

Advanced Manufacturing Processes
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Module - 1
Introduction
Lecture - 3
Manufacturing Aspects Selection and Classification

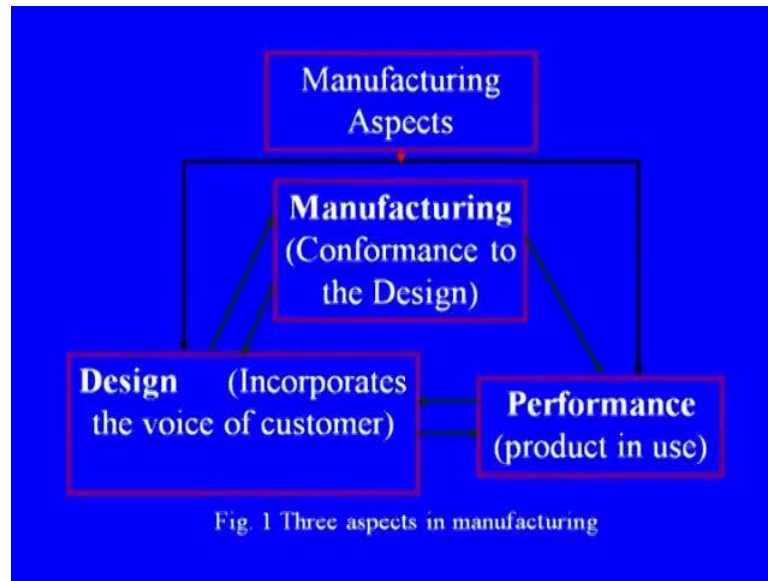
Dear students, in this session we will discuss different aspects of manufacturing, process selection criteria, process capability, and classification of manufacturing processes. First let us look into the different aspects of manufacturing.

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- There are three major aspects of manufacturing –
 - Design,
 - Translation of Design into Product, which is also called actual manufacturing, and
 - Performance of the Product.
- Their relationship with each other are shown in the Fig. 1.

There are three major aspects of manufacturing; design, translation of design into product, which is also called actual manufacturing and performance of the product. The relationship between these are shown in figure one.

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Manufacturing aspects or design, performance, and manufacturing; in the design phase the concept of the product is translated into a written document. This incorporates the voice of the customer, then this design is converted into a product by means of various manufacturing techniques, which is called manufacturing. Here the design will be converted into the product by conforming to the design specifications. Then the resultant product will be moved to the market, where they will be put to use. Here at this stage, the performance of the product will be tested and depending on its performance.

The feedback of the user will be giving to the designers, where the design of the product may get improved according to the feedback of the customers. Then the improved design will be implemented in the manufacturing phase and or an improved product will be resulted and thus the cycle will continue. What is the customer prospective of this design process?

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Design: Consumer's Perspective

- The product must be designed to meet the requirement of the end-customer. It must be designed 'RIGHT', the very first.
- While designing, all aspects of the customer expectations must be incorporated into the product.

The product must be designed to meet the requirement of the end customer. It must be designed right the very first time. While designing all aspects of the customer expectations must be incorporated into the product. And what is the manufacturer's perspective?

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Manufacturer's Perspective

- The product must be manufactured exactly as designed. The activities involved at this stage include:
 - Defect Prevention,
 - Defect Finding,
 - Defect Analysis and Rectification.

The product must be manufactured exactly as designed. The activities involved at this stage include; defect prevention, defect finding and defect analysis and rectification, if

there is any. The difficulties encountered at the manufacturing stage must be conveyed to the designers for modifications in design.

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- The difficulties encountered at the manufacturing stage must be conveyed to the designers for modifications in design.
- Two-way communication between design and manufacturing (concurrent approach) can help to improve the quality of product to a great extent, as different issues such as practical difficulties, achievable tolerances and process capabilities will be addressed.

Two way communication between design and manufacturing, which is also called concurrent approach can help to improve the quality of the product to a great extent. As different issues such as practical difficulties, achievable tolerances and process capabilities will be addressed.

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Performance of the manufactured Product

- The product must function as per the expectations of the end customer. The continuous communication between designer and customer is the key to have a high quality product.

Performance of the manufactured product: The product must function as per expectations of the end customer. The continuous communication between designer and customer is the key to have a high quality product. Next come to the manufacturing process selection. There are different criteria for selection of manufacturing process, the following points need to be considered before actual product manufacturing.

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Manufacturing Process Selection criteria

1. Material selection, which includes considerations relating to:
 - Product requirements,
 - Environmental and recycling aspects, and
 - Cost.

Number one, material selection this includes; the considerations related to product requirements, environmental and recycling aspects and cost.

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2. Selection of Processing Methods such as –

- Metal casting,
- Metal forming,
- Sheet metal working,
- Powder metallurgy,
- Machining,
- Joining,
- Finishing etc.

Number two selection of processing methods, such as metal casting, metal forming, sheet metal working, powder metallurgy, machining, joining, finishing etcetera. Selection of the process sequence appropriate tooling and equipment constitutes the third step.

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3. Selection of the process sequence, appropriate tooling and equipment.
 - This is an important phase from manufacturing point of view.
 - The flow sequence is decided basically depending on:
 - the design requirements, and
 - the processing constraints,

This is an important phase from manufacturing point of view. The flow sequence is decided basically depending on the design requirements and the processing constraints. An engineering drawing is the fundamental element for deciding process and sequence. Right equipment and tool selection is vital in order to produce the product most economical and quality wise competitive.

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9. Production quantity required:
 - It depends on whether it is one-off item, batch production or mass-production item.
10. Safety and environmental concerns
11. Overall cost criteria and feasibility.

Number nine, production quantity required, it depends on whether it is one off item batch production or mass production item. Safety and environmental concerns is the next step. And number eleven overall cost criteria and feasibility. Now, let us move on to process capability.

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Process Capability

- Process capability is defined as the ability of the process to produce output within specification limits.
- It is applied to processes which are under statistical control.
- It helps us to know how much natural variation exists when all other parameters are under control.

Process capability is defined as the ability of the process to produce output within specification limits, it is applied to processes which are under statistical control. It helps

us to know, how much natural variation exists, when all other parameters are under control.

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Process Capability Indices

1. $C_p = (USL - LSL) / 6 \sigma$

where, USL = Upper specification limit,
LSL = Lower specification limit, and
 σ = Standard deviation

- Assuming the processes are normally distributed. This index estimates the capability of production, if the process mean were to be centered between the specification limits.

There are number of process capability indices number one, C_p . It is defined as the ratio of differences between the upper specification limit and lower specification limit, to the 6 sigma, where sigma stands for standard deviation. Assuming the processes are normally distributed, this index estimates the capability of production. If the process mean were to be centered between the specification limits.

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2. $C_{p\text{Lower}} = (\mu - LSL) / 3\sigma$

where, μ = mean

- This is used to estimate the process capability when the specification is of lower limits only (single value, for example, strength)

Number two, C_p lower, which is defined as μ minus lower specification limit divided by 3 sigma, where μ stands for mean. This is used to estimate the process capability when the specification is of lower limits only, that is single value. For example, strength.

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3. $C_{p \text{ Higher}} = (USL - \mu) / 3\sigma$
 - This is used to estimate the process capability when the specification is of upper limit only (Single value, for example, concentration)

Number three, C_p higher, which is defined as upper specification limit minus μ divided by 3 sigma. This is used to estimate the process capability, when the specification is of upper limit only, this is also single value, for example concentration.

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4. $C_{pk} = \min[(USL - \mu)/3\sigma, (\mu - LSL)/3\sigma]$
(whichever is lower)
 - This index helps to estimate the process capability considering the process mean may not be centered between the specification limits.
 - All the indices assume the process is normally distributed.

The fourth index is C_{pk} , which is defined as the minimum of upper specification limit minus μ divided by 3σ and μ minus lower specification limit divided by 3σ , whichever is lower is accepted. This index helps to estimate the process capability, considering the process mean may not be centered between the specification limits. All the indices assume the process is normally distributed.

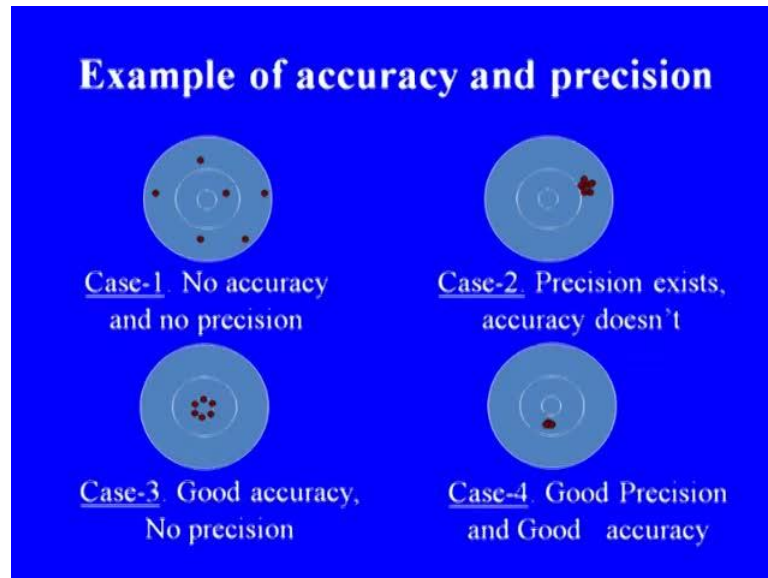
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Accuracy and Precision

- The term accuracy is referred to as the ability of the product to perform within the design specifications.
- Precision refers to repeatability: It is the ability of the system to give the same set of readings or results during each run/attempt.

Then what accuracy and precision? The term accuracy is referred to as the ability of the product to perform within the design specifications. While precision refers to the repeatability, it is the ability of the system to give the same set of readings or results during each run or attempt. Here is an example, a very good example of accuracy and precision can be understood, considering the shooting. Example as shown in the subsequence slide, the inner most circle and this represents the tolerance or specification limit.

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Here, there are four cases. In case one, bullets are being fired in this fashion. This represents a case where no accuracy and no precision. Whereas in case two, bullets are fired in a very narrow zone. Here we can say precision exist, but accuracy does not. In the third case the bullets are being fired near to the target, but not consistently in the single place. Here we can term this as having good accuracy, but without any precision. On the other hand, the fourth case represents a case were good precision and good accuracy both exist. In this case bullets are being fired very near to the target and all shots are concentrated very near.

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Product Design

- Product design is the most important parameter amongst all the parameters of the manufacturing system.
- Design starts from the “idea”, which initiates in the designers mind or through group discussions. It is further developed into a concept .

Then let us move on to product design, product design is the most important parameter amongst all the parameters of the manufacturing system. Design starts from the idea, which intimates in the designers mind or through group discussions it is further developed into a concept.

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Essential factors in product design

- **Need:**
 - This can be individual or social, it also depends on the available technology and resource status.
- **Physical Realizability:**
 - Design should be convertible into material goods or services, i.e., physically realizable. The success of a complex design depends on success of its sub-assemblies and manufacturability.

Essential factors in product design are; need. This need can be individual or social. It also depends on the available technology and resource status. The next factor is physical realizability. Design should be convertible into material goods or services, that is physically realizable. The success of a complex design depends on success of its sub assemblies and manufacturability.

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- **Economic Worthwhileness:**

- The products utility to consumers should be greater than the sum total costs of making it available to him.
- E.g., a bulb of luminous intensity 3 and life 400 hrs, has a lower utility than a bulb of luminous intensity 2.5 and life 500hrs. Utility should be maximum.

Next factor is economic worthwhileness. The product utility to consumers should be always greater than the sum total cost of making it available to him. For example, a bulb of luminous intensity 3 and a life of 400 hours has a lower utility than a bulb of luminous intensity 2.5 and life of 500 hours. Utility should be maximum.

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- **Financial feasibility:**

- The finance should be fundable: i.e., the worth of cash flows into the project when added up during the useful life of the project, should be greater than initial investment for the project. (Net Present Value)

- **Optimality:**

- Its choice must be optimal amongst available alternatives in terms of strength, weight, cost, etc..

Next factor is financial feasibility. The finance should be fundable, that is the worth of cash flows into the project when added up during the useful life of the project, should be greater than initial investment for the project, which is net present value. Next is

optimality. Its choice must be optimal amongst available alternatives in terms of strength weight cost etcetera.

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- **Design Criterion:**
 - Optimality must be established relative to a design criterion which represents the designer's compromise among possible conflicting value judgments which include those of consumer, producer, distributor and his own.

Next comes design criteria. Optimality must be established relative to a design criteria, which represents the designers compromise among possible conflicting value judgments, which include those of consumer, producer, distributor and of his own. Next is morphology of design.

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- **Morphology of Design:**
 - Design is the progression from abstract to concrete. The three phases of design as proposed by Asimov are:
 - a) Feasibility Study phase,
 - b) Preliminary design phase and
 - c) Detailed design phase.

Design is the progression from abstract to concrete, the three phases of design as proposed by Asimov are; Feasibility study phase, then followed by preliminary design phase and finally, the detailed design phase. What are the idea and concepts? The idea initiates from requirements of customers or in some case by the imagination of the designer, to benefit the individual by some means. Developing the idea further requires transforming idea into a concept and further into a product.

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- **Converging the Idea into Reality:**
 - The idea is a resemblance of such system or concepts existing in nature or some earlier developed man-made systems.
 - Additional features and requirements as deemed necessary are fitted into it.
 - These are further converged into the realistic designs and models through rigorous designing and simulations.

Converging the idea into reality, the idea is a resemblance of such system or concepts existing in nature or some earlier developed man made systems. Additional features and requirements as deemed necessary are fitted into it. These are further converged into the realistic designs and models through rigorous designing and simulations. Let us now see what is meant by a product?

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Products

- A **Product** is a bundle of satisfaction to the customer. It can be an assembly of sub-parts, designed for some useful purpose.
- Some Examples include: A vehicle, a refrigerator, a television, a computer, a hydraulic power-pack, a manifold assembly or a spectacle.

A product is a bundle of satisfaction to the customer it can be an assembly of sub parts designed for some useful purpose. Some examples include; a vehicle, a refrigerator, a television, a computer, a hydraulic power pack, a manifold assembly and a spectacle. Let us move on to quality control.

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Quality Control

- As quality is imbibed at each stage in the product, if the product has not been designed right at the first stage, no subsequent operation or steps can further bring back the quality into the product.
- Strict controls and checks need to be established at each stage in the processing.

As quality is imbibed at each stage in the product, if the product has not been designed right at the first stage no subsequent operation or steps can further bring back the quality

into the product. Strict controls and checks need to be established at each stage in the processing let us move on to classification of manufacturing processes.

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Classification of Manufacturing Processes

- There are six basic / fundamental classifications of manufacturing processes.
- A.) Metal casting or Molding:
 - Expendable mold and
 - Permanent mold

There are six basic fundamental classifications of manufacturing processes. The first metal casting or molding, there are two different approaches in this. Number one expendable mold and number two permanent mold. Next class is metal forming and shearing.

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B.) Metal Forming and Shearing:

- Rolling,
- Forging,
- Extrusion,
- Drawing,
- Sheet Forming and
- Powder Metallurgy

This includes a number of techniques called rolling, forging, extrusion, drawing, sheet forming and powder metallurgy. Next category is material removal, which are also called machining processes. In this there are two broad categories termed as conventional and non conventional.

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C.) Material Removal (Machining Processes)

- Conventional:
 - Turning,
 - Boring,
 - Drilling,
 - Milling,
 - Planing,
 - Shaping,
 - Broaching,
 - Grinding.

In the conventional category the processes include; turning, boring, drilling, milling, planning, shaping, broaching, grinding etcetera.

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– ADVANCED PROCESSES :

- Ultrasonic Machining,
- Chemical Machining,
- Electric Discharge Machining (EDM),
- Abrasive Flow Machining (AFM),
- Abrasive Jet Machining (AJM),
- Abrasive Water Jet Machining (AWJM),
- Electrochemical Machining (ECM),
- High-energy Beam Machining,
- Laser Beam Machining (LBM) etc.

Advanced processes; ultrasonic machining, chemical machining, electro discharge machining, abrasive flow machining, abrasive jet machining, abrasive water jet machining, electrochemical machining, high energy beam machining, laser beam machining etcetera. These processes are also termed as unconventional or nontraditional machining processes. Next major classification is joining.

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D.) Joining:

- Welding, Brazing and Soldering,
- Advanced Joining Processes:
 - Plasma arc and Plasma MIG,
 - Projection welding,
 - Ultrasonic welding,
 - Electron beam welding,
 - Laser welding,
 - Microwave joining etc.
- Diffusion bonding,
- Adhesive bonding.

This include; welding, brazing and soldering. Then advanced joining processes this include; plasma arc and plasma MIG, projection welding, ultrasonic welding, electron beam welding, laser welding microwave joining etcetera. Other categories of joining include diffusion bonding and adhesive bonding. Then there are few finishing processes.

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E.) Finishing :

- Polishing,
- Buffing,
- Painting,
- Anti-corrosion coatings etc.

These include; polishing, buffing, painting, anti corrosion coatings etcetera.

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F.) Rapid Manufacturing:

- Stereo-lithography,
- Selective laser sintering (SLS),
- Fused deposition modeling (FDM),
- Three dimensional printing (3D),
- Laminated object manufacturing (LOM),
- Laser engineered net shaping.

Next category is rapid manufacturing which include; Stereo lithography, selective laser sintering, fused deposition modeling, three dimensional printing, laminated object manufacturing, laser engineered net shaping etcetera. Selection of appropriate process one or more appropriate manufacturing processes amongst the discussed processes are chosen while considering the following factors.

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Selection of Appropriate Process

- One or more appropriate manufacturing processes amongst the discussed processes are chosen while considering -
 - the design requirement,
 - resource availability,
 - process capability,
 - feasibility,
 - available skills, and
 - time.

Number one the design requirement, number two the resource availability, number three process capability, number four feasibility, number five available skills and then rest leave the time. Let us consider some examples of manufacturing product.

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- Let us consider some examples of manufacturing product :



A Hydraulic Manifold

A hydraulic manifold is a classic example of manufacturing product, it is a machined component generally made of mild steel on which valves fittings and houses are seated. It reduces piping to a great extent and is considered as the heart of the hydraulic system. It resembles and integrated circuit of an electronic system machine requirements.

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Machine requirements

- The machines required for processing this component would be:
 1. Power / Band-saw for cutting
 2. Milling or Planning for sizing.
 3. Drilling or CNC machining center.
 4. Surface grinding machine for finishing
 5. A test rig for testing after all its sub-components are assembled.

The machines required for processing this component would be, power or band saw of cutting, milling or planning for sizing, drilling or CNC machining center, surface grinding machine for finishing and a test rig for testing after all its sub components are assembled.

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To manufacture this part, preferred machining sequence would be:

1. Cutting of the required billet.
2. Milling it to the size (add some grinding allowance + 0.2 mms)
3. Drilling, counter-boring and tapping.
4. Honing,
5. Grinding,
6. Assembly and Testing.

To manufacture this part preferred machining sequence would be, cutting of the required billet, milling it to the size adding some grinding allowance say for example, plus 0.2

millimeters, then drilling counter boring and tapping, honing and grinding for finishing and finally, assembly and testing.

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And final product after getting assembled would look like this. Let us now see the processing summary for the above product.

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Processing Summary		
Process	Finish Required	Equipment/ Tooling
Cutting	In mms	Power hack-saw, vernier
Milling	Size control in mms, (SF: Ra = 0.3-0.5 μ)	Milling machine, Verniers
Drilling, Tapping	Size control in mms, (SF: Ra = 0.3-0.5 μ)	Radial drilling machine or CNC

Here processes are cutting, milling, drilling, tapping etcetera. In cutting finish required in mms millimeters and equipment or cooling required are power hack saw and vernier. Similarly, in milling size control should be in millimeters, where a surface roughness in

the order of 0.3 to 0.5 micrometer of R a values will be maintained and the equipment or tooling requirement will be milling machine and verniers. Then in drilling and tapping, again the size control will be in millimeters in a range of 0.3 to 0.5 micrometers as R a values and the machines required will be radial drilling machine or a CNC machining unit.

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Process	Finish Required	Equipment/ Tooling
Grinding	Size control in microns (SF: Ra = 0.1-0.2 μ)	Surface grinding machine and micrometer, Surface finish tester.
Assembly and testing	Functionality and rated pressure tests	Test rig, pressure gauges, timers.

Then the grinding process in which the size control will be again in the range of 0.1 to 0.2 micrometer of R a values and the equipment required will be surface grinding machine and micrometer. Of course, a surface finish tester, for verifying the surface is produced. Finally, the assembly and testing in which, the functionality and rated pressure test will be done. Here the required tooling may be a test rig, then pressure gauges, timers etcetera. Let us now see, one more example on the process capability to understand the concept.

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- Assessing process capability value for an individual process first requires the process to be under statistical control.
- To understand this let us see some examples:

Assessing process capability value for an individual process first requires the process to be under statistical control. To understand this let us see some examples.

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Central Limit Theorem:

- Irrespective of the shape of the distribution of the population or universe, the distribution of average values of samples drawn from that universe will tend towards a normal distribution as the sample size grows.

A very important consideration in this is the central limit theorem, which governs most of the control schemes or most of the control schemes use this theorem. So, this theorem says irrespective of the shape of the distribution of the population or universe, the distribution of average values of samples drawn from that universe will tend towards a

normal distribution as the sample size grows. The practical applications of central limit theorem are immense further.

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- The practical applications of central limit theorem are immense.
- Further all the process control tools/ charts are based on this central limit theorem.
- Processes have Controllable causes and special causes present in them.
- When we remove these, then the processes will be under statistical control.

All the process control tools or charts are based on this central limit theorem. Processes have controllable causes and special causes present in them. When we remove these, then the processes will be under statistical control.

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- Pareto analysis is a process of ranking opportunities to determine which of many potential opportunities should be pursued first.
- It states “ Separating the vital few from the trivial many”.

Pareto analysis is a process of ranking opportunities to determine which of many potential opportunities should be pursued first. It states, separating the vital few from the trivial many.

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- Controllable causes include those which can be reduced and are produced due to known causes, such as human errors, machine settings etc.
- Un-controllable causes or inherent variations that are beyond the control and are some times termed as natural variances, which exist in all processes.

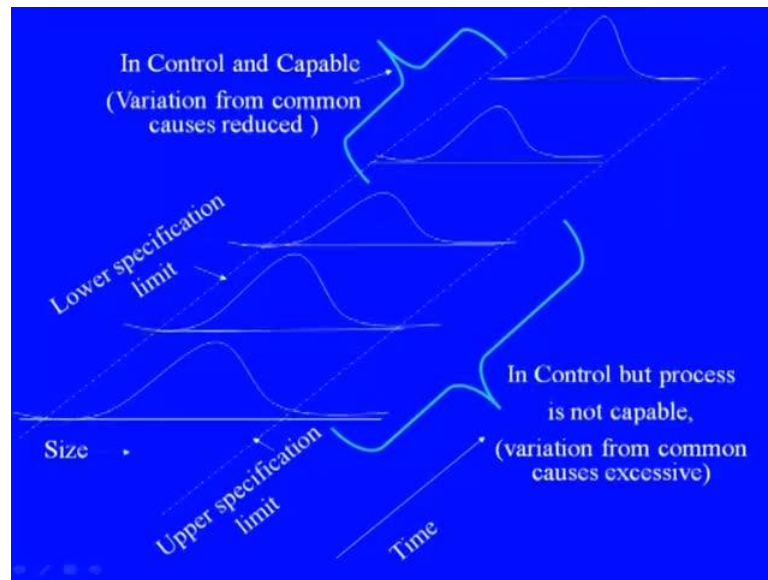
Controllable causes include those which can be reduced and are produced due to known causes such as human errors, machines setting, etcetera, etcetera. Uncontrollable causes or inherent variations that are beyond the control and are sometimes termed as natural variances, which exist in all processes.

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- Once the controllable causes are removed, to a large extent the process comes under control or is commonly termed as under statistical control.
- Then only the inherent causes remain.
- The following curves in the next slide demonstrate the same effects.

Once the controllable causes are removed to a large extent the processes come under control or a process is commonly termed as under statistical control. Then only the inherent causes remain, the following curves in the next slide demonstrate the same effects.

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So, these curves are on the screen. So, here so this is let us consider as size, and this is the time axis, then this is the distribution. This shows the distribution and if we consider two limits, that is one is lower specification limit in short, known as $l s l$ and the other one is upper specification limit in short $u s l$. Then we will call the process to be under control. Under statistical control, if the distribution is completely within these two limits. Now, here here we have seen the curve is going away slightly, that means we can interpret this.

So, in this case also it is although looks like within this, but there are little variations. So, in these cases we can interpret this as they are in control or these processes are in control, but the process is not capable. Since, they are going beyond this control limits. So, this can be variation of from common causes of excessive, on the other hand if we see the other two curves, normal distribution, these are normal distribution curves. So, if you see these curves as shown in the screen, they represent the processes which are under control and they are at the same time also capable, the process is capable. That means variation from common causes are reduced.

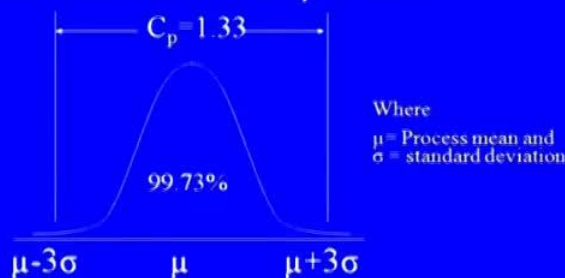
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- One way of ascertaining the process capability is through its measurement. For this the commonly used indices are C_p and C_{pk} .
- C_p simply makes a direct comparison of the process to the engineering requirements.
- Assuming the process distribution to be normal and the process average exactly centered between the engineering requirements.

One way of ascertaining the process capability is through its measurement for this the commonly used indices are C_p and C_{pk} . C_p simply makes a direct comparison of the process to the engineering requirements. Assuming the process distribution to be normal and the process average exactly centered between the engineering requirements.

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- A C_p index of 1 would give a capable process. However to allow a small room for process drift, the generally accepted minimum value for C_p is 1.33



A C_p index of 1 would give a capable process. However, to allow a small room for process drift, the generally accepted minimum value for C_p is 1.33. This can also be explained with the help of this figure, in which a normal curve, bell curve is shown. And

here with little drift on the both side, that is plus minus 3 sigma. So, mu represents the mean and from mu this is plus minus 3 sigma are allowed on both sides. That gives the C_p towards or to be equal to 1.33, which is generally acceptable. The C_p has two major shortcomings, it cannot be used unless we have upper and lower specification limits and it does not account for process centering.

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- The index of C_{pk} is more informative and accurate.
- It tells us, if the process is truly capable of meeting requirements.
- A C_{pk} value of 1 is required and 1.33 is preferred.

The index of C_{pk} is more informative and accurate. It tells us if the process is truly capable of meeting requirements A C_{pk} value of 1 is required and 1.33 is preferred. C_{pk} is closely related to C_p , the difference between C_p and C_{pk} represent, the potential gain from centering the process. Let us take an example to explain this importance of C_p and C_{pk} .

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Example:

- A particular process has a centre value is 1.00, Upper limit is +0.1, lower limit is -0.1 and the process mean is 1.02. From the trial experiments conducted, the σ as 0.03, then the
 - The C_p can be calculated as:
 - The $C_p = (USL-LSL) / 6 \sigma$
 $= (1.1-0.9) / 6 (0.03)$
 $= 1.11$

A particular process has a centre value, let us consider to be 1 and the upper limit is plus 0.1 while the lower limit is minus 0.1, and the process mean is 1.02. From the trial experiments conducted the sigma is obtained to be 0.03, then the C_p can be calculated as C_p equal to upper specification limit minus lower specification limit divided by 6 sigma, which comes out to be using these values just now mentioned, 1.11.

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- $C_{pk} = \min ((USL-\mu)/3\sigma, (\mu-LSL)/3\sigma)$
(whichever is lower)
 $= \min (1.1-1.02)/(3 \times 0.03),$
 $(1.02-0.9) / (3 \times 0.03)$
 $= \min (0.88 \text{ and } 1.33) \text{ (whichever is lower)}$
 $= 0.88$

On the other hand C_{pk} for the same situation at the same values given can be calculated as minimum of upper specification limit minus mean by 3 sigma and mean minus lower

specification limit by 3 sigma, whichever is lower. And this comes out to be 0.88 with the calculations using those values. Thus the lower one being 0.88 is considered to be the C_{pk} .

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- The lower one being 0.88 is the C_{pk} value.
- Hence the implication is that although the process is capable ($C_p > 1$), it is drifting away from the mean and needs more control to get better C_{pk} value.

Hence, the implication is that although the process is capable because the C_p is greater than 1, it is drifting away however from the mean and needs more control to get better C_{pk} value. This is the interpretation of this analysis. Now, let us summarize what we have studied in this session. In this session, we have discussed about few important terminologies or concepts used in manufacturing processes like; precision, then process capability. We have discussed different classifications of manufacturing have also been introduced. We hope this session was informative and interesting.

Thank you.