

Oil Hydraulics and Pneumatics
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Basic Laws of Oil Hydraulics and Pneumatics

Lecture – 07

Part 1 : Pascal's law and its application – Hydraulic jack, Hydraulic brake and Numerical

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- Oil Hydraulics and Pneumatics**
- Hello friends, Very good morning to one and all
 - Hope you have enjoyed the Lecture 2
 - You have studied in the last lecture the following:
 - Basic Components of Oil Hydraulics
 - Basic Components of Pneumatics
 - Main Differences
 - Application Areas- Industrial Hydraulics and Mobile Hydraulics
 - Research Challenges
 - Status and Developments of Fluid Power System
 - In today's lecture we will **discuss/brush-up some of the Basics / Laws of Fluid Mechanics** mainly required to understand this Oil Hydraulics and Pneumatics Course



My name is Somashekhar, course faculty for this course. Hello friends, very good morning to one and all; hope you have enjoyed lecture 2. You have studied in the last lecture the followings; basic components of oil hydraulics, basic components of pneumatics, main differences between the oil hydraulics and pneumatics, application areas as a industrial hydraulics, where power pack is fixed and mobile hydraulics where power pack is moving along with the equipment.

Also we discussed the research challenges in the fluid power system and finally, we ended with status and development of fluid power system in the lecture 2. In today's lecture, we will discuss or brush up some of the Basics or Laws of fluid mechanics mainly required to understand this oil hydraulics and pneumatics course better.

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Lecture 3 **Organization of Presentation**

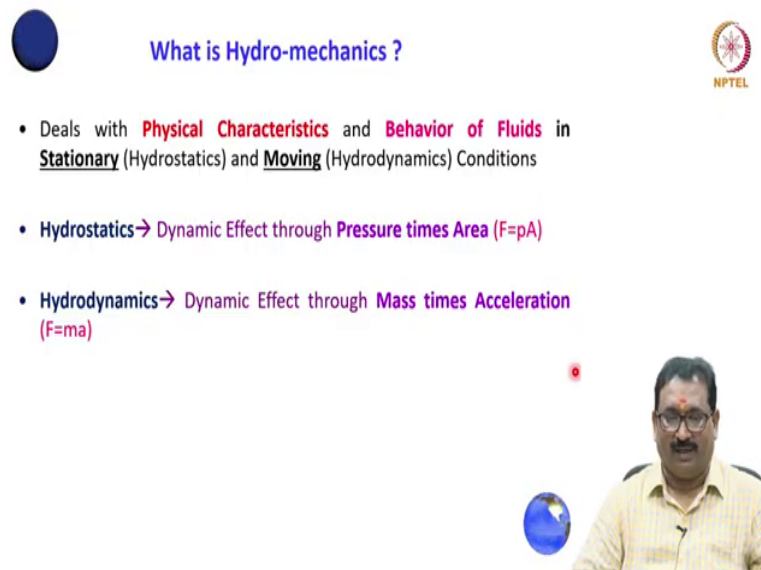
- **Hydro-mechanics**
- **Laws related to Hydraulics**
 - **Pascal's Law and its applications** – Hydraulic jack and Hydraulic press
 - **Law of conservation of Energy** – Bernoulli's theorem, Energy Equation and its applications in
 - ✓ Torricelli's theorem
 - ✓ Siphon
 - **Continuity Equation**
 - **Flow Configurations**
- **Laws Related to Pneumatics**
 - ✓ **Gas Laws**
- **Concluding Remarks**



This is organization of presentation of lecture 3. We will start with hydro mechanics, laws related to hydraulics; here we will discuss Pascal's law and its application, specifically for hydraulic jack and hydraulic press. Law of conservation of energy, here we will discuss some of the theorems like a Torricelli's theorem, siphon.

Later we will move onto continuity equation, flow configurations, laws related to pneumatics; here we will discuss various types of gas laws, Boyles law, Charles law, Gay-Lussac law and Ideal Gas laws. And finally, we will conclude this lecture with concluding remarks.

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What is Hydro-mechanics ?

- Deals with **Physical Characteristics** and **Behavior of Fluids** in **Stationary** (Hydrostatics) and **Moving** (Hydrodynamics) Conditions
- **Hydrostatics** → Dynamic Effect through **Pressure times Area** ($F=pA$)
- **Hydrodynamics** → Dynamic Effect through **Mass times Acceleration** ($F=ma$)

The slide includes a blue circle icon on the left, the NPTEL logo on the right, and a video inset of a man in a yellow shirt speaking, with a small globe icon next to him.

Can you please tell me friends, what is a hydro mechanics. Yes, it deals with physical characteristics and behavior of fluid in stationary and moving conditions. In stationary, we can call it as a hydrostatics; in moving fluids, we can call it as a hydrodynamic. Hydrostatics here, the dynamic effect through pressure times an area very important.

Please note here, in hydrostatic we are studying the dynamic effect in the fluid through pressure times an area, F equal to p into A . Similarly in the hydrodynamics, dynamic effect

through mass times acceleration; F equal to m into a ; please remember friends, in hydro mechanics we are studying the hydrostatics and hydrodynamics.

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Pascal's law



Blaise Pascal (1623-1662)

- Blaise Pascal (1623–1662) was a French philosopher, mathematician, scientist, inventor, and theologian developed a law applicable to **fluid inside a closed container (hydrostatics)**, known as **Pascal's principle or Pascal's Law**

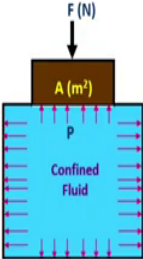


Now, we will move to the first and primary law Pascal's law. Blaise Pascal was a French philosopher, mathematician, scientist, inventor and theologian developed a law applicable to fluid inside a closed container meaning hydrostatics, known as Pascal's principle or a Pascal's law.

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Pascal's law


- It is **most fundamental** principle in fluid power and it deals with **Hydrostatics** → i.e. the **transmission of force through the confined fluid** under pressure
- It can be defined as "Pressure exerted on a confined fluid is transmitted **undiminished in all directions** and **acts at right angles** to the containing surfaces"
- Demonstrates as....



- **Pressure generated in the container, $P = F/A$ (N/m^2)**
- Where P is the pressure, F is the force applied and A is the area
- The most common units for these quantities in both US Customary and Metric (SI) Unit System are as follows:

Quantity	US Customary Unit	Metric (SI) Unit
Force (F)	Pounds (lbs)	Newtons (N)
Area (A)	Square Inches (in^2)	Square meters (m^2)
Pressure (P)	Pounds per square inch (lbs/in^2 , psi)	Newton per square meter (N/m^2 , Pa)

Note : $1 N/m^2 = 1 Pa$; $1 bar = 10^5 Pa = 0.1 MPa$



It is the most fundamental principle in fluid power and deals with hydrostatics; that is the transmission of force through a confined fluid under pressure. It can be defined as pressure exerted on a confined fluid is transmitted undiminished in all direction and it right angles to the containing surfaces.

It is easily demonstrated as follows. Take the closed container in the cylinder, fitted with the piston what I will call a plunger with an area A, apply the force F on the plunger, which in turn generate the pressure P; because pressure is force by an area. The generated pressure is transmitted undiminished and acts perpendicular to the wall surfaces.

This is one of the principle developed by the Pascal, the pressure generated in the container P equal to F by A, where P is the pressure, F is the force applied and A is the area.

Here the most common units, these quantities in both US customary and metric SI unit are as follows; you will see here friends, I am listing here in the first column the quantity, the major quantities force, area and pressure. US customary unit force is a pounds, area is a square inch, the pressure is pounds per square inch.

Still many of the devices, pressure gauges are in psi in a pounds per square inch. That is why I am listing US customary unit, but generally we will follow the metric unit SI unit, in which forces is a Newton, area is a square meter; meaning force by an area is Newton's per square meter or it is also known as a Pascal.

Please note friends, 1 Newton per meter square equal to 1 Pascal or 1 bar equal to 10 to the power of 5 Pascal or 0.1 mega Pascal. Please remember pressure in oil hydraulics represented frequently in Pascal, bar, and mega Pascal.

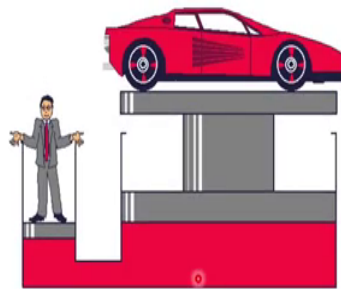
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Application of Pascal's Law

- The principle of Pascal's law was successfully applied by an English Engineer, **Joseph Bramah (1795)**, to develop a hydraulic press known as Bramah's Press, in which by applying a small input force a large output force was generated



Hydraulic Jack → Force Multiplication



Let us we will see the application of the Pascal's law. The principle of Pascal law was successfully applied by an English engineer Joseph Bramah to develop a hydraulic press known as a Bramah's Press, in which by applying a small input force you will generate the larger output force. That is what we known as the hydraulic jack, in all hydraulic jack to lift the vehicle body; we are using the force multiplication, which is given by the Pascal. How it is I will demonstrate it here.

This is a U tube, you will see the friends here it is a U tube; you will apply the small force here, you will see here how the vehicle body car is lifting. But you will remember friends, in the U tube the fluid is incompressible fluid; it is applicable to closed container what I will call hydrostatic.

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Hydraulic Jack

• When the System is in Equilibrium : ✓ Distance $s_1 > s_2$, since the area $A_1 < A_2$

<p><i>Pressures are equal</i></p> $P_1 = P_2$ $\frac{F_1}{A_1} = \frac{F_2}{A_2}$ $\frac{F_2}{F_1} = \frac{A_2}{A_1} = \frac{d_2^2}{d_1^2}$	<p><i>Displaced volumes are equal</i></p> $V_1 = V_2$ $s_1 A_1 = s_2 A_2$ $\frac{A_2}{A_1} = \frac{s_1}{s_2}$	$Q_1 = Q_2$ $A_1 V_1 = A_2 V_2$ $\frac{A_2}{A_1} = \frac{V_1}{V_2}$
<p><i>Work done, assuming no friction</i></p> $W_{in} = W_{out}$ $F_1 s_1 = F_2 s_2$ $\frac{s_1}{s_2} = \frac{F_2}{F_1}$	<p><i>All together</i></p> $\frac{F_2}{F_1} = \frac{A_2}{A_1} = \frac{d_2^2}{d_1^2} = \frac{s_1}{s_2} = \frac{V_1}{V_2}$	

Let us we will see now, some of the parameter how we will arrive from the hydraulic jack. As I have told you here F_1 is a force acting on the plunger, this is a U tube and another other side is the large piston of area A_2 .

And when you apply the small force F_1 on the plunger, it will generate the P_1 pressure; the P_1 pressure as we know in the closed container, it will act perpendicular to the wall surface and undiminished, which in turn acts on the larger piston area, which will generate the large pressure to lift the loads.

Please remember here friends, when I will apply the force F_1 , the piston will move to this by an displacement s_1 , which in turn it will lift the larger piston by the distance s_2 . Please note here s_1 is greater than s_2 ; because A_1 is less than A_2 .

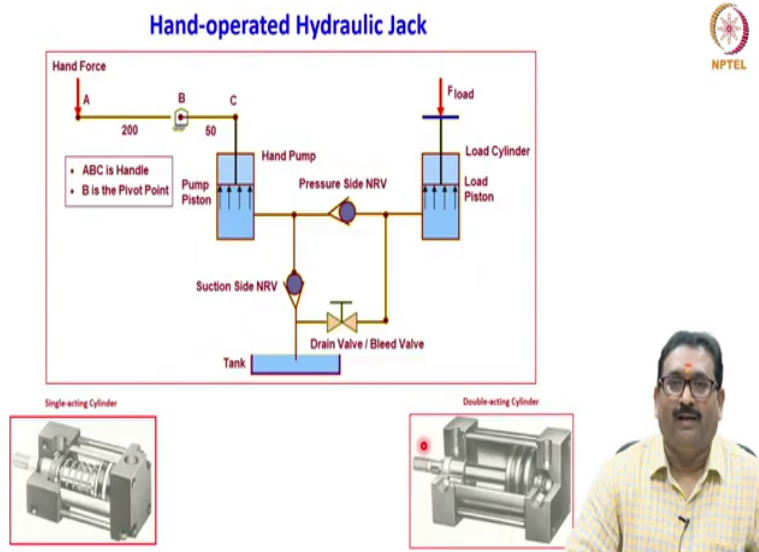
So, when the system is in equilibrium friends, when the system is in equilibrium will arrive the pressures are equal P_1 equal to P_2 ; the P_1 already know that forced by any area, here it is P_1 is F_1 by A_1 , here the pressure P_2 is F_2 by A_2 . Or you will modify here by cross multiplying the parameter F_2 by F_1 equal to A_2 by A_1 . What is A_2 ? A_2 is π by $4 d_2^2$ square, A_1 is π by $4 d_1^2$ square.

After cancelling some of the term, we will get d_2^2 square by d_1^2 square. Similarly, the displaced volumes are also equal in equilibrium condition; meaning what? The volume displaced V_1 equal to V_2 ; what is a V_1 ? s_1 into A_1 here and here it is s_2 into A_2 ; after cross multiplying, I will get A_2 by A_1 equal to s_1 by s_2 .

Similarly, the quantity of fluid Q_1 equal to Q_2 meaning here $A_1 V_1$ equal to $A_2 V_2$; meaning what it is friends? A_2 by A_1 equal to V_1 by V_2 . Similarly, the work done assuming no friction between the valves and a tubes, W_{in} , here W_{in} is equal to W_{out} . Meaning what friends it is? F_1 into s_1 equal to F_2 into s_2 ; after cross multiplying I will get s_1 by s_2 equal to F_2 by F_1 .

The finally friends, these parameter pressures are equal, displacements are equal, the volume flow equal and work done equal; meaning it is all together I will write here F_2 by F_1 equal to, you will see here F_2 by F_1 equal to A_2 by A_1 is equal to d_2^2 square by d_1^2 square, which is equal to s_1 by s_2 and V_1 by V_2 . Please remember friends, when the system is in equilibrium, all these parameters follows this.

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Now, I will explain you to you the simple hand operated hydraulic jack. Let us you will see here friends in the schematic diagram shown here, it consists of the hand pump and the load cylinder. The hand pump is connected to the hand lever here, you will see the ratio 200 to 50; A, B, C is a handle and B is a pivot point friends.

And this hand pump is connected to the what I will call, this is a power pack, it is a suction side non return valve, tank and a drain valve or a bleed valve; why it is required I will tell you. You will see friends here, these are the main components in the hand operated hydraulic jack. How it operates friends?

When you will apply the force here what happens, it is intern connected to the piston of the hand pump, when you will push this, this will move. Immediately what happened, here the suction will create; it will lift the fluid from the tank, it will enter here. When you will move

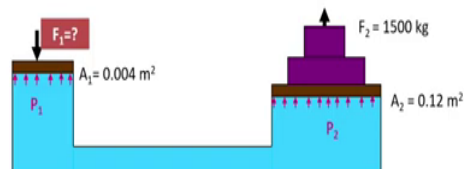
up what happens friends, the fluid sucked here; it will go to the load cylinder through the pressure side non return valve; it will not go here, because it is a only unidirectional.

It will allow the flow from here to here, not from here to here; then only when you will move up, whatever the fluid is there, it will push to the load cylinder through the pressure side NRV. Then what happen, here whatever the load you will kept here vehicle body, it will lift up. But when you want to lower the vehicle, what it will do?

If to lower the vehicle, the fluid will not go through this NRV; because it is unidirectional. Then only way is to lower the weight what you will do; you will open the drain valve, manually drain valve or a bleed valve you will open, then fluid present here it will go to the tank directly. This is a very very simple hand operated hydraulic jack works on the closed container; fluid is in the closed container, not open flow.

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1. A vehicle is to be lifted by a hydraulic jack. The mass of the vehicle amounts to 1500 kg. The small and large piston areas are 0.004 m² and 0.12 m². Calculate the **minimum force required** at the smaller piston ?



• When the System is in Equilibrium :

$$P_1 = P_2$$

$$F_1/A_1 = F_2/A_2$$

$$F_1 = (A_1/A_2) \times F_2$$

$$= 500 \text{ N}$$

$$F_2 = m \cdot g$$

$$= 1500 \text{ kg} \times 10 \text{ m/s}^2$$

$$= 15000 \text{ N}$$



Let us we will see now, to understand this I will give you a simple numerical here; a vehicle is to be lifted by a hydraulic jack. The mass of the vehicle amounts to 1500 kg. The small and larger piston areas are 0.004 meter square and 0.12 meter square. Calculate the minimum force required at the smaller piston.

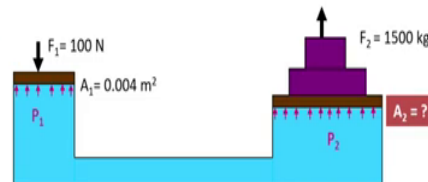
As I have told you it is a hydraulic jack, the figure is like this; here the given parameters are A_1 is given and A_2 is given and the load is given. Then what is our objective? Our objective is to calculate what is a minimum force required to lift the 1500 kg load. As we know that when the system is in equilibrium, P_1 equal to P_2 ; what is a P_1 ?

F_1 by A_1 equal to F_2 by A_2 . Then what is a F_1 ? F_1 equal to A_1 by A_2 into F_2 . Meaning how much I will get? F_2 F_1 required F_1 required to lift the F_2 is 500 Newton. Please note here, because mass of the vehicle is given as in kg; what I did? I multiplied by a with g 9.81; I am taken round figure as a 10 meter per second square, you will get this.

Please note friends, by applying the very small force; how much? 500 Newton, I am able to lift 1500 kg or 15000 Newton, using the confined incompressible fluid in the U tube.

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2. It has been proved that the Force F_1 of 100 N is too great for actuation by hand lever. **What must be the size of the piston surface A_2 be** when only a piston force of $F_1 = 100$ N is available? The mass of the vehicle amounts to 1500 kg. The area of small piston is 0.004 m^2 .



- When the System is in Equilibrium :

$$P_1 = P_2$$

$$F_1/A_1 = F_2/A_2$$

$$A_2 = (F_2/F_1) \times A_1 \\ = 0.6 \text{ m}^2$$

$$F_2 = m \cdot g \\ = 1500 \text{ kg} \times 10 \text{ m/s}^2 \\ = 15000 \text{ N}$$

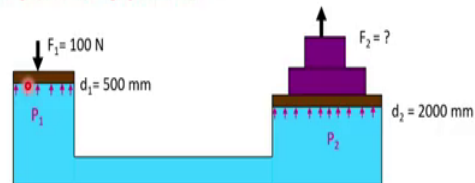


One more example we will see now, it has been proved that the force F_1 of 100 Newton is too great for actuation by hand lever. What must be the size of the piston area A_2 be when only a piston force of F_1 equal to 100 Newton is available? Again as usual the mass of the vehicle amounts to 1500 kg, the area of the small piston given is 0.004 meter square. As usual, what are the things given here friends?

Again I drawn here schematic of the hydraulic jack; here the given parameter is F_1 is given, A_1 is given and F_2 is given. Now, our objective is to find out, what is the area of the larger piston to lift this load? As usual when the system is in equilibrium P_1 equal to P_2 and F_1 by A_1 equal to F_2 by A_2 ; then A_2 is 0.6 meter square, correct. Very simple friends it is; any problem we will do by understanding the basic principle of Pascal's law applicable to hydraulic jacks.

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3. A downward force of 100 N is applied to the small piston with a diameter of 500 mm in the hydraulic lift system. a) What is the **upward force exerted** by the large piston with a diameter of 2 m. b) What is the **mechanical advantage** of the hydraulic lift ? c) If the input force of 100 N pushes the small piston down by 2 m, **how high will the large piston rise ?**



a) Pressures are equal

$$P_1 = P_2$$

$$\frac{F_1}{A_1} = \frac{F_2}{A_2}$$

$$\frac{F_2}{F_1} = \frac{A_2}{A_1} = \frac{d_2^2}{d_1^2}$$

$$F_2 = \left(\frac{d_2^2}{d_1^2}\right) F_1 = \left(\frac{2000^2}{500^2}\right) \times 100 = 1600 \text{ N}$$

b) Mechanical Advantage M_A

$$M_A = \frac{F_2}{F_1} = \frac{1600}{100} = 16$$

c) Already we know that

$$\frac{F_2}{F_1} = \frac{A_2}{A_1} = \frac{d_2^2}{d_1^2} = \frac{s_1}{s_2} = \frac{V_1}{V_2}$$

$$\frac{F_2}{F_1} = \frac{s_1}{s_2}$$

$$s_2 = \left(\frac{F_1}{F_2}\right) s_1 = \left(\frac{100}{1600}\right) 2000 = 125 \text{ mm}$$



I will show you one more example for easy understanding, a downward force of 100 Newton is applied to the small piston with a diameter of 500 mm in a hydraulic lift system. What is the upward force exerted by the larger piston with a diameter of 2 meter? What is the mechanical advantage of the hydraulic lift? If the input force of 100 Newton pushes the small piston by 2 meter; how high will be the large piston rise?

Same as usual it is same here friends, what are the things here; diameter of the smaller piston is given as 500 mm, diameter of the larger piston is given as 2 meter, meaning 2000 mm I am writing. Now, F 1 is also given small force; our objective is to find out what is my F 2 and mechanical advantages and what it is and if the small distance if will give, what is a the distance moved up?

Now, we will see as we know that, pressures are equal when the system is in equilibrium P_1 by P_2 ; then after substituting all, I will get F_2 equal to 1600 Newton. Similarly, the mechanical advantage is given by the ratio of F_2 by F_1 ; already F_2 I am getting here 1600, F_1 I know already 100, meaning mechanical advantage is 16.

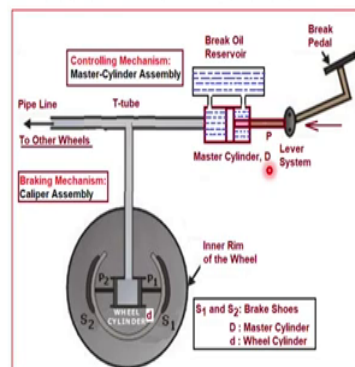
Similarly, already we know this formula in the previous slide; then what is our objective? Our objective is to find out what is s_2 here, if I know the s_1 here; you will get s_2 equal to 125 mm. Any parameter if you will vary in this in the problem, you are able to calculate the unknown parameter in the hydraulic jack; very simple friends it is, very very simple.

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Hydraulic Brake



- **Hydraulic Brake** uses brake fluid, typically containing ethylene glycol to transfer pressure from the **Controlling Mechanism (Master Cylinder Assembly)** to the **Braking Mechanism (Caliper Assembly)**
- Figure shows the **Schematic of Braking Mechanism**



Now, we will see one more application of the Pascal's law is a hydraulic brake. You come across this in the two wheeler as well as in the 4 wheeler hydraulic brake; very very accurate,

they will stop at a instant at the same place. This is the beauty of hydraulic brake; how it will works, we will see now.

As we know that, hydraulic brake uses a brake fluid, typically a ethylene glycol to transfer a pressure from the controlling mechanism to the braking mechanism. Here controlling mechanism is a master cylinder assembly, braking mechanism is a caliper assembly. I will show you how these systems are connected in the hydraulic brake.

Figure shows us schematic diagram of the braking mechanism; you will see friends as I have told you here, there are two important devices; master cylinder assembly, what you call a controlling mechanism and another is a braking assembly, caliper assembly in the wheel side.

Understand here friends, what are the components are there you will see here; here this is what they will call break pedal, then it is connected to the lever through the piston. This is a master cylinder having diameter capital D , which is connected to the oil reservoir, ethylene glycol or a brake fluids are here.

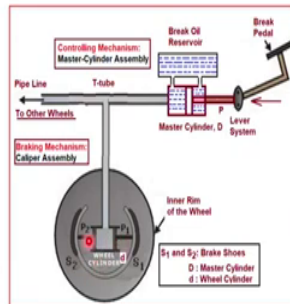
And then what happens, the whatever when you will push this when you apply this, it will move; then whatever the fluid is there, it will come here and push the what it is. Here you will see the braking mechanism, here the wheel cylinder is there, diameter is D here; P_1 and P_2 are the two piston connected to the what is that brake shoes S_1 and S_2 .

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Hydraulic Brake

• It mainly consists

- Brake Pedal with Lever System
- Pushrod (P)
- Master Cylinder (D) With Piston
- Fluid Reservoir
- Reinforced Hydraulic Lines: T-tube



- Brake Caliper assembly → Caliper pistons (P1 and P2), a set of brake pads/brake shoes (s1 and s2) and a rotor (also called a brake disc or drum attached to an axle)



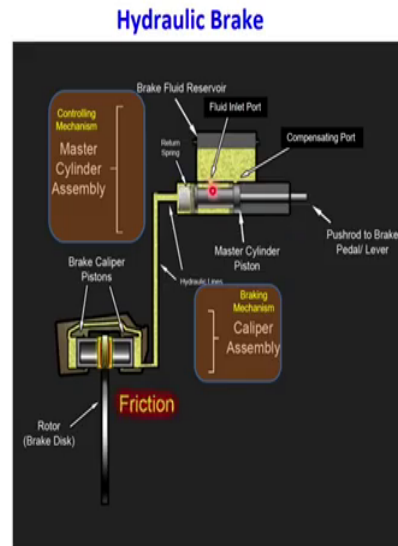
How it is I will explain to you in the next slide. This is a mechanism what I have shown in the previous slide. Already we know that, it consists of a brake pedal; see here a brake pedal with a lever P, push button, push rod it is, P is nothing but the push rod, the master cylinder diameter with piston.

Fluid reservoir correct and the reinforced hydraulic T tube; then you will see here friends, when you will push, some among the fluid go here, some of the fluid will go to the next wheels here, there are so many wheels are there. For example, in case of that 4 wheeler, it will go to the other wheels.

Then here you will see the braking mechanism or caliper assembly, it consists of what is this; caliper piston you will see P 1 and P 2 caliper piston, a set of brake pads s 1 and s 2 or a brake

shoes and a rotor correct, it is connected it is connected to the rotor it is, inner rim of the wheel, correct.

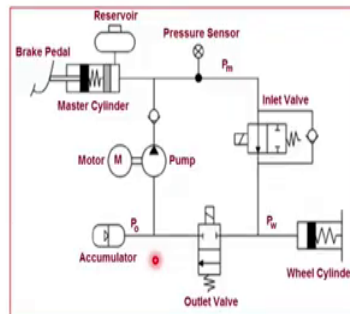
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Now, we will see this the how it operates, I have shown you the very simple sketch here; when he will apply the push rod here, what happens here friends? You will see whatever the fluid is there here, it will go to the either side of the piston P 1 and P 2. P 1 and P 2 will push the rotating disk. Then already we know that the pressure generated here is acting equally in both the cylinder piston; meaning at a time the wheel will be stopped, because it is incompressible fluids, that is a beauty of in the hydraulic brake.

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Simple Hydraulic Brake Circuit



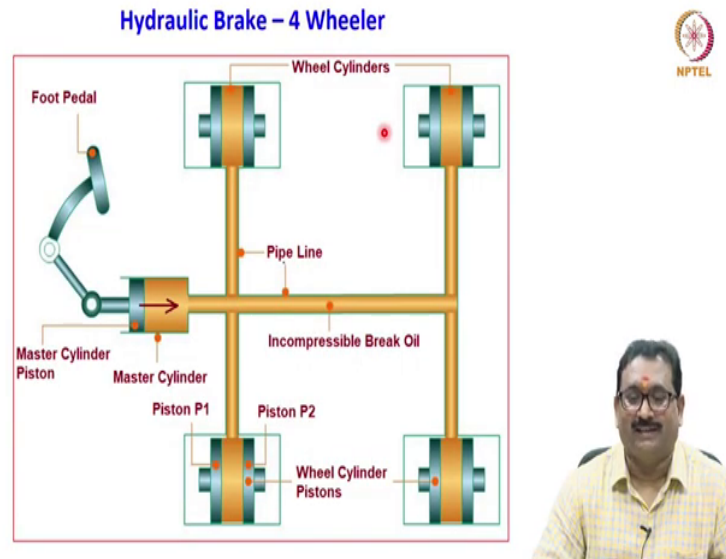
Hope you understood this, next we will I will show you the simple schematic diagram of the brake circuit. Here as usual as I have told you here, it is you will see here, the brake pedal I have shown here, it is a cylinder correct, the master cylinder; when you will push this, the fluid will come here through the 2 by 2. So, Raynaud approached the valve it is, then it will go to the wheel cylinder.

When brake will release here, fluid will come here, it will lift here, it will go to that reservoir again here. The some of the things are there here, motor and pump and accumulators and outlet valves.

This is a simple hydraulic brake circuit; these circuits will come to know that, when we are dealing with the circuit design. Now, we will understand only this; what is required here is,

the brake pedal is connected to the master cylinder, then it is connected to the wheel cylinder through the sum of the valves, ok.

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Now, we will see the schematic diagram in which the same hydraulic brake for the 4 wheelers, you will see here. Very simple here friends, again the foot pedal is there; from the foot pedal when you will, this is a master cylinder and these are the what it is the wheel cylinders, all are wheel cylinder, 4 wheel cylinders. Here you will see here, the yellow what I have shown, here it is moving the braking fluid.

When you will push this, the pressure generated here is acting equally without diminishing on these areas; automatically it will push the rod, piston rod to stop the wheel rotation immediately, ok.

But you will remember here, the Pascal's law is applicable to the closed contained fluids, not the open fluids; as because as we know in the Pascal law, when you will apply the pressure through the force, the generated pressure is acting equally in all the sides without diminishing. The same principle is used in the hydraulic brake.