

Experimental Stress Analysis
Prof. K. Ramesh
Department of Applied Mechanics
Indian Institute of Technology - Madras

Lecture - 29
Strain Sensitivity of a Strain Gauge, Bridge Sensitivity, Rosettes

We have started our discussion on the method of strain gauges, and we looked at to measure strain at a point you do not have a material which has a very high resistance, so that I take a small pack of material and then find out what is the strain at a point of interest. I need to have a minimum length of wire for me to give changes that could be measured, and when I have a long wire I cannot paste it on the specimen and make the strain measurement.

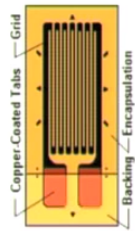
I have to necessarily make it as the loop, make it as a grid and then only make a strain measurement, and I also caution a single strain gauge provides you only a component of strain along its gauge length, if you have to measure strain as a tensor suppose I want to do it on a free surface, I need to find out 3 independent quantities, so I need at least 3 strain gauges for me to measure state of strain at a point, so you need to understand these 2 differences.

And in the last class we had developed, what is a strain sensitivity of a single conductor, the idea of the discussion was to understand the role of various parameters. I also mentioned in strain gauge instrumentation any effect due to thermal influence need to be looked at very carefully, and we are measuring very, very small quantities, so any small changes also can have a significant effect. So now we look at what is the strain sensitivity of a strain gauge.

(Refer Slide Time: 02:11)

Strain Sensitivity of a Strain Gauge

- When the conductor is formed into a grid to reduce its length, the strain sensitivity changes and the gauge exhibits sensitivity to both axial and transverse strains.



Courtesy: Vishay Micro-Measurements

- The response of the gauges subjected to ϵ_a , ϵ_t and γ_{at} is given by

$$\frac{dR}{R} = S_a \epsilon_a + S_t \epsilon_t + S_\gamma \gamma_{at} \quad \longrightarrow (1)$$



Because we have looked at the conductor is formed into a grid to reduce its length the strain sensitivity changes, because it is now made into a grid the gauge exhibits sensitivity to both axial and transverse strains, gauge latest look at closely what the strain gauge is, you know I have a metal foil gauge shown here, because it is made up of a metal foil I have a luxury when I make a loop, I make this n loop as thick.

And I said earlier that when you have this n look as thick, the reason why we do this is to reduce its sensitivity to transverse strain by making the loop wider we reduce the resistance, so its sensitivity to transverse strain will be minimum. And when you look at the strain gauge like this you have markings like this, these are needed for aligning the strain gauge at the point of interest, and you also find that there is backing, the metal file supported by a backing.

And you have a very large copper coated tabs for soldering, and also you find in this strain gauge you also have a encapsulation this is needed in certain applications where the environment has a negative role to play, you need to protect the gains from the influence of environment, and this provides you one type of improvement over normal strain gauges, there are also other methods. And the advantage of metal foil is I can make the metal foil as thin as possible so that increase the resistance.

We have also seen strain gauges are available at 120 ohms, 350 ohms and so on, so when you want to go for higher values of resistances you can do only a comfortably in a metal foil gauge, you have a provision to do that. And as engineers we need to bring in approximations, first observation is whatever the resistance change dR/R will now be a function of axial strain, function of the transverse strain, as well as the shear strain.

You know in many problems what we have seen, we will first neglect the shear effects, because we will always say shear effect is there but its influence is quite small, so as a first approximation let us neglect it and proceed. So we will follow the same route here also, in general $dR/R = S_a \epsilon_a + S_t \epsilon_t + S_s \gamma_a$, and note the way the subscripts are denoted here, I used the small letter a.

So the moment I use this I am talking of a strain gauge and not a conductor, for the conductor the axial sensitivity is given as S suffix capital A, when I take it as a grid the axial sensitivity is given as S_a , but even this kind of expression is not convenient for users, the users want a very, very simple representation of change of resistance to the strain, not only this many users may not even know how the strain gauge instrumentation really calculates.

They would have only see this strain reading because instrumentation is so well developed when you connect the strain gauge, you look at the strain reading it is all done by the electronics, and this is where people mistake that anybody can do and perform an experiment. And I caution when you are doing strain measurement you are talking of microstrain which is 10^{-6} , and you will also have to measure the change in resistance which is again 10^{-6} .

It is a very small quantity first if you recognize this fact, it will go to a long way in respecting the procedures given by the manufacturer, because many times you do not want to follow a procedure you want to quickly go and make measurement that will not do when you want to do strain gauge instrumentation.

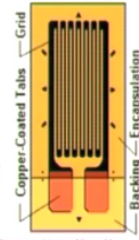
(Refer Slide Time: 07:35)

Transverse Sensitivity Factor, Gauge Factor – Definitions

- In general S_s is small and can be neglected

$$\frac{dR}{R} = S_a (\epsilon_a + K_t \epsilon_t) \quad \text{--- (2)}$$

$$K_t = \frac{S_t}{S_a} \quad K_t \text{ is the transverse sensitivity factor}$$



Courtesy: Vishay Micro-Measurements

- Strain gauge manufacturer supplies a gauge factor S_g which is experimentally determined for an uniaxial stress field, for that particular batch.

$$\frac{dR}{R} = S_g \epsilon_a \quad \text{--- (3)}$$



Copyright © 2005 Prof. K. Ramesh, IIT Madras, Chennai, India

You should know, what is the constraints that you have. And now we look at how we simplify the set of expression, and I said earlier we will start with the first approximation that shear effects are neglected, so S_s is small and can be neglected, and we have also done one more modification we have taken out S_a from this and brought in another factor which is called K_t which is defined as S_t/S_a , this is just out of convenience.

And what you find here is the change in resistance to the resistance of the gauge is now $=S_a \epsilon_a + K_t \epsilon_t$, in fact if you go and look at carefully the specification given by the strain gauge manufacturer, he would provide you what is known as gauge factor, he will also provide you the transverse sensitivity factor that is how manufacturers give out their parameters define in the same page, and that is where you have what is defined as K_t .

And typically we want to keep K_t as small as possible while designing the grid, and we will also see later by making almost $=$ the Poisson's ratio of the base material, you can have what is known as the stress gauge. See we have only looked at strain gauge why you call that strain gauge, because it is primarily gives you the strain, and when you say stress analysis there are also occasions where I want to directly get the stress.

So people look that cannot we not make a stress gauge, so that whatever the electrical signals that I record is proportional to stress measurement, so there you play with the transverse

sensitivity, you want to make it very high. In this case general strain gauge, we would like to have the grid to measure strain primarily along the strain gauge that makes our life simple. So you have a definition of what is the transverse sensitivity factor.

And as I said the user want to have a much simpler expression and the strain gauge manufacturer supplies what is known as a gauge factor, which is given as S_g , and what you have is you have $dR/R = S_g \cdot \epsilon_a$, and what does the manufacturer do? He performs an experiment and determines, what is the value of S_g . Our focus is we want to find out the component of strain along the gauge length, suppose I call that as ϵ_a .

Now I have a very simple expression where change in resistance to original resistance is related by a factor S_g to the linear strain, and we have to look at what is the interrelationship between S_g and S_a , this S_a , S_t , S_s comes directly from our understanding that we take a conductor and then perform experiment pull it and then determine the strain sensitivity, now you adopt the same thing for a grid, the grid is sensitive to axial, transverse, as well as shear.

so you bring in 3 factors, but from user point of view he does not want to look at all these quantities, he wants some much simpler expression and that is also given by the manufacturer where he simply says $dR/R = S_g \cdot \epsilon_a$. And once you have to use this expression you should know, what are the constraints behind it, because I have been saying Poisson's ratio has a role to play in all the experiment technique.

(Refer Slide Time: 12:01)

Experimental Determination of Gauge Factor S_g

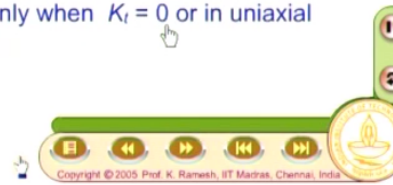
$$\varepsilon_t = -\nu_0 \varepsilon_a$$



- For the calibration beam material $\nu_0 = 0.285$

$$S_g = S_a (1 - \nu_0 K_t)$$

- S_g relates dR to axial strain only when $K_t = 0$ or in uniaxial stress field where $\nu_0 = 0.285$.



And what does the manufacturer do? He takes a cantilever puts the strain gauge, and for a given load or a set of loads he would find out the strain, from the analytical solution you would be able to correlate and establish the parameters. When you do an experiment like this Poisson ratio of the calibration material comes into play, because I have always said a cantilever beam experiences any axial stress, but biaxial strain you should never forget that.

And the transverse strain is controlled by the Poisson's ratio, so without your knowledge Poisson's ratio enters into a strain gauge instrumentation it is very important, if you only use the equipment and read the strain you miss out how the whole technology has developed, you should know the theory behind it. And since I know the axial strain I can find out the transverse strain simply as $\varepsilon_t = -\nu_0 \varepsilon_a$, and for the calibration beam material ν_0 is given as $\nu_0 = 0.285$.

And you get an expression for S_g as a function of axial sensitivity and transverse sensitivity you have here transverse sensitivity factor, so I have $S_g = S_a (1 - \nu_0 K_t)$, so what does this signify? Only if you conduct an experiment on a specimen material which has the same Poisson ratio your expression $dR/R = S_g \varepsilon_a$ is a valid expression, for all other cases the mismatch of Poisson ratio will influence in some fashion. I had also raised this when we discuss brittle coatings, one of the suggestions I said was the interplay of Poisson's ratio was quite involved.

So the recommendation is if I have to do it on a prototype which I am going to do it repeatedly, it is better to take the prototype material make a calibration specimen, and evaluate the failure strain in the case of brittle coating, on similar lines do the similar exercise and find out S_g , what you should remember is S_g is experimentally calculated by the manufacturer, it is not a theoretical quantity and Poisson ratio mismatch can affect all your strain gauge instrumentation you should never forget that.

And again I want to emphasize in all the coating techniques you use calibration specimen, you use cantilever beam, and in the case of photoelastic coating you determine K , in the case of brittle coating you determine ϵ_d , in the case of strain gauge you do not do the experiment the manufacturers supplies you, because he supplies you S_g and then you will make your life simple, and you follow his recommendation in bonding the strain gauge and directly use S_g for all your strain gauge instrumentation.

Because normally you do not do performance and determined S_g , because he finds it out for a batch, and it is reasonably a value which does not change like what you seen in the case of polymers with change the properties slowly, so it is mandatory that you perform your own experiment. So from batch to batch the value of S_g and vary, you should know that. So if I have a transverse sensitivity 0 a very ideal strain gauge, then I have no problem.

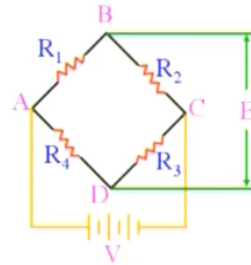
I can have S_g , I will have from this expression S_g is directly related to S_a when $K_t=0$, but K_t will have some value which is very small but in critical applications you may also have to correct for the transverse sensitivity effects. We will also see how do we account for transverse sensitivity error later.

(Refer Slide Time: 16:57)

Wheatstone Bridge

$$V_{AB} = \frac{R_1}{R_1 + R_2} V$$

$$V_{AD} = \frac{R_4}{R_3 + R_4} V$$



And I have been saying that you need to measure very small quantities, and how do you measure the change in resistance, and in your high school physics you would have seen about use of wheatstone bridge, it is a very popular and simple yet robust method of measuring small changes in the resistance. And what you have here? I have 4 arms of the bridge, I have arm AB, BC, CD and DA, and what I do is I supply voltage between the points A and C.

And I measure what is the potential difference in points B and D that is what I measure. And in your earlier class you would have also seen how to find out the voltage AB and voltage AD, and these are given as this expressions, but our focus is different.

(Refer Slide Time: 18:10)

Wheatstone Bridge

....contd

$$E = V_{BD} = V_{AB} - V_{AD} = \frac{R_1 R_3 - R_2 R_4}{(R_1 + R_2)(R_3 + R_4)} V$$

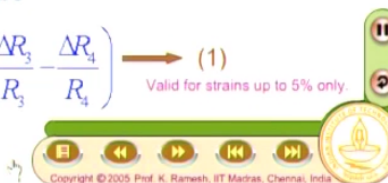
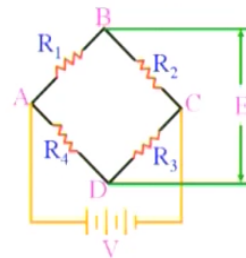
- The bridge is initially balanced ($E = 0$) when $R_1 R_3 = R_2 R_4$

For an initially balanced bridge the output voltage ΔE for an incremental change in the resistances can be shown to be

$$\Delta E = V \frac{R_1 R_2}{(R_1 + R_2)^2} \left(\frac{\Delta R_1}{R_1} - \frac{\Delta R_2}{R_2} + \frac{\Delta R_3}{R_3} - \frac{\Delta R_4}{R_4} \right) \quad (1)$$

Valid for strains up to 5% only.

Opposite arms add and adjacent arms subtract.



Our focus is what happens, when the resistance changes slightly, and whenever I do any instrumentation I initially balance the bridge, and while balancing the bridge I essentially make $E=0$ that is $V_{BD}=0$ that gives me an expression $V_{BD} = \frac{R_1 R_3 - R_2 R_4}{R_1 + R_2 + R_3 + R_4} \frac{V}{R_1 + R_2}$, when I make $E=0$ this gives me a condition $R_1 R_3$ should be $= R_2 R_4$. So when I construct a wheatstone bridge I need to maintain this relationship.

What should be the individual values of $R_1 R_3$, $R_2 R_4$, which would give me a optimal response of the wheatstone bridge, I would like to have an optimal response because I am measuring very small quantity, so I must also look for every single effort to maximize the signal. And if I have to maximize the signal I should understand how a wheatstone bridge functions, and I should also bring in my understanding of solid mechanics in strain gauge instrumentation.

So the first conditions show when the bridge is initially balanced, I get interrelationship between the resistances, we will see further what way $R_1 R_3$, $R_2 R_4$ should be by looking at the performance of the bridge. What we have seen when I put a strain gauge on one of the arms under the application of the load the resistance of strain gauge will change slightly, and what you have here the expression is.

Suppose, I have 4 strain gauges connected and each one is measuring the respective strain there would be changes in R_1 , R_2 , R_3 , R_4 which would be measured as ΔE , and you have this expression as $\Delta E = V \frac{R_1 R_2}{R_1 + R_2} \left[\frac{\Delta R_1}{R_1} - \frac{\Delta R_2}{R_2} + \frac{\Delta R_3}{R_3} - \frac{\Delta R_4}{R_4} \right]$, what you will have to keep in mind is I have labelled it in a cyclic fashion R_1 , R_2 , R_3 , R_4 this sequence has to be maintained in this expression also.

And what I find here, mathematically I see -sign and +sign, but how we will look at is R_1 and R_2 are adjacent arms, and I have a -sign in between what way we will look at is similar strains in adjacent arms cancel each other, so this is one of the principle used when I want to remove the thermal influence. And what you find R_1 and R_3 they are opposite arms, opposite arms add each other that is how we look at this expression from Solid Mechanics point of view.

And this if you want to maximize I can make this -2 positive, if I have opposite strains on adjacent arms I can make this quantity=4, so that way I will amplify my signal, so the idea is you are measuring very small quantity, and we should always look for ways to increase the signal output. This is also one of the requirement particularly in transducer design, they would have this bridge factor as 4. So now we look at the performance of the bridge.

(Refer Slide Time: 22:41)

PERIMENTAL STRESS ANALYSIS Strain Gauges

Strain Measurement Options

- Measure ΔE directly and relate it to strain.
 - Useful for both static and dynamic strain measurements
 - The bridge has to be initially balanced before making any strain measurement
- Adjusts the resistive balance of the bridge such that $\Delta E = 0$
 - Useful only for static experiments.
 - Can provide higher accuracy but the process is slow.
- In both static and dynamic cases, direct measurement of ΔE is convenient for strain measurement.

Navigation bar: Home, Previous, Next, Stop, Play, Refresh, Search

So before we go into that we look at what are the strain measurement option, and then we will go and optimize the bridge. What way we can do? I can measure the change in EMF directly and related to strain, and this is useful for both static and dynamic strain measurements absolutely no difficulty, but for me to do that the bridge has to be initially balanced before making any strain measurement, so this is very important.

So initial balance of the bridge is very important criteria, and this becomes a very significant when I have thousands of channels, you know I must have electronics and multiplexing type of situation, where I am able to balance and then start doing a measurement. So that is where the instrumentation is now focusing on. The other approach is adjusted the resistive balance of the bridge such that $\Delta E=0$, but it is slow it will take some finite time for it to do.

This is good for static experiments, but it can provide high accuracy. Nevertheless, for both static and dynamic cases direct measurement of ΔE is convenient from practical view point, and that

is what we will try to do. So now we will go and look at how I can improve the signal from my wheatstone bridge.

(Refer Slide Time: 24:38)

EXPERIMENTAL STRESS ANALYSIS Strain Gauges 4

Bridge Sensitivity

- It is a function of
 - Magnitude of bridge voltage
 - Gauge factor S_g
 - Bridge factor n
 - Ratio of resistance m or R_2/R_1

$I = 0.1 \text{ A};$
 V by current capacity
 3 - 5 Volts is nominal

For constant V, n and S_g

$$\Delta E = V \frac{R_1 R_2}{(R_1 + R_2)^2} n \frac{\Delta R}{R}$$

$$= V \frac{m}{(1+m)^2} n S_g \epsilon$$

Hence, choose $m = 1$

So I have the bridge sensitivity, it is a function of magnitude of bridge voltage, gauge factor S_g , bridge factor n , and the ratio of resistance R_2/R_1 . See what we want to look at is, your initial balance only gives me a condition between the resistance, now I will find out for maximum sensitivity what should be the value of the ratio of R_2/R_1 , and we write this expression as ΔE in a much convenient fashion, I have this as $V \cdot R_1 R_2 / (R_1 + R_2)^2$.

And the long expression is replaced by n , which I call it as a bridge factor, and you are essentially measuring $\Delta R/R$, and $\Delta R/R$ can be replaced by $S_g \cdot \epsilon$. So if I have to maximize my ΔE one can also say I have a very large value of S_g , this is one of the focus in semiconductor gauges. But if I want to measure strain both in elastic and plastic regions without altering the instrumentation, we have seen it is desirable that gauge factor is around 2.

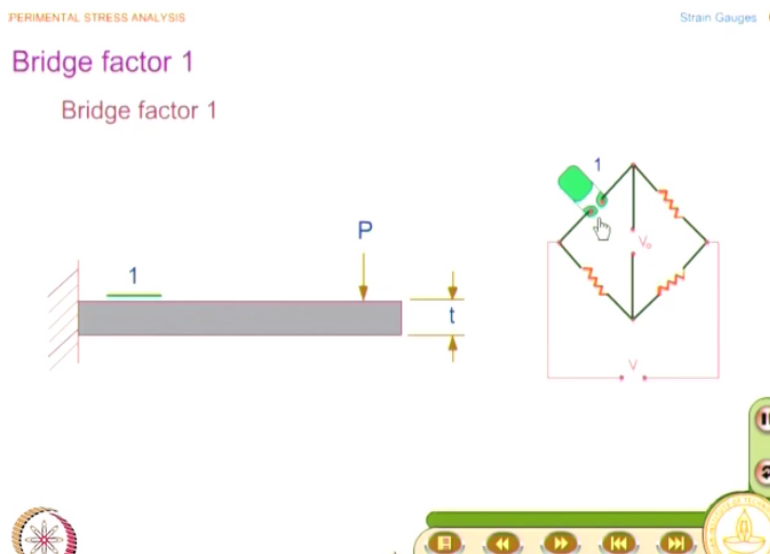
So most of the problems whatever the strain gauge that you have you will find the gauge factor is around 2 to 2.1 that is how you will have it, and so you will not have much change in the value of S_g when you are using the metal foil strain gauges. I can play with maximizing $m/(1+m)^2$ and n , and I can also look at what way I change the voltage, so you should know the relative parameters that we can modify to improve the bridge sensitivity.

And if you look at the current capacity is very small we are only sending 0.1 ampere, and then the voltage that you are going to energize the bridge is only between 3 to 5 volts, you are not supplying a very high voltage, so it is a very small voltage. So now what I will have to do is with these constraints I must maximize this term $m/1+m$ whole square, so if I look at its variation, how does it appear? So what I have here is for constant voltage and bridge factor n and gauge factor S_g .

You find the ratio $m/1+m$ whole square reaches the value of 0.25 when $m=1$, so what does it translate to? You want 4 arms of the bridge to have equal magnitude of resistances, so that is how we will construct a wheatstone bridge, and we also have configuration where I will just use only one strain gauge or use 2 strain gauges or I use 4 strain gauges that is how I will make the bridge depending on the requirement.

So when I do that I will be essentially playing with the factor n , so if you want to have a better sensitivity for the bridge ensure that each arm of the bridge has same resistance to start with.

(Refer Slide Time: 28:31)



Now we look at what is the bridge factor, it is a very simple one I have a single strain gauge connected, and when I do this only one arm of the bridge is connected to the strain gauge, and from our earlier understanding, what this resistance should be? They should be equal to the strain

gauge assistance never forget that, because you know you may have a strain gauge meter which has a provision to connect default 120 ohms or 350 ohms maybe with the model development you may also have selection for 500 ohms and 1000 ohms.

If the bridge is configured for a particular strain gauge you must ensure that you put the balance resistance equal to the strain gauge resistance, you should not miss this fact then your calibration everything will not match for the strain meter. And another caution is we will also have a discussion later connecting only 1 strain gauge poses a lot of difficulties, so it is better to avoid a quarter bridge configuration from minimizing the role of thermal influence, we will see that in detail later.

And there is also a via media I have to use only quarter bridge, how do I reduce the errors we will look at a 2 wire circuit and 3 wire circuit, a 3 wire circuit will minimize the thermal influence significantly. See you will have to look at each aspect, each aspect has to be looked at very closely, and find out how you can improve the sensitivity, what are the kind of errors that come. So that understanding is very much needed.

When I have only 1 strain gauge what happens the bridge factories only one, and this is good enough for strain measurement.

(Refer Slide Time: 31:02)

EXPERIMENTAL STRESS ANALYSIS Strain Gauges 20

Bridge factor 2

Bridge factor 2

Copyright © 2005 Prof. K. Ramesh, IIT Madras, Chennai, India

But when I go for transducer application, I always go for a full bridge for me to find out the maximum signal, and here I have it for a bridge factor 2, and you bring in your understanding of solid mechanics here, what is done here? Suppose I connect strain gauges on the top surface and bottom surface to opposite arms what would happen? For any load, I will have 0 strain, you should not think that my strain meter as gone bad, it is not so.

It is how you have connected the strain gauge to the Wheatstone bridge it is also equally important. See, in strain gauge instrumentation, how do you paste the strain gauge, how they are connected in a Wheatstone bridge, both are important. See, in most of the strain measurement scenario what you do you? You decide that this is the critical location, so I invariably put a one single strain gauge and connect it to my Wheatstone bridge.

You may essentially use a quarter bridge. Only in situations, where the signal is so low, you want to amplify, you may find out methodologies to amplify the signal, and suppose once such application you have put 2 strain gauges on the top of the cantilever and bottom of the cantilever, you know from solid mechanics, for the kind of loading that is applied, the top fiber is subjected to tension and bottom fiber is subjected to compression, and you connect them appropriately on the Wheatstone bridge.

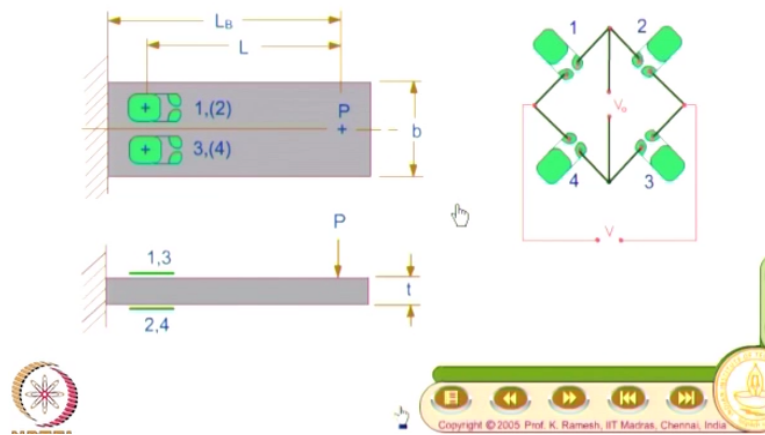
So here the focus is more on amplifying the strain signal, and this also has an advantage that whatever the thermal induced apparent strain in this gauge is cancelled by the thermal strain introduced in this gauge. So you have a better thermal management when you have a half bridge, but you may not be able to use half bridge in many of your applications. In transducer application yes, in strain measurement application it may not happen.

So you will have to find out what application you are looking at, how you can manage the thermal influence. And suppose I want to use bridge factor as 4 with same cantilever, how can I go and do it?

(Refer Slide Time: 33:59)

Bridge factor 4

Bridge factor 4



I can paste instead of one strain gauge on the top surface, I can go and paste 2 strain gauges on the top surface, and connect them appropriately, this is very important, and you will be tested in the examination on this aspect. Because pasting the strain gauge, you need to apply principles of solid mechanics, because you should know how a beam behaves you should know when the beam bends top fiber will be in one state of stress and bottom fiber will be in a opposite state of stress that you should know.

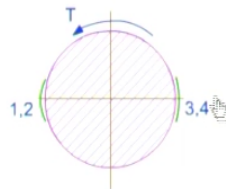
And how they are connected, this is a very, very important and subtle information in strain gauge instrumentation.

(Refer Slide Time: 34:50)

Bridge factor 4

....contd

Bridge factor 4



And you know, I am going to give you one more example, which I leave it as a home exercise. You know, I have taken a shaft under torsion and what I want you to do is, I want you to identify how do I paste the strain gauge 1 and 2, how do I paste the strain gauge 3 and 4, and how do I connect them into Wheatstone bridge for me to measure the torque. See you will have to notice a strain gauge measures strain along its gauge length.

So when I have to decide how to identify the strain gauge to measure torque, you should also look at what is the alignment that I should paste. So all this knowledge you have to get from your basic understanding of mechanics of solids you should understand how a pure shear state can be expressed, you have to use that knowledge, identify the orientation for pasting not only this, how do I connect. See it is very tricky, you know people can make mistake in this.

How do I align the strain gauge, and how do I connect it on the Wheatstone bridge? So I leave this as a home exercise and we will see in the next class what way you have got the answer.

(Refer Slide Time: 36:30)

EXPERIMENTAL STRESS ANALYSIS Strain Gauges

Foil Strain Gauges – Accuracy Achievable

- Foil Strain gauges can be produced with
 - Gauge resistance accurate to $\pm 0.3\%$
 - Gauge factor accurate to $\pm 0.5\%$
- The accuracy of strain measurement are functions of the
 - Installation procedure
 - State of strain being measured
 - Environmental conditions
- The technology is well developed to measure even $0.5 \mu\epsilon$ accurately.

Copyright © 2005 Prof. K. Ramesh, IIT Madras, Chennai, India

See what I have been mentioning is, strain gauge instrumentation, we are looking for measuring small quantities. So we have to pay attention for every minute detail. We looked at strain sensitivity of a conductor, then we graduated and looked at strain sensitivity of grid, and then we also looked at bridge sensitivity. In bridge sensitivity we understood, if I do strain gauge instrumentation each arm of the bridge should have same resistance to start with.

And using the principles of solid mechanics, I can have bridge factor up to 4, this may be good enough in the case of transducer applications in normal strain measurement you may paste just one strain gauge. And what is the level of accuracy that we can think of? It depends on what way we get individual accuracies of the various factors influencing the strain gauge instrumentation. And what is the accuracy achievable possible?

Foil strain gauges can be produced with gauge resistance accurate to + or - 0.3%. And one of the first steps in strain gauge instrumentation is you would measure the resistance of the gauge, and you also need gauge factor measurement, because you may have to set the knob of your strain gauge instrumentation to the gauge factor. Because gauge factor essentially works like a multiplication factor.

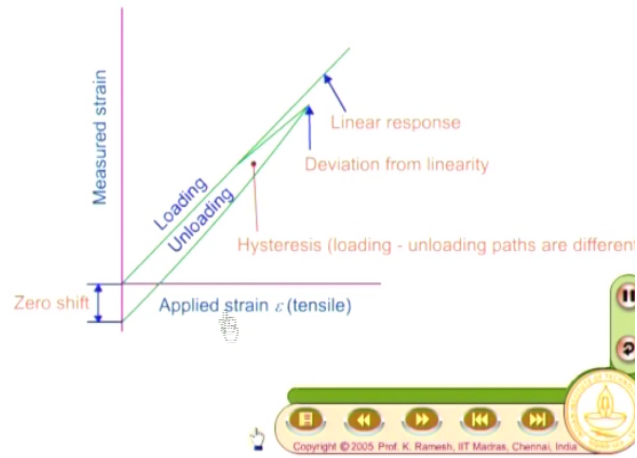
And if you do not set the knob properly, you will not be able to interpret the strain, and in gauge factor can be obtained with an accuracy of + or - 0.5%, reasonably good. See we saw in the case of brittle coating, the failure strain accuracy is only + or - 20%, so strain gauge instrumentation the accuracy levels are much higher. And the strain measurement accuracy depends on what factors? Though I get the gauge resistance and gauge factor very accurate.

If I do not do the installation properly, my entire strain gauge instrumentation can be faulty, and installation is the very important step and you need trained technicians to do that, so this is one factor. The second factor is, what is the state of strain being measured? We will also see different types of strain gauge patterns that will give you an indication how problem becomes complex when I have to find out, what I should do?

Suppose I have a bending scenario, what type of gauge configuration I should use, I have to select. And finally your environmental conditions, you have to take special precautions in aggressive environments, and what you will have to keep in mind is, accuracy in measurement is closely related to technology. And you should be happy that technology is now very well develop to measure even 0.5 microstrain accurately that is an achievement.

(Refer Slide Time: 40:49)

Strain Gauge Linearity, Hysteresis and Zero Shift – Definitions



For you to get that, you need to be very careful about insulation and all the other recommendations that the manufacturer ask you to do that. And there is also another aspect which will have to look at, what is the strain gauge linearity? What is hysteresis? And what is the zero shift? See you would like the loading and unloading path to be same, but in reality the loading and unloading path can be different.

So this constitutes what is known as hysteresis, and when the load is reduced to 0, you may have some apparent strain, it may not necessarily come to 0 and this is called a zero shift. You need to make a decent sketch of it, because when we go and discuss various strain gauge materials, the backing and also the adhesive, we would say certain comments about how does this influence linearity or hysteresis or zero shift, and zero shift is a nuisance in strain gauge instrumentation.

In fact, before the development of SR 4 strain gauges, they had also painted carbon, and then they had (()) (42:26) type of strain gauges, which had very difficult problem about hysteresis and zero shift. And I also mentioned if you have to make a measurement on plastics because current flows through the strain gauge, you have small heat is generated plastic being a poor conductor of a heat, it will not dissipate the heat energy and this heat energy will build up.

And we have also seen, resistance can also change as a function of temperature, so you would find as a function of time, the strain meter will keep on drifting if you do not take care of thermal

effects, do not think that your component is behaving that strain is keep on increasing, it is not so it is a zero shift and that is the nuisance that has to be addressed very carefully. Particularly, when you are going to make measurements for long durations of time, for months and years, you have to worry about zero shift.

And what we will see later is choice of the backing, choice of the adhesive and choice are the alloy for the strain gauge grid everything has an influence. See the advantage of strain gauge is, its versatility it can be applied to a range of problems, but for each class of problems you should select an appropriate strain gauge and all the other associated features, what glue you should use, what backing you should use, these are all not trivial things.


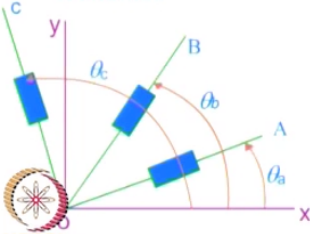
But to an extend that will look boring, because you know you should collect facts, it is not explaining a concept, collection of facts is also important and that is also part and parcel of your learning.

(Refer Slide Time: 44:36)

PERIMENTAL STRESS ANALYSIS Strain Gauges

Determination of Strain at a Point

- A single strain gauge can give only the strain component along its gauge length.
- In many applications, one wants to measure in-plane strain on a free surface.
- In such a case, three components of strain are to be determined.
- This is done by measuring strain along three directions at the point of interest.



Copyright © 2005 Prof. K. Ramesh, IIT Madras, Chennai, India

Now we come to the very important aspect, how do I measure strain at a point. This I have been mentioning it many times, a single strain gauge can give only the strain component along its gauge length. In many applications one wants to measure in-plane strain on a free surface. Mind you, suppose I want to go and paste a strain gauge inside a pressure vessel, I want to know, what is the way the inner surface is stressed, and then I need to bring in certain correction factor.

What happens there? When I paste a strain gauge you have fluid pressure acting on it. So we will postpone how to analyze strain data in those class of problems later, first we are looking at suppose I have a beam that is bend, it has a free surface I paste a strain gauge and find out what is the strain on the surface. So the strain gauge as such is not loaded externally whatever the strain of the base component is faithfully transferred through adhesive, backing system to the strain gauge.

So we want to find out in-plane strain and I need 3 components of strains to be determined. And you know here only you look at strain is a tensor of rank 2 and you bring in the tensorial transformation law. So what I have? I need to find out 3 components of strain, so I need to have 3 strain gauges oriented at angles θ_a , θ_b and θ_c . And you have to bring back your old memories, how do you write strain along a given direction in terms of the tensorial components.

And that is a very famous expression that you have, you can take a minute to recall that expression and try to write. See strain tensor and stress tensor share commonality, tensorial transformation law is similar. And if you know how to write this transformation law, your rosette analysis becomes child's play it is not no longer Greek and Latin, because there the angles are well known you are not taking arbitrary angles, you take certain fixed angles.

So finding out how to get the strain at a point using a rosette becomes very simple, if you know the strain transformation law, I think some of you have written it.

(Refer Slide Time: 48:02)

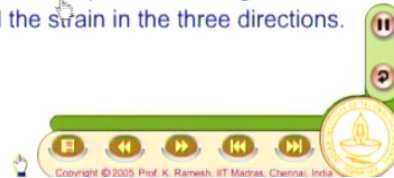
Determination of Strain at a Point

...contd

- Based on strain transformation equations, it is possible to get the components of strain tensor from these measurements.

$$\varepsilon_j = \varepsilon_{xx} \cos^2 \theta_j + \varepsilon_{yy} \sin^2 \theta_j + \gamma_{xy} \sin \theta_j \cos \theta_j$$

- Pre-aligned strain gauges mounted on a single carrier are available from strain gauge manufacturers – these are known as strain gauge rosettes.
- The conversion of strain data to stress on planes normal to the free surface at a point of interest requires knowledge of the elastic constants E and ν and the strain in the three directions.



And the strain transformation law is very simple that is what you have here, I can write it as $\varepsilon_j = \varepsilon_{xx} \cos^2 \theta_j + \varepsilon_{yy} \sin^2 \theta_j + \gamma_{xy} \sin \theta_j \cos \theta_j$. I have written the engineering shear strain component, if you write it in terms of tensorial components it is $\varepsilon_{xy}/2$, and when I go to different rosettes the θ_j will change that is all the difference.

So what I do? I get strain from this expression, and if I use the elastic constants, I can also get the stress information, and the θ measurement becomes very critical that is the reason why you have pre-aligned strain gauges, they are mounted on a single carrier and they are called by a special name called rosettes. And you need these strain gauge rosettes for finding out the strain tensor at a point of interest.

The greatest advantage is, they are pre-aligned and because you are having a metal foil, it is easy to do this very precisely. And I have always been saying the basic information given by experimental techniques is dictated by the physics that we exploit. So in a strain gauge you essentially employ change of stress modifies the resistance of the conductor, and I essentially measure a component of strain.

Once I measure the components of strain, if I know the elastic constants of the base material, it is possible for me to find out the stress on the specimen by invoking equations from mechanics of solids. And let us see 2 famous configurations of the rosettes.

(Refer Slide Time: 50:56)

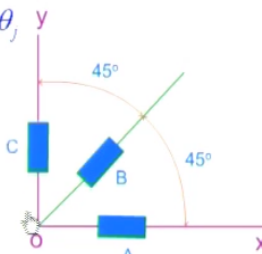

PERIMENTAL STRESS ANALYSIS Strain Gauges 25

Three element rectangular rosette

$$\epsilon_j = \epsilon_{xx} \cos^2 \theta_j + \epsilon_{yy} \sin^2 \theta_j + \gamma_{xy} \sin \theta_j \cos \theta_j$$

$$\theta_A = 0^\circ; \theta_B = 45^\circ; \theta_C = 90^\circ;$$

$$\epsilon_A = \quad \quad \quad \epsilon_C =$$

$$\epsilon_B =$$



Copyright © 2005 Prof. K. Ramesh, IIT Madras, Chennai, India

And one of the rosette is called a rectangular rosette is primarily because I have a strain gauge along the X axis, and the second strain gauge at 45 degrees and the third strain gauge is along the Y axis. So what is the strain measured by the strain gauge A? If I have this as my reference axis, I could simply say its equivalent to epsilon x, and strain measured by the strain gauge C is epsilon y. So now you use this strain transformation law and find out what is the shear strain.

If I will have epsilon A, epsilon B, epsilon C measured from the actual strain gauge use it and find out what is the state of strain at a point. See you have to look at the certain subtle things when I developed the definition of gauge factor Sg, I also cautioned that you have a sensitivity in the transverse direction, which is given by a transverse sensitivity factor Kt. The moment I go to rosette analysis I assume that K t equal to 0, and then write this strain transformation law and find out what is the strain at the point of interest.

Later, we will also see you can bring in correction due to transverse sensitivity effect to the rosette also, in that case the equations will become very complex and that is given by the manufacturer. The manufacturer provides you all this information also, and what will have to

look at, another issue is from measurement of strain by a strain gauge A, B and C, I say that I measure strain at point O that is a point where this strain gauges meet.

If I have to offset this, one way of doing this is, I put this strain gauge move it and then have it here, move this also have it here, move this also have it here, then I will have three strain gauges stack over the other, this is good enough for axial problem. Suppose, I go to a bending problem, the stacking height also can affect your reading okay. Another aspect is, what is its thermal influence?

When I stack it, I am going to have high thermal influence because of current flowing through all the 3 strain gauges. I can probably do it on a thick metallic specimen, where heat is dissipated, so this is where the selection comes. See strain gauge selection is a very big topic by itself, rather than postponing our discussion on strain gauge selection, as and when we learn certain aspects of strain gauge, how this aspect influences strain gauge selection.

And you should also know what kind of approximation that we do, first approximation is I have a finite grid, we have looked at how the gauge length is going to affect your strain measurement. Now you find in a rosette I have to be careful about how this strain gauges are aligned with respect to the point O. So keep thinking about these issues these are very important. Because strain gauges is so versatile.

People think that I paste a strain gauge, connect to the strain meter, they had look at the reading and they go and make the fast conclusions. You know if you do not know the nuances in strain gauge instrumentation you can be way of. And I will show you some example, where if you are not account at certain parameters, a simple calculation can result in 20% error. So you have to know on which kind of component that you are pasting the strain gauge.

And in this class, we have started what is the strain sensitivity of a strain gauge. Then we moved on to how to measure change of resistance, we said Wheatstone bridge is the most celebrated type of measuring approach. Then we looked at what is the accuracy achievable in strain gauge instrumentation. And finally, we had a brief discussion on how do you find out state of strain at a

point, and we have also seen what is the rosette. And in the next class when you come, get the shear strain in the case of the rectangular rosette, thank you.