

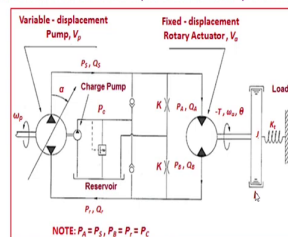
Oil Hydraulics and Pneumatics
Prof. Somashekhar S
Department of Mechanical Engineering
Indian Institute of Technology, Madras

Part 03: Pump controlled actuator system: Variable-displacement, Pump-controlled rotary actuator system
Lecture - 82
Pump-Controlled Hydraulic Systems

(Refer Slide Time: 00:23)

Variable-displacement Pump Control of a Rotary Actuator

- Variable-displacement, pump-controlled rotary actuator system is frequently used in the off-highway mobile equipment industry for propelling work vehicles without the use of standard transmissions
- This control system is often referred to as a “continuously variable hydrostatic transmission”; or, in more common language this system is often referred to simply as a “hystat”
- Figure shows control system utilizes a variable-displacement pump to control the output characteristics of a fixed-displacement rotary actuator



- In this figure the load to be moved by the actuator is shown as a single mass-spring-damper system with a load disturbance torque given by T



My name is Somashekhar course faculty for this course. Now, we will move on to the Variable-Displacement Pump Control of a Rotary Actuator. Variable-displacement pump-controlled rotary actuator system as I have told you frequently used in off-highway mobile equipment industry for profiling the work vehicles without the use of standard transmissions.

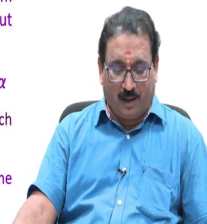
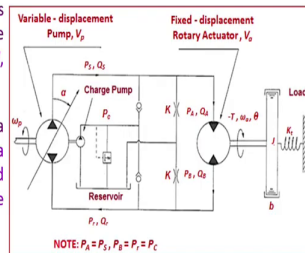
This control system is often referred to as a continuously variable hydrostatic transmission, or in more common language this system is often referred to as a hystat. Figure shows a control system utilizes a variable-displacement pump to control the output characteristics of a fixed-displacement rotary actuator.

Now, we will see here friends I have shown you the many components here. Here you will see now pump is a variable-displacement pump. The angular velocity is ω_p . Here you will see it is a the fixed-displacement rotary actuator. Again here I have connected the load arrangement which is shown as J , b damping and a spring k_t . Let us we will see now here. Also you will see a charge pump circuit I have shown here which is coupled to the main pump.

Let us will discuss this thing in detail. In this figure, the load to be moved by the actuator is shown as a single mass-spring damping system with a load disturbance torque T .

(Refer Slide Time: 02:21)

- The mass, spring rate, and viscous drag coefficient for the load are shown in Figure with the symbols J , b , and k_t respectively
- The rotary actuator is shown to be a fixed-displacement type with a volumetric displacement of the fluid per unit of rotation given by the symbol V_a
- The volumetric flow of hydraulic fluid into the actuator is controlled by the output flow of the variable-displacement pump
- This pump is constructed as a variable-displacement pump with V_p as the maximum volumetric displacement per unit of rotation and is typically operated at a fixed input speed, ω_p
- The variable displacement of the pump is achieved by altering the swash plate angle α
- In this design, the swash plate angle (α) may be positive or negative depending on which direction flow is being directed through the hydraulic circuit
- When the swash plate angle changes sign it is said to have gone "over center" and the direction of flow has been reversed



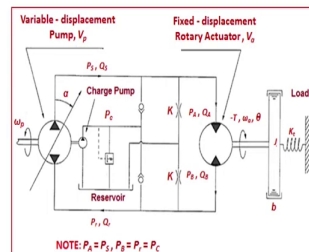
So, the mass, spring rate and a viscous drag coefficient for the load are shown in the figure with the symbols J , b , and k_t respectively. The rotary actuator system shown here it is a fixed-displacement type with a volumetric displacement of the fluid per unit rotation is given by the symbol V_a here. The volumetric flow of the hydraulic fluid into the actuator is controlled by the output flow of the variable-displacement pump.

This pump is constructed as a variable-displacement pump with a V_p as the maximum volumetric displacement per unit rotation and is typically operated at a fixed input speed ω_p . The variable-displacement of the pump is achieved by altering the swash plate angle α .

In this design, the swash plate angle α may be positive or a negative depending on which direction flow is being directed through the hydraulic circuit. When the swash plate angle is changes sign it is said to have gone over center and the direction of flow has been reversed.

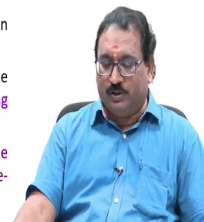
(Refer Slide Time: 04:10)

- Assuming for a positive swash plate angle of the pump (α), the pump flow is directed into side A of the actuator, then the load turn in a positive angular direction. The flow exit the actuator from side B



- Now for a negative swash plate angle of the pump (α), the pump flow is directed into the side B of the actuator and then then the load turn in a negative angular direction. The flow exit the actuator from side A
- These two volumetric flow rates into and out of the actuator are shown in Figure by the symbols Q_A and Q_B

- Referring to the Figure, the orifice flow passages from both sides of the circuit are shown with flow coefficients given by the symbol K
- These flow passages exist inherently within the system; however, they may also be designed intentionally for the purposes of directing fluid flow into the reservoir for cooling and filtration (coolers and filters are not shown)
- A charge pump circuit, shown in Figure is used to pressurize the low-pressure side of the control system and to sometimes provide an auxiliary pressure source for the variable-displacement pump control



Assuming for a positive swash plate angle of the pump α , the pump flow is directed into the side A of the actuator then the load turns in a positive angular direction. The flow exit the actuator from the side B. Now, for a negative swash plate angle α , the pump flow is directed into the side B of the actuator and exit the actuator from the A side vice versa here. These two volumetric flow rates into and out of the actuator are shown here as a Q_A and Q_B .

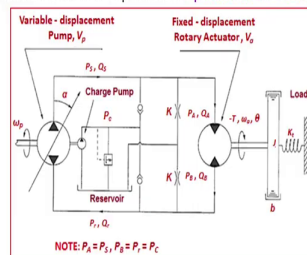
Referring to the figure, the orifice flow passages from both sides of the circuit are shown with flow coefficients given by the symbol K, low Reynolds number leakage coefficient it is.

These flow passages exist inherently within the system; however, they may also be designed intentionally for the purpose of directing the fluid flow into the reservoir for cooling and filtration which is not shown here.

A charge pump circuit shown in figure is used to pressurize the low pressure side of the control system and to sometimes provide an auxiliary pressure source for the variable-displacement pump controlled system.

(Refer Slide Time: 06:00)

- The charge pump is directly coupled to the main pump using a through drive shaft. This arrangement requires the charge pump to operate at the same angular velocity as the main pump.
- The charge pump itself is a fixed-displacement pump (usually a gear pump or a gerotor pump) that is used in conjunction with a relief valve for the purposes of providing makeup flow to the main pump inlet
- The pressure setting on the relief valve P_c is typically about 2 MPa, while the high-pressure side of the hydraulic circuit often operates at a pressure over 10 times this amount



- The check valves in Figure are used to block the high-pressure side to the charge circuit
- This feature ensures that the low-pressure side is always maintained at a constant pressure given by P_c and prevents pump cavitation during fast alterations of the swash plate angle α



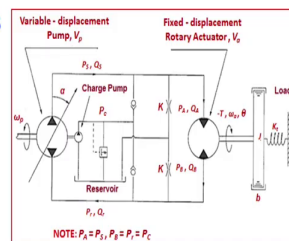
The charge pump is as I have told you directly coupled here, you will see directly coupled to the main pump using the drive shaft. This arrangement requires the charge pump to operate at the same angular velocity of the main pump. The charge pump itself is a fixed-displacement pump usually it is a gear pump or a gerotor pump that is used in conjunct conjunction with the relief valve for the purpose of providing the makeup flow to the main pump inlet.

The pressure setting on the relief valve the P c is typically about 2 MPa, while the high pressure side of the hydraulic circuit often operates at a pressure over 10 times this amount. The check valves shown in figure are used to block the high pressure side to the charge circuit.

This feature ensures that the low pressure side is always maintained at constant pressure given by P c, and prevents a pump cavitation during fast alteration of the swash plate angle alpha. After knowing the constructional details, let us we will move on load pressure analysis.

(Refer Slide Time: 07:36)

Load and Pressure Analysis



- **Load Analysis** : The equation of motion for the load may be written by neglecting the angular inertia of the actuator itself since it is much smaller than the actual torque that is generated by the actuator:

$$J\ddot{\theta} + b\dot{\theta} + k\theta = n_{act}(V_a(P_A - P_B)) - T \quad (1)$$

P_A and P_B	Fluid pressure on either side of the actuator
n_{act}	torque efficiency of the actuator
T	Load force exerted on the actuator

- P_A and P_B are the required inputs for adjusting the position of the load and hence we will derive these pressure terms in the following pressure analysis



Let us we will see the load analysis. Similar to previous one, the equation of motion for the load may be written by neglecting the angular inertia of the actuator itself, since it is much smaller than the actual torque that is generated by the actuator.

Now, here $J \dot{\theta} + b \dot{\theta} + k \theta = T$. Now we will see the torque efficiency of the motor η_t multiplied by the pressure multiplied by the volumetric displacement of the actuator and minus T .

Here P_A and P_B are the required inputs for adjusting the position of the load and hence we will derive these pressure terms in the following pressure analysis as we have done for the linear actuator, similar way we have to do it here.

(Refer Slide Time: 08:47)

- Pressure Analysis :** Assuming there are no or negligible pressure transients that result from the fluid compressibility in the transmission lines, the volumetric flow rate Q_A is given by (we know that $Q = AV$)...

$$Q_A = \frac{V_a}{\eta_{av}} \dot{\theta} \quad (2)$$


V_a	Volumetric displacement of the actuator
η_{av}	Volumetric efficiency of the actuator
- Referring to Figure, the actuator flow rate Q_A is given by :


$$Q_A = Q_s - K P_A \quad (3)$$

Q_s	Volumetric flow rate of the pump
K	Low Reynolds number leakage coefficient
- Already we know that volumetric flow rate of the variable displacement pump is mathematically defined as :

$$Q_s = \eta_{pv} (V_p \omega_p) \left(\frac{\alpha}{\alpha_{max}} \right) \quad (4)$$

η_{pv}	Volumetric efficiency of the pump
V_p	Volumetric displacement of pump per unit of rotation
ω_p	Instantaneous shaft speed of the pump
α_{max}	Maximum swash plate angle of the pump





Pressure analysis, assuming there are no or negligible pressure transients that results from the fluid compressibility in the transmission lines. The volumetric flow rate Q_A is given by already we know that $Q_A = AV$ – A into V . So, $Q_A = V_a \dot{\theta}$

dot. Here V_a is the volumetric displacement of the actuator; η_{av} is the volumetric efficiency of the actuator.

Referring to the figure the actuator flow Q_A is given by $Q_s - K P_A$; Q_s is a volumetric flow rate of the pump; K is the low Reynolds number leakage coefficient. Already we know that the volumetric flow rate of the variable-displacement pump is mathematically given by $\eta_{pv} V_p \omega_p$, now you will see here friends α by α_{max} .

Where α_{max} is the maximum swash plate angle of the pump, ω_p is a instantaneous shaft speed, and V_p is the volumetric displacement of the pump per unit rotation, η_{pv} is the similarly volumetric efficiency of the pump.

(Refer Slide Time: 10:19)

- Now substitute this Q_s in above equation (3), then Q_A becomes..

$$Q_A = \left(\frac{\eta_{pv} V_p \omega_p}{\alpha_{max}} \right) \alpha - K P_A$$

$$K P_A = \left(\frac{\eta_{pv} V_p \omega_p}{\alpha_{max}} \right) \alpha - Q_A$$

- Now substitute Q_A from equation (2) in the above equation and derive P_A as follows:

$$K P_A = \eta_{pv} \left(V_p \omega_p \right) \left(\frac{\alpha}{\alpha_{max}} \right) - \frac{V_a}{\eta_{av}} \theta \quad (5)$$

$$P_A = \frac{\eta_{pv} \left(V_p \omega_p \right)}{K} \left(\frac{\alpha}{\alpha_{max}} \right) - \frac{V_a}{\eta_{av} K} \theta \quad (5)$$

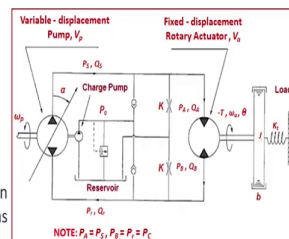
- As I have previously mentioned the check valves in Figure, are used to connect the low-pressure side of the hydraulic circuit to the charge circuit

- So the pressure on side B of the actuator is given by

$$P_B = P_c = P_c \quad (6) \quad P_c \text{ Fluid pressure in the charge circuit, which is normally about 2 MPa}$$

- Important Note:** From equation (5), a pump swash plate angle and an actuator velocity dependence for the fluid pressure on side A

- An adjustment of the pump swash plate angle is used to provide a control input to the dynamic load equation while the velocity term is useful in providing favourable damping characteristics for the system

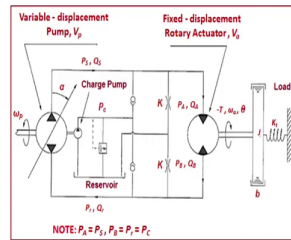


Now, substitute this Q_s in the above equation 3, then Q_A equal to I am getting this. Now, we will see what we will do, I will transfer minus $K P_A$ here because I want to find out P_A then Q_A will transfer here. Now, what we will do now next? Now, we will substitute the value of Q_A from the equation 2 which gives us $K P_A$ equal to I am substituting here Q_A . Now, what you will do now? P_A equal to you will transfer this K here. This is a very important equation we can call it as equation 5.

As I have previously mentioned the check valves in the figure are used to connect the low pressure side of the hydraulic circuit to the charging circuit. So, the pressure on side B of the actuator is given by P_B equal to p_r that is equal to P_c . The P_c is a fluid pressure in the charge circuit which is normally 2 MPa.

Important note here, you will see here from the equation 5, the pumps swash plate angle and the actuator velocity depends for the fluid pressure on side A. An adjustment of the pump swash plate angle is used to provide a control input to the dynamic load equation. while the velocity term is useful in providing a favourable damping characteristics of the system.

(Refer Slide Time: 12:08)



- **Summary:** To summarize the analysis of the actuation system shown in Figure, we substitute equation (5) and (6) of P_A and P_B in to equation (1) to produce the following equation of motion for the system:

$$J\ddot{\theta} + \left(b + \frac{\eta_m V_a^2}{\eta_m K} \right) \dot{\theta} + k\theta = \frac{\eta_m \eta_p V_a V_p \omega_p}{K \alpha_{min}} \alpha - \eta_m V_a P_c - T \quad (7)$$

- From the equation (7) it can be seen that the mechanical design of the rotary actuator and the volumetric displacement of the pump have a decisive impact on the overall dynamics of the hydraulic control system
- In particular, it may be seen from equation that these design parameters help to shape the effective damping of the system and to provide an adequate gain relationship between the input velocity of the pump and the output motion of the load



Quickly I will summarize this. To summarize the analysis of the actuation system shown in figure, we substitute the equation 5 and 6 for P A and P B in equation 1 to produce the equation of motion of the system. I am substituting now P A and P B in the equation number 1 which will gives us the complete equation.

From the equation 7, it can be seen that the mechanical design of the rotary actuator and the volumetric displacement of the pump have a decisive impact on the overall dynamics of the hydraulic control system. In particular, it may be seen from the equation that these design parameters help to shape the effective damping of the system and to provide an adequate gain relationship between the input velocity of the pump and the output motion of the load.

(Refer Slide Time: 13:16)

Mechanical Design Parameter



- Mechanical design parameter that must be specified in order to achieve satisfactory output of the system from a steady-state perspective
- Hence we will quickly see the important parameters to be considered in actuator design, pump design and input power
- **Actuator Design:** Usually, for a given application the maximum working torque is known along with the maximum working pressure in the system
- These two quantities can be used together with the steady-state form of equation 1 to design the fixed volumetric displacement rotary actuator and it is given by

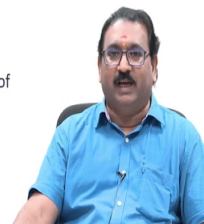
$$T = n_a (V_a (P_A - P_B)) \quad (8)$$

- The design specifications at the working force conditions are given by

$$T = T_w, P_A = P_s, \text{ and } P_B = P_c \quad (9)$$

- Substituting these quantities into equation (8) to arrive volumetric displacement of the actuator (V_a) as :

$$V_a = \frac{T_w}{\eta_a (P_s - P_c)} \quad (10)$$



Now, quickly we will see the mechanical design parameters, mechanical design parameter that must be specified in order to achieve the satisfactory output of the system for a steady-state perspective. Hence we will quickly see the important parameter to be considered in actuator design, pump design and input power. Actuator design, usually, for a given application the maximum working torque is known along with the maximum working pressure of the system.

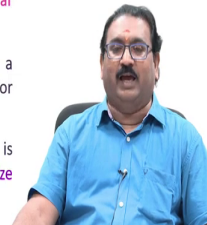
These two quantities can be used together with the steady-state form of equation 1 to design the fixed volumetric displacement rotary actuator. And it is given by the T equal to n_a into $V_a (P_A - P_B)$. We can call it as equation 8.

The design specifications at the working force conditions are given by T equal to T_w , P_A equal to P_s , and P_B equal to P_c – call it as equation number 9. Substitute these quantities

into equation 8 to arrive the volumetric displacement of the actuator V_a as T_w by $\nu_a f$ into P_s minus P_c , we can call it as equation number 10.

(Refer Slide Time: 14:50)

- These results may be used to design or select a rotary actuator that provides a sufficient working torque for a given supply pressure
- Since the rotary actuator is simply a hydraulic pump operating in a reverse direction, the type of actuator to be used may range from a gear type machine to an axial-piston machine
- Usually, the choice of the actuator is based on the performance that is needed from the actuator itself
- For instance, if a high operating efficiency is needed with a high starting torque, the best actuator selection would be a bent-axis axial-piston machine. Axial-piston machines (bent-axis or swash-plate type) must generally be used for operating pressures that exceed 20 MPa.
- On the other hand, if efficiency is not a significant factor in the application and if the pressures are below 20 MPa, a less-expensive option would be to select either a gear or a vane type actuator
- **Pump Design:** The pump used is a variable-displacement pump that produces a volumetric flow rate that is proportional to the swash plate angle of the pump. For these systems the input speed of the pump is maintained at a constant value ω_p
- In order to determine the maximum volumetric displacement of the pump it is common to specify a no-load velocity requirement for the rotary actuator and to size the pump in such a way as to achieve this velocity requirement



These results may be used to design or select a rotary actuator that provides a sufficient working torque for the given supply pressure. Since the rotary actuator is simply a hydraulic pump operating in a reverse direction, the type of actuator to be used may range from a gear type machine to an axial-piston machine. Usually, the choice of the actuator is based on the performance that is needed from an actuator itself.

For instance, if a high operating efficiency is needed with a high starting torque, the best actuator selection would be a bent-axis axial-piston machine. Axial-piston machine meaning a bent-axis or a swash plate type must generally be used for operating pressures that exceeds 20 Mega Pascal.

On the other hand, if the efficiency is not a significant factor in the application and if the pressures are below 20 Mega Pascal, a less-expensive option would be to select either a gear or a vane type actuator.

Pump design, the pump used is a variable-displacement pump that produces a volumetric flow rate that is proportional to the swash plate angle of the pump. For these system the input speed of the pump is maintained at a constant value ω_p . In order to determine the maximum volumetric displacement of the pump, it is commonly to specify a no-load velocity requirement for the rotary actuator and to size the pump in such a way as to achieve this velocity requirement.

(Refer Slide Time: 17:00)

- For the no-load case, the equation (5) may be used to show that the volumetric displacement of the pump must be designed so that:

$$V_p = \frac{\omega_o}{\omega_p} V_a \quad (11)$$

ω_o Specified no-load angular velocity for the system and where the volumetric efficiencies for the pump and actuator η_{pv} and η_{av} have been set equal to unity for the no-load condition of the system

- Equation (11), is the designed volumetric displacement of the actuator given in Equation (10) and ω_p is the angular velocity of the pump at the no-load condition specified in the problem
- From Equation 11, it can be seen that the ratio of the pump volumetric displacement to the actuator volumetric displacement V_p/V_o is equal to the no-load speed ratio or the gear ratio of the transmission ω_o/ω_p
- Though the pump size has been specified for the system based on certain system needs nothing has been said about the physical construction of the pump
- Since the pump is of the variable-displacement type it is most likely an axial-piston wash-plate type pump
- Nevertheless it may be any positive displacement pump that is constructed to vary its displacement based on the adjustment of some internal parameter of the machine
- For instance, a vane pump or a radial piston pump may be used with variable eccentricity dimension



For the no-load case the equation 5 may be used to show that the volumetric displacement of the pump must be designed. So, that V_p equal to ω_o naught by ω_p into V_a . ω_o

naught is specified no-load angular velocity of the system. And where the volumetric efficiency for the pump and actuator η_{pv} and η_{av} have been set equal to unity for the no-load condition of the system.

Equation 11 is the designed volumetric displacement of the actuator given in equation 10. And ω_p is the angular velocity of the pump at the no-load condition specified in the problem. From the equation 11, it can be seen that the ratio of the pump volumetric displacement to the actuator volumetric displacement that is V_p is to V_a is equal to the no-load speed ratio or the gear ratio of the transmission ω_{naught} by ω_p .

Though the pump size has been specified for the system based on a certain system needs nothing has been specified about the physical construction of the pump. Since the pump is of the variable-displacement type it is most likely an axial-piston swash-plate type pump.

Nevertheless it may be any positive displacement pump that is constructed to vary its displacement based on the adjustment of some internal parameters of the machine. For instance, a variable pump or a radial piston pump may be used with variable eccentricity dimension.

(Refer Slide Time: 19:16)

- Usually, the pump construction type is selected based on the required supply pressure of the system and the desired operating efficiency of the pump
- Axial piston pump tend to operate at higher pressures and provide a higher operating efficiency as compared to gear and vane type pumps
- On the other hand, axial-piston pumps tend to increase the upfront cost of the control system
- Now let us we will see the input power design....
- **Input power design:** The input power that is required to operate the hydraulic control system is given by the standard power equation



$$\Pi = \frac{V_p \omega_p (P_s - P_c)}{\eta_p} + \frac{V_c \omega_p P_c}{\eta_c} \quad (12)$$

η_p	Overall efficiency of the main pump given by the product of the volumetric and torque efficiency values $\eta_p = \eta_{vt} \cdot \eta_{pv}$
ω_p and P_s	Instantaneous operating angular velocity and pressures of the pump
P_c	Charge pressure of the system and second term on the right-hand side describes the power that is required to operate the charge circuit
η_c	Overall efficiency of the charge pump



Usually, the pump construction type is selected based on the required supply pressure of the system and the desired operating efficiency of the pump. Axial-piston pump tend to operate at high pressures and provide a higher operating efficiency as compared to gear and a vane type pumps. On the other hand, axial-piston pumps tend to increase the upfront cost of the control system.

Now, let us we will see the input power design. The input power that is required to operate the hydraulic system is given by the standard power equation as $\Pi = \frac{V_p \omega_p (P_s - P_c)}{\eta_p} + \frac{V_c \omega_p P_c}{\eta_c}$. Here η_p is a overall efficiency of the main pump which is given by $\eta_p = \eta_{vt} \cdot \eta_{pv}$.



ω_p and P_s , the instantaneous operating angular velocity and a pressure of the pump. P_c is the charge pressure of the system. And the second term here is there no it is describes the

power that is required to operate the charge circuit. Here η_c is the overall efficiency of the charge pump.

(Refer Slide Time: 20:58)

Concluding Remarks

- So in the today's lecture we have discussed in detail the followings
 - **Pump controlled hydraulic systems** – Linear actuator and Rotary Actuator
 - **Drive Concept**
 - **Hydrostatic Transmission** – Different configurations
 - **Fixed-displacement Pump Control of a Linear Actuator**
 - **Load and Pressure Analysis**
 - **Mechanical Design Parameter** – Key factors in Pump, Actuator and Input Power
 - **Hydro-Static Transmission (HST)** – Variable-displacement Pump Control of a Rotary Actuator
 - **Load and Pressure Analysis**
 - **Mechanical Design Parameter** – Key factors in Pump, Actuator and Input Power
- Ok friends, We will stop now and see you all in the next class
- Until then Bye Bye...



Navigation icons: back, forward, search, refresh, home, list, close

Now, let us we will conclude the today's lecture. So, in today's lecture, we have discussed in detail the followings. Pump controlled hydraulic system – here we have seen the linear actuator as well as rotary actuator. Different drive concepts, hydrostatic transmissions and a different configurations, fixed-displacement pump controlled linear actuator – here we have discussed in detail load and pressure analysis.

Then mechanical design parameter particularly on the pump, actuator and input power. Similarly, the hydrostatic transmission what we can call it is a variable-displacement pump controlled rotary actuator. Here also we will discussed already load and pressure analysis,

mechanical design parameters. Ok friends, we will stop now and see you all in the next class.
Until then bye bye.

(Refer Slide Time: 22:08)

**Thank You one and all
for Your kind attention**



Sarvejana Sukinobavanthu



Feel free to contact me.....

Somashekhar S.

Department of Mechanical Engineering
Indian Institute of Technology Madras
Chennai-600036, Tamil Nadu, India

Email: somashekhar@iitm.ac.in Phone : +91 - 044 - 2257 4681



Thank you one and all for your kind attentions. [FL]