_{R1}$  and this is blade inlet velocity inlet angle. Now the issue is that blade inlet angle is depended on the inlet velocity. Suppose the inlet velocity changes inlet velocity is reduced i want less power inlet velocity is reduced diagram will be modified like this right.

And in that case blade inlet angle will change to  $\beta_2$  this is  $\beta_2$  right but we cannot say we cannot open a turbine for different loads and change the blade angle. It is not possible at all blades are fixed and they are fixed at a particular angle but when the  $V_1$  is reduced. So definitely the blade inlet angle will change and when the blade angle inlet angle is more there will be shock they will be the change in blade angle will call the shock entry in the blade and this may damage the blade also right.

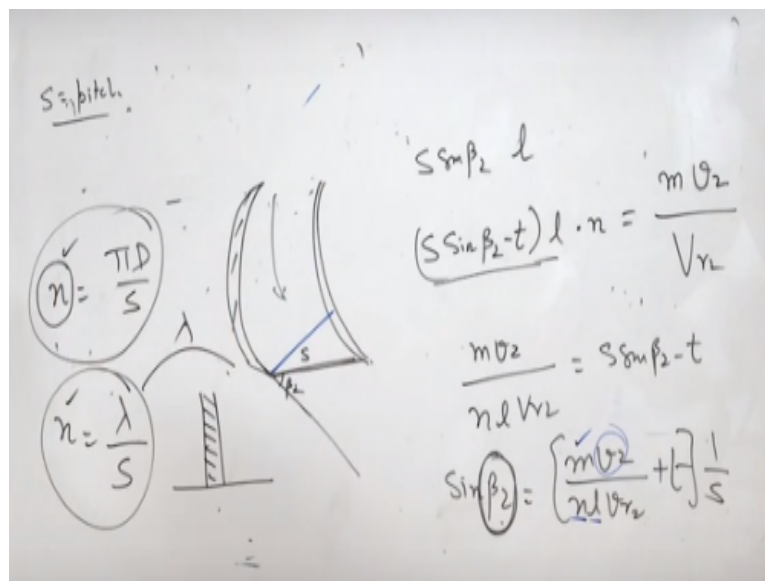
So in at this happens in the case only when then there is a variation in  $V_1$ . So because  $\beta_1$  if you want to calculate  $\beta_1$  it is going to be  $V_1 \sin \beta_1$  sorry  $\alpha_1$  divided by  $V_1 \cos \alpha_1 - U$  right. So normally what we do when there is a partial load the velocity in the last two three stages reduces drastically. So whatever blade angle we calculate with from

the velocity diagram in the last stage the blade angle is purposefully increased by 5 to 10 degree.

This is for the design purpose right in last but one is stage the blade angle is reduced by 4 sorry increased by 4 to 5 degree in remaining stages blade angle is increased by 2 to 3 degree. So after all these calculations when we do in the this velocity diagram finally when we go for a design and manufacturing of the turbine so these allowances are taken so whatever value are getting.

So as we are getting 35 initial stage we will take the blade angle 37 or 38 degree so that shock entry is avoided at par root. Now for the outlet of the blade now this is about the inlet for outlet of the blade the different procedure is adopted because the issues related outlet are different.

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Let us take the two blades one is this one another is this one between them there is a space  $S$  or the pitch of the blade is  $S$ .  $S$  is the pitch of the blade outlet angle is  $\beta_2$  right and cross section area perpendicular to the flow is this one right or it is  $S \sin \beta_2$ . So  $S \sin \beta_2$  that is the distance multiplied to the height of the blade will have certain height. So it is  $S \sin \beta_2$  multiplied by blade height or length of the blade.

It has got certain thickness here also normally the edges the thickness is 0.001 inch or 0.0254 millimeters there is a blade thickness. So here we will take blade thickness also into the count  $S \sin \beta_2 - T$  multiplied by  $L$ . So this is the cross section area of these passage



perpendicular to the flow right and this multiplied by number of passages  $N$  this multiplied by number of passages.

Now how would you get number of passages this is number of passages is  $N = \pi D$  by  $S$ .  $D$  is a diameter  $S$  is the pitch will get  $N$  the number of passages. Suppose there is an arc there is a purpose in impulse turbine it is a partial entry of steam as well in some of the cases in that case suppose if the arc is of  $\lambda$ .

So  $N$  is going to be  $\lambda$  by  $S$  so let us assume there is a entry sorry either of the case whether it is a full entry or partial entry we can have the value of  $N$ . So this is the total area is equal to mass flow rate multiplied by specific volume divided by  $V_r^2$  relative velocity of steam leaving the blades right. Now from here if we resolve this then we will get  $M V_r^2$  by  $N L$   
 $V_r^2 = S \sin \beta_2 - T$  or  $\sin \beta_2 = \frac{M V_r^2}{M L V_r^2 + T}$  divided by  $1$  by sorry  $S$ .

So from this we can get the value of angle  $\beta_2$  because here we have the mass flow rate which is already with us is specific volume. This we can get from the properties of the vapor then number of nozzles length is say this passage suppose this is perpendicular to this white board and you look at the elevation it is going to be like this right.

So this length of the blade so blade will have certain height or length. So length of the blade is  $L$  this is the  $S \sin \beta_2$   $S \sin \beta_2 - T$  is in  $X$  direction  $L$  radial direction that is how we are getting the area multiplied by number of such type of passages. Now from here we will get the blade outlet angle as  $\beta_2$ . Now here in this case in that inlet for designing purpose we are taking the blade angle larger than the what we have calculated here.

But here in this case the blade angle is taken 2 to 3 degree less than that calculated from this so that i mean in partial load also it works well and further because blade angle is less we will get some reaction also by the changes of velocity of the vapor. So that is why this angle  $\beta_2$  is taken normally 2 to 3 degree less then actually which is actually calculated from this formula after this i think we have completed the choice of the bladed that is alpha today.