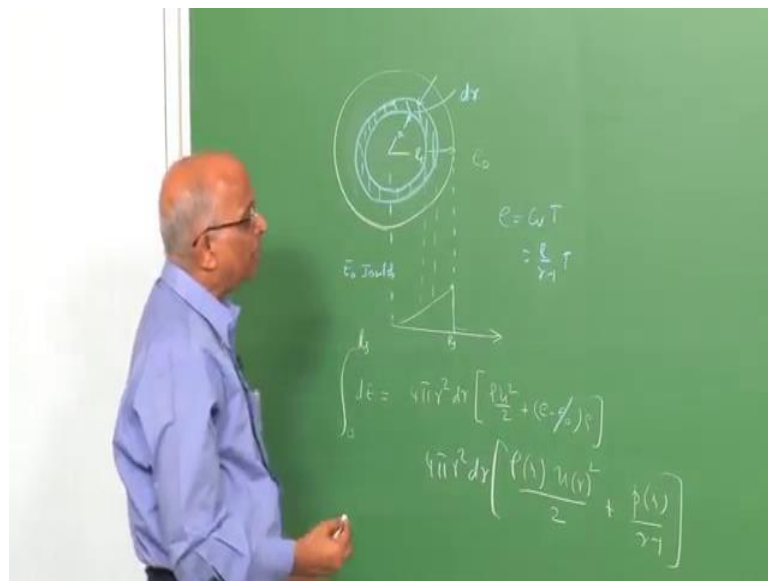


Introduction to Explosions and Explosion Safety
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Lecture - 07
Blast Waves

Good morning.

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You know in the last class we were looking at the formation of a spherical blast wave from an explosion which realised. Let us say E_0 joules of energy, in other words we are looking at the spherical blast wave which is formed at this spherical blast wave keeps propagating outer. So, we told ourselves that this lead blast wave at time T is at a distance R s from the source of energy release. We looked the energy balance and what did the blast wave do you form a blast wave let us take a look at the blast wave you form a blast wave it keeps propagating.

Now, at different times it keeps moving out and, therefore this energy which is deposited is dispersed within the region of the blast wave as the blast wave propagates out. Therefore, we look at the, we look at the conservation of energy namely e_0 joules of energy which is dissipated in the medium and which creates the spherical blast wave. So, what did we do in the last class let us quickly go through the point because we will continue on the energy release and how the blast wave changes.

Therefore, for that I again look at the energy that means we dissipate some energy the blast wave is the distance R_s from the source which is the lead shock wave. We look at the energy which is balanced or we look at the energy which is available at some radius r and of that means I look at this spherical shell of thickness, let us say dr at a distance r . Now, the blast wave is at a distance r, R_s from the source, therefore may be this is my distance this is my distance let us say R_s over here.

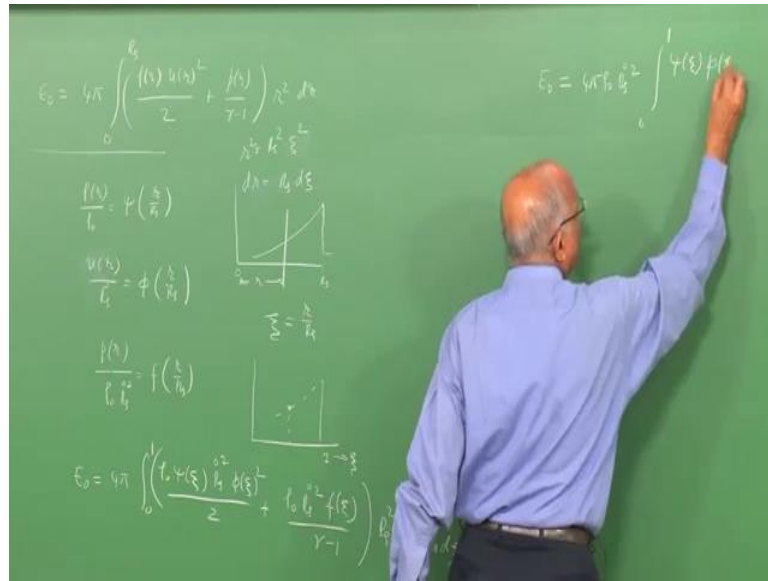
So, the initial pressure jumps up over here and then may be the thing expands out we looked at the expansion in the context of the mass conservation. So, we found that well most of the mass tends to be concentrated different and thereafter there is not much mass left because all the densities over here. Therefore, there is something called as gradient over here we were interested to write the energy which is contained in this small spherical shell over here element of the shell over here.

So, that means the blast wave is here the energy is dissipated I am just interested in the energy here and we got the expression $d e$ is equal to the kinetic energy and what was the kinetic energy. So, the volume of this element is the surface areas $4\pi r^2$ into dr $4\pi r^2$ into dr which is the volume into the kinetic energy per unit volume is the ρu^2 divided by 2 plus. So, you have the internal energy and initially let us say the medium outside has a n internal energy e_{naught} we have e minus e_{naught} into $\rho \omega$ is the change in the internal energy.

Here, we consider that the internal energy change due to the blast wave processing which is very much greater than the initial internal energy. So, this drop out we wrote e is equal to $C_v T$, C_v we said C_p minus C_v is r . Therefore, we could write e, e as equal to $C_v T$, C_v could be written as γ is as equal to r divided that. So, that is the specific gas constant divided by γ minus 1 into T is equal to p by $\rho \omega$ and, therefore this equation became $d e$ is equal to $4\pi r^2$ into dr into I have $\rho \omega$.

So, what is this $\rho \omega$, let us be very careful it is a distance r from the it is it is the distance r from the source of explosion u at r^2 divided by 2 plus I have. Now, p at distance r because r^2 is equal to p by ρ p get p gets cancelled divided by γ minus 1 is the energy which is available in this spherical shell. Now, I integrate the total energy from here to here that means I integrate out from 0 to R_s and that will be equal to this energy and, therefore the expression which we got was e_0 .

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That is the energy in joules which is dissipated to form the blast waves I, now take 4π which is constant outside. Now, I take integral 0 to R_s of I have row r into the value of u at r square divided by 2 plus I have p r divided by $\gamma - 1$ into I have r square into dr this is the expression which we got. Now, when we look at the distribution we say from starting from R_s it keeps decreases over here or it changes over here.

So, I can as well say that my density at r divided by the initial density I can write it as equal to ψ of r by R_s because why do I have to write this you know initially, I have the jump. Then it keeps coming down, therefore we wrote this as row r divided by row s into row s by row 0, row s by row 0 is known. Therefore the density distribution as a function of the initial density could be written in this particular form.

Similarly, I could also write the other expressions the other expressions were we could write the value of u dot by R_s . So, that means let me, let me put down the value of r as specifically the velocity behind the shock at the radius r divided by R_s dot is equal to let us say ϕ into r by R_s . Similarly, I have p at r divided by row 0 into R_s dot square is equal to f into r by R_s all function of the distance from the shock to maybe I am interested in this particular r , I am looking at the value of r by R_s .

Therefore, I would like to solve this equation subject to some distributions like this in the last class when we did the mass conversation we took a power of profile. But, maybe we will, we will consider some of these things again for energy balance, but as of now I

would like to substitute the expressions into this particular energy balance equation and try to solve for it. But, while doing so I can also represent this in a slightly different way let me try to tell what I want to do all. So, what we are telling is we have R_s over here at R_s I have a step change taking place in may be the density may be the particulate velocity may be the pressure.

So, there after it decays down it decays from R_s to 0 I am interested in a distance r over here I can as well change the coordinate system such that I am always saying that well. So, the shock is moving I am having always having R_s as variable, but I am considering at a particular r as the value of r . Therefore, I can consider let us say ζ is equal to r by R_s and I could say well I am considering that case wherein the lead shock is at 1, I am considering the properties let us say.

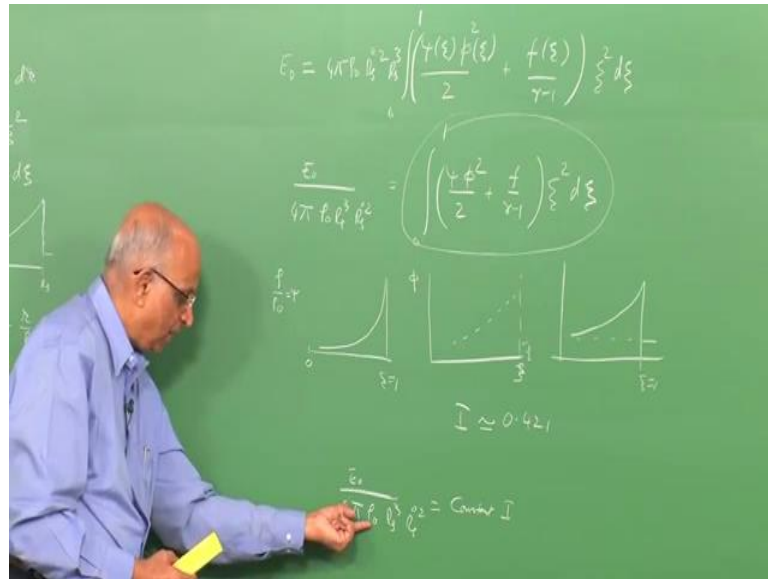
Now, I am coordinate shifts to ζ I am considering the value of ζ over here which is less than 1, I am looking at the property at this particular value of ζ . Therefore, if ζ is equal to r by R_s , well can I change this coordinates automatically r square becomes equal to R_s square is equal to $d\zeta$ and well $d\zeta$ or dr . Let us, let us substitute the value dr over here from this expression becomes equal to equal to R_s for a particular value of R_s I have R_s into r .

So, r square is equal to R_s square into ζ I am sorry r , r square is equal to ζ square into R_s dr is equal to R_s into $d\zeta$. Thus, the limits of integration instead of being R_s over here it becomes R_s by R_s which is 1 and, therefore the above equation for the energy balance will now be given by e_0 is equal to 4π into 0 to 1 into our row r .

So, row r can be written as equal to ζ row 0, row r is equal to row 0 into ψ of ζ into u_r , u_r is equal to ϕ that means R_s dot. So, what is it we have u_r square, therefore R_s dot square into ϕ ζ square divided by 2 plus I have the value of pressure r pressure r is equal to row 0 R_s dot square into ϕ ζ .

Therefore, I have row 0 into R_s dot square into ϕ f of ζ divide by γ minus 1 and this value is multiplied by r square r square is equal to R_s square into ζ square. So, dr is equal to R_s into $d\zeta$ and, therefore if I were to simplify this equation, I get e_0 that is the energy released is equal to. Now, take the terms of said well row 0 is the ambient, the shock is moving or the blast wave at that point is moving with the velocity of R_s dot square.

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Therefore, I get 4π into row 0 into R^3 dot square this is the expression for this taking out then I get the value 0 to 1 and what is it I get. So, I get the value of ψ and ξ divided by the value of velocity that is the velocity at the particular point is ψ divided by ϕ square ϕ . So, ψ square divide d by 2 plus I get f of ξ to the power γ minus 1 into what is left over here I have R^3 and R^3 cube well at a particular radius I am interested.

Therefore, R^3 cube can be taken outside and I have ξ^2 into $d\xi$ this is the expression I get and therefore, now I take, I bring the terms which are outside the integral sign over here. So, I get e_0 by 4π into row 0 R^3 cube into R^3 dot square is equal to this particular integral 0 to 1 of let me take, let me recognize. So, that ψ is a function of ξ ϕ is a function of ξ f is a function of ξ and, therefore I can write it as ψ^2 divided by 2. Now, keeping in mind these are all functions of ξ such that I do not need to carry these symbols as I am doing plus f over γ minus 1 into ξ^2 into the ξ .

Now, you know this expression tells us that the energy deposited in the medium of density ρ_0 is there this energy. So, if I look at that denominator I have $4\pi R^3$ cube 4 upon $3\pi R^3$ cube is the volume this is the mass this is something like the kinetic energy term. Therefore, this expression is an indication of how much of the energy or how much of this energy deposited gets into their kinetic energy of the medium provided. So, that

the entire medium, let us go back to this if the entire shock medium we had to travel at R_s^2 that is the net kinetic energy.

Then this expression tells us that what part of the energy travels at the kinetic energy such that the velocity R_s^2 . Now, this is what this expression tells and, therefore this integral denotes part of the energy which is getting converted into kinetic energy provided all the particles are travelling. But, at the blast wave speed namely R_s^2 you know if I look at this expression little more closely you know yesterday I looked at this point source. So, we said ζ is equal to one at ζ is equal to 1 if I am interested in row by row 0 which is equal to your ψ and ψ we are plotting between 0 to this.

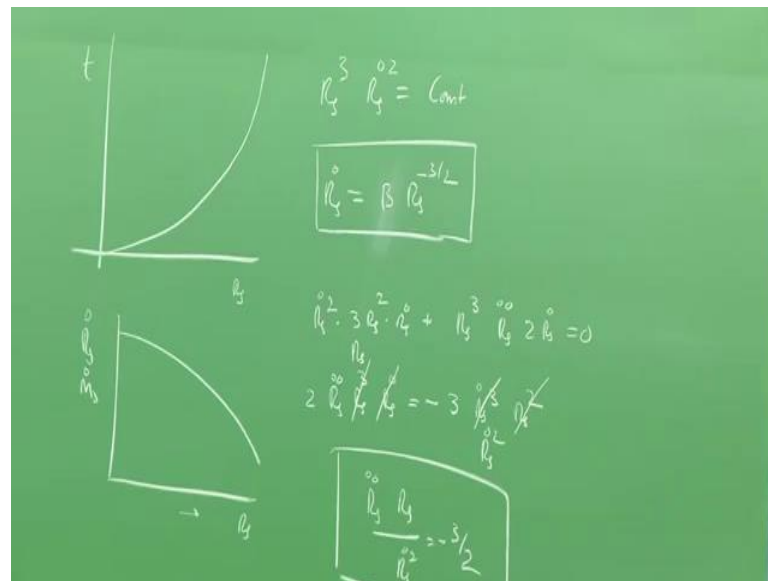
So, that is ζ equal to 0 that ζ is 1 we found well the slope is like this, similarly if I, if I had to take the value of let us say ϕ as a function of ζ and you know at ζ equal to 1 where is there is jump in velocity or there is a change in velocity. So, there is a slope in velocity and, similarly for pressure there is a jump in pressure at ζ is equal to 1 and this jump there is a slope that means between 1 and 0 there is a slope over here. Therefore, we expect there to be something like a power law and this is what we said original used these equations.

Again, we said well William Ray also used these equations to solve for these and you know there are different ways of solve may be could get these things analytically. So, for instance we solve the conservation equations in a blast sort of numerically or we use the perturbation techniques to solve for it or we use the similarity solutions. But, we look at similarity solutions a little later, you know we can always get these slopes and, therefore if we are talking in terms of strong shocks. Well, the jump conditions at ζ is equal to 1 do not really change with the mark number and, therefore we would expect this particular integral to be near a constant namely if I denote this integral by let us say I .

So, I should be near about a constant intend if you really calculate these things using different numerical methods or as I said may be a perturbation method. Now, let us say the similarity solutions I get I is equal to around 0.421 for the case of this sphere spherical wave which we are considering. Therefore, we tell ourselves well this integral is expected to be a constant and, therefore I can write this value. So, let us write this value I get e_0 by 4π into row 0 into R_s^3 into R_s^2 is equal to a constant.

So, this constant is equal to I , which we just now said is equal to this particular integral or this integral which is a constant. So, that tells you what is a fraction of the energy which is deposited gets into their kinetic energy of the medium and this kinetic energy of the medium. Now, we evaluate it at the shock velocity or the blast velocity at that point in time, therefore if this is a constant can I use this equation. So, to interpret something well for a given energy release e_0 in a given medium of density ρ_0 that means let us put down.

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For a given value of e_0 joules in a given medium of density of ρ_0 kilogram per meter cube what is it I get, you know e_0 I have specified ρ_0 I have specified. Therefore, it is a constant, therefore immediately I tell myself well according to this equation $R_s \dot{R}_s^2$ into $R_s \dot{R}_s^2$ is equal to a constant. So, what is it I get, I get R_s^3 into $R_s \dot{R}_s^2$ it is a constant or rather from this equation I get $R_s \dot{R}_s$ is equal to a constant.

So, let us say this constant is v into R_s to the power minus 3 by 2, well if you recall in the second lecture what we had. So, we had used the dimensionless method of deriving the decay of a blast wave, we had got the identical expression let us take a look at this again. So, we have we have to differentiate this, if I differentiate this by parts I get $R_s \dot{R}_s^2$ into differential that is three R_s^2 into $R_s \dot{R}_s$ plus I .

Now, I keep the first value r constant R_s^3 into I get $R_s^2 \dot{R}_s$ into I have 2 into $R_s \dot{R}_s$ is equal to 0 constant is equal to 0. So, let me again repeat $R_s \dot{R}_s^2$ into

differential of the first term $3 R \dot{s}^2$ into $3 R \dot{s}^2$ plus I have over here $R \dot{s}^3$ which I am, which I am which is the first term. So, differential of the second term is a $R \dot{s}^2$ into $2 R \dot{s} \ddot{s}$ and what is it I get immediately I tell myself well in this two terms if I had to take one on the left hand side.

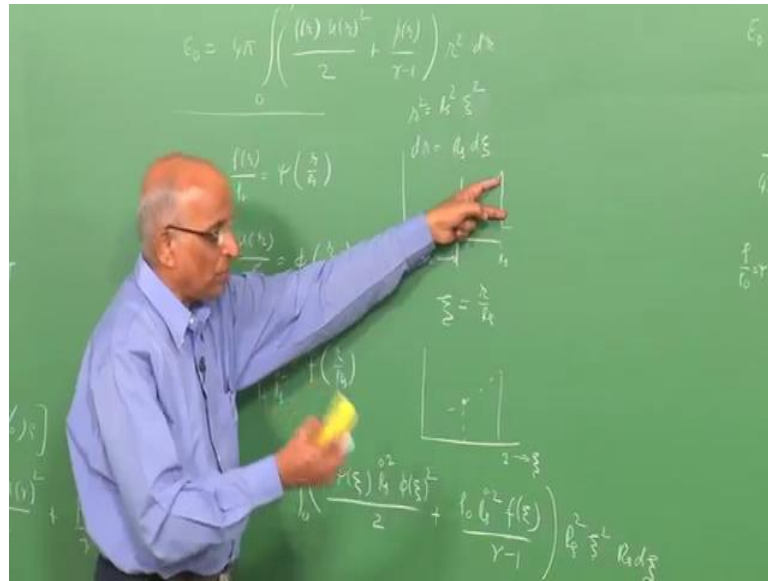
So, I have $R \dot{s}^2$ into $R \dot{s}^3$ into 2 over here into $R \dot{s} \ddot{s}$ is equal to minus 3 on the right hand side. Now, I take it on the right hand side I have $R \dot{s}^3$ into $R \dot{s}^2$ and if I have to take out the common terms over here well $R \dot{s}^2$ cancels here gives me $R \dot{s}$. So, I have $R \dot{s} \ddot{s}$ over here gives me $R \dot{s}^2$ and, therefore I get the value of $R \dot{s}^2$ into $R \dot{s}$ divided by $R \dot{s}^2$ is equal to minus 3 by 2 which was again the result.

So, which way I had got from the dimensional analysis in other words there is a decay that is the shock is decelerating because of the negative sign. So, we got the shock velocity in terms of this and the same results which we got by dimensionless analysis or dimension analysis we are able to get through the energy conservation. Now, this is 0.1 of the energy equation, this must be clear we have solved the energy equation and we get back the condition 12 in a blast wave.

So, what is it which we are telling ourselves in a blast waves well you have the streak diagram temperature versus $R \dot{s}$ you form strong waves. So, it keeps decaying or rather in the frame of preference of $R \dot{s}$ versus $R \dot{s}$ you start with the wave and it steepens as the distance increases the velocity at the front decreases. Well, this is the same signature for $m \dot{s}$ also well this comes from the energy equation let us try to see whether I can use the energy equation to better advantage.

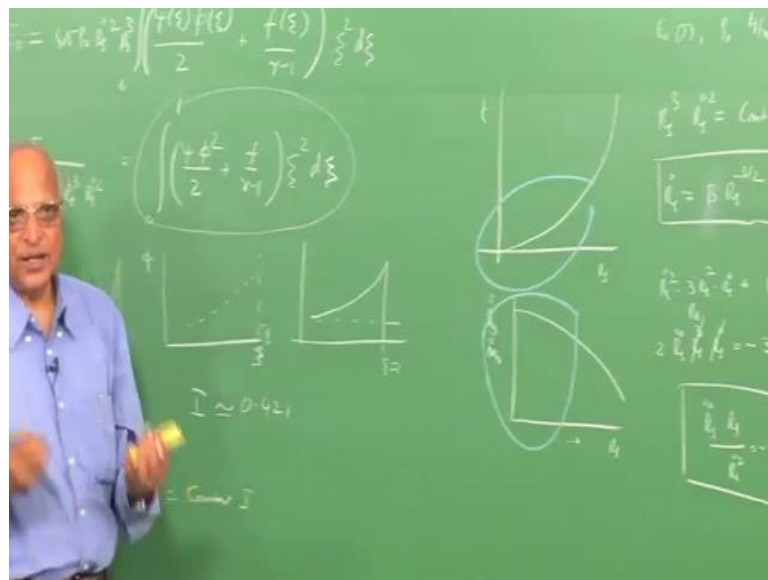
So, to get some more characteristics of these blast waves mind you we must keep something in mind when we did all this we presumed over here. So, that they initial energy of the medium is small, in other words we told ourselves well the blast wave must be strong enough that the value of e_0 can be neglected. Now, second is we also use these profiles which was strictly true only for the case when the Mach number of the blast wave was quite high that means we are talking of strong blast wave.

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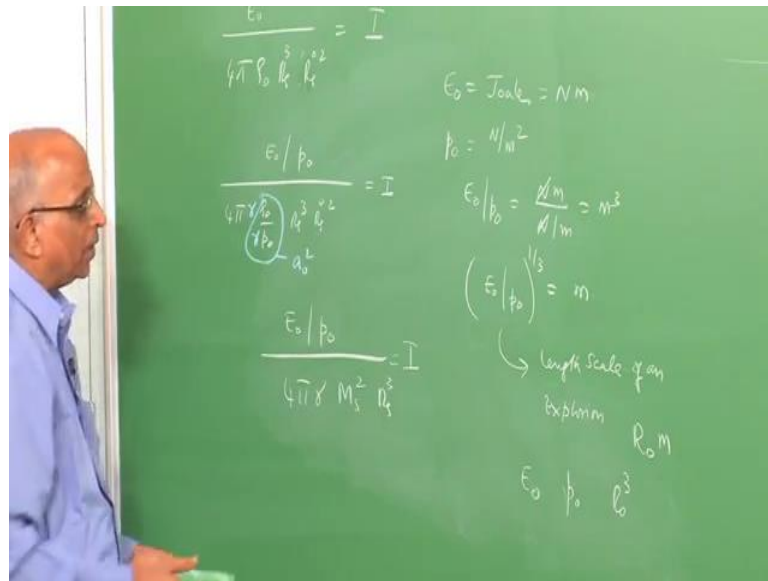
Therefore, the conditions we have derived here are suited only for this initial region or for the initial region over here.

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So, having said that let us go into some more details some more characteristics of the blast wave and try to solve some more parameters for some more parameters. So, let us pick up from this equation itself, let us pick up from this equation namely over here ϵ_0 by 4π let me write it over here.

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We have e_0 , that is the energy released in a medium ρ_0 is equal to we do not need to construct the integral. So, let me, let me put it in terms of the fraction what we have got we got e_0 divided by $4\pi R^3 \rho_0$ is equal to I . Now, I want to slightly transform this equation into something which is more usable which will help me to scale different types of blast waves. So, let us therefore divide the numerator and denominator by ρ_0 that is e_0 by ρ_0 divided by $4\pi R^3$ I also divide the denominator by ρ_0 into I get R^3 is equal to I over here.

So, I have just copied this equation here I have $e_0 / 4\pi R^3 \rho_0$ is equal to I , I get this particular expression. Now, let me do something let me multiply the denominator by γ and also divide by γ such that I still retain the same. Now, I look at this particular equation I have $\gamma \rho_0$ is equal to a_0^2 that is the sound speed in the free stream medium. So, that is ahead of blast wave and I also know well R^2 divided by a_0^2 is equal to the mark number of the shock.

So, Mach number M_s is equal to R by a_0 and, therefore substituting this expression in this particular one. Now, what is it we will get we will get the value of e_0 by ρ_0 divided by $4\pi \gamma$ into M_s^2 is equal to I which is a constant. So, we say it is equal to around when the, for the spherical case which we are right now dealing its equal to something like 0.423. Therefore, now let us take a look at this particular

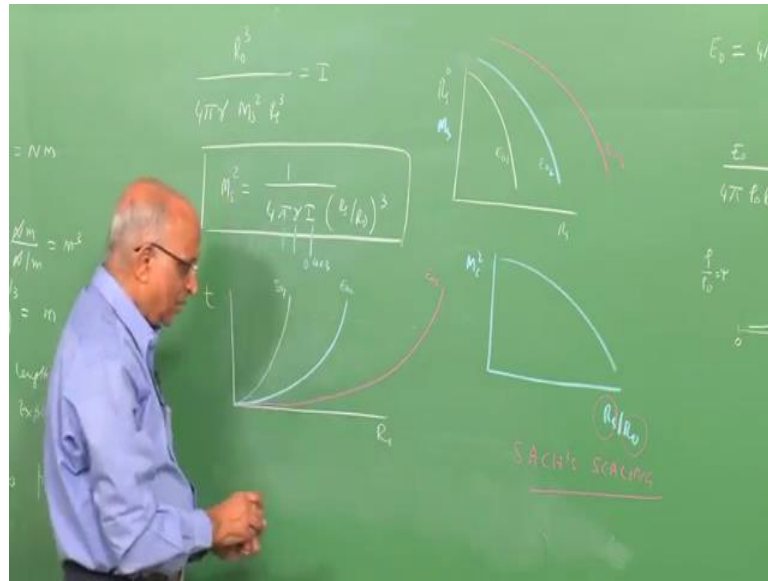
expression whether it will help us to simplify things well in this equation $4 \pi \gamma$ into $M s^2$.

But, I think I have still to write the gamma of R^3 is equal to I , now if I were to look at the parameters. Now, I say well e_0 , e_0 is equal to energy releasing Joules what is a joule is a Newton meter if I look at the value of pressure is Pascal which is Newton per meter square. So, if I look at the dimensions of e_0 by p_0 I find that the dimension is equal to Newton meter by Newton per meter which is equal to meter cube Newton and Newton gets cancelled. So, it becomes meter cube or rather if, now I say I am looking at the value of the e_0 by p_0 to the power one-third I get the unit as equal to meter.

Therefore, now I tell myself well e_0 by p_0 is equal to meter cube or e_0 by p_0 to the power $1/3$ is a matter. Therefore, I can talk in terms of e_0 by p_0 as a length scale which is associated that is a length scale associated when an energy is impressively released in a medium whose density is p_0 . So, that means I say length scale of an explosion I define length scale of an explosion is equal to e_0 by p_0 and it tells me if an energy e_0 joules is deposited in a medium of pressure p_0 .

So, I get a length scale and this length scale of an explosion I denote by r_0 so much meters, in other words when I have an energy release e_0 joules in a medium of p_0 . So, the ratio of e_0 p_0 is equal to the explosion length square and, therefore I use this explosion length in this particular expression and what is it I get, let us put that down I get the value of...

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Over here I get r_0 explosion length square divided by $4 \pi \gamma$ into the value of M_s square into R_s cube is equal to I or rather from this can I get the value of let us say I . So, I take the value, the r_0 naught I bring it here I get explicitly the value of M_s square the mach number of the blast wave what it is it going to come. So, it is going to come is equal to 1 over 4π into γ into I into I get R_s by r_0 naught cube this is the value of the mach number of the lead blast wave.

Now, what does this expression tell us all what we had telling is instead of considering the distance if I consider the distance which is divided by the equal and explosion length. So, that means I have the distance which is scaled then I get a value of Mach number square which is given by this if I look at this expression. Well, γ is 3.14 for if, I am sorry π is 3.14 to γ for particular air is 1.4 we said is a constant around 0.423 .

Then what we find m square is a function of R_s by r_0 naught cube, in other words what does happen when we reduce the energy release in terms of an equal length scale. So, namely the explosion length what is it we have done let us take a look at the figure again and try to interpret this result. So, we tell ourselves, we will go back to the streak diagram with which we are all familiar by, now we say this is the distance followed by the lead blast wave.

So, initially some energy is deposited in a medium I get this to be my blast wave let us say that the energy release is e_0 1 joules from a strong shock wave which decays. Now,

I deposit much higher value of energy what is going to happen well if the shock is going to be getting started strongly and it decays after a longer time. Well, this is what the case of $e_0 2$ joules in which $e_0 2$ joules is greater than the $e_0 1$ joules if, now I deposit even a much larger value of energy.

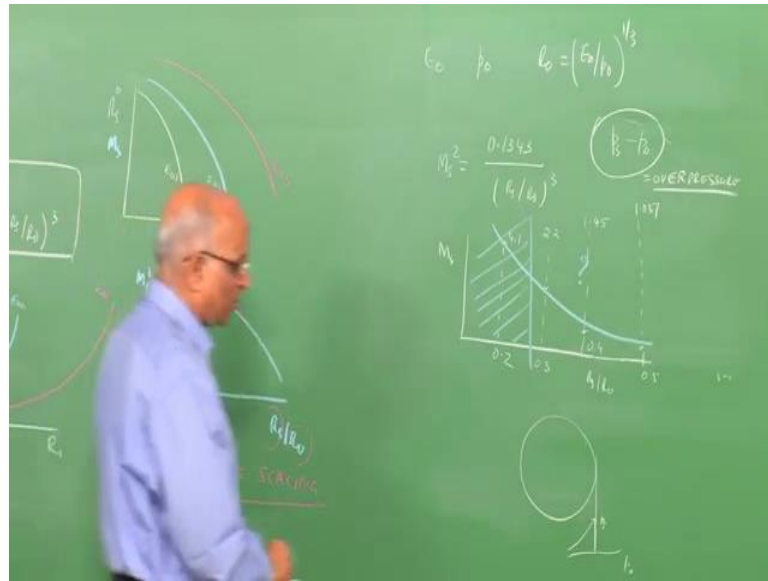
So, what is it I get well, therefore since the energy released is higher it travels a further distance this is $e_0 3$ Joules. Therefore, may be if I the depending on the energy release I get for this same time may be I get a blast which is which is farther away. So, rather if I there to put this particular figure in terms of let us say the mach number or the $R_s \dot{}$ as a function of R_s what is it I get you recall s . So, we looked at the decay initially I get a for $e_0 1$, I get this type of result may be for $e_0 2$ may be I get some result like this we use the blue colour may be I get $e_0 2$ like this.

So, may be when I talk in terms of $v_0 3$, I get a result like this that means I get at this distance when energy release is higher. So, I expect a stronger shock and this is what it tells and, therefore what is it we are telling well $R_s \dot{}$ depends on well $R_s \dot{}$ divided by a 0 is M_s over here it has this dependence. Now, what happens instead of using R_s if I use the value of R_s by r naught what is it I get, now I am able to convert this figure into a figure which says if I use this scale distance R_s by r naught.

So, I am looking at M_s square from this particular expression all what it tells is well I have a single curve for the value of $e_0 1$, $e_0 2$, $e_0 3$. But, irrespective of the energy release which gets a portion here I get a single curve and, therefore I am in a better position to solve the equations. So, this ray of characterising that distance travelled by the shock in terms of the explosion length is what is known as Sach's scaling.

So, that means we are able to scale the mach number of the shock in terms of the scale distance and I do not really to construct the energy gets embedded here. Therefore, I do not need this multiply energy curves to do that I can solve the equations straight forward. So, that means let us, let us think in terms of problem all what we say is the following we deposit some energy in the medium.

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Let us say e_0 joules if the pressure p_0 I get the explosion length r_0 is equal to e_0 / p_0 for the spherical as $1/3$ and once I know this. Well, I use this particular expression r_0^3 by $4\pi r$, $r M_s^2$ is equal to $1/4\pi \gamma I$ into R_s at the particular distance R_s . Since, r_0 is known I can calculate the value of my M_s^2 , therefore let us take a look at this expression, again we plot some figures over here I show this on this figure.

But, maybe I look at M_s^2 I substitute the value of these things and what is it I get, I get the value M_s^2 is equal to $0.1343 / (R_s/r_0)^3$. Now, if I have to plot this, what is it I get, I get maybe the value of M_s lets say I take the under root and I plot it as a function of R_s/r_0 .

So, what is it I get when R_s/r_0 is 0.2 the value of my mach number is 4.1 from the above equation I when the value of R_s/r_0 is 0.3. So, I get the value as 2.2 when the values are around 0.4 and how do I get it I just substitute the value here I divide this when it is 0.4 the value is 1.47, 1.45, I am sorry. So, then it is 0.5 the Mach number is 1.037, in other words 4.1, 2.2, 1.45, 1.037 and, therefore this is my Mach number distribution.

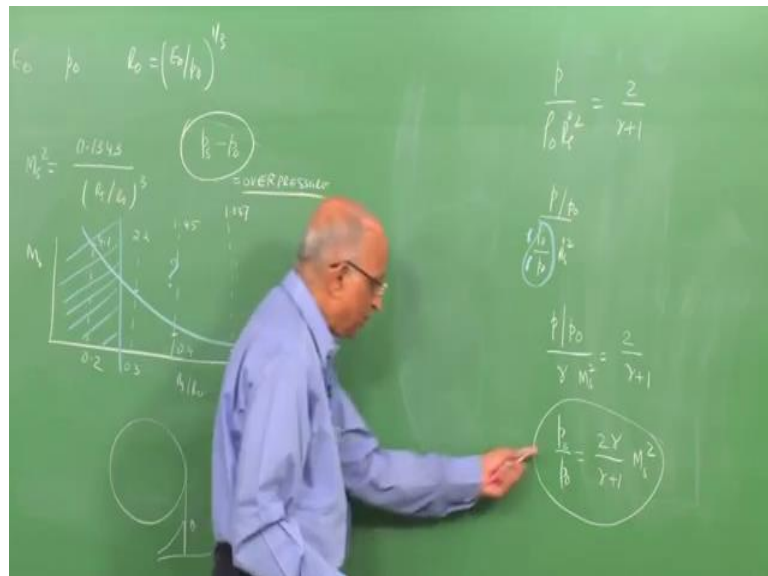
So, what is it I must infer from this well I made a strong blast assumption, but I keep getting numbers and strong blast is normally we form when we were looking at the density ratios? So, yesterday we found that well it must be maybe getting the constant

values of row by row ρ by row ρ R s dot square. So, u by r is when the mach number is typically greater than 4 and, therefore the validity of these particular results are only in this region.

So, in this region the Mach number influences let us say the initial the jump conditions influences the profile and if we in this case the predictions may not really be that good. Therefore, what is it we have done using energy balance we are able to get the lead shock Mach number and if I get the value of M s square. So, I will be in a position to get my pressure also that means I have when the shock is propagating away at the lead shock. Well, I have the pressure initial pressure is p_0 , I have a jump pressure to a value p_s and then it decays, further I can find out what is the jump in pressure.

But, if I know the jump in pressure I can always calculate the jump in pressure is p_s the initial pressure is p_0 and $p_s - p_0$ is the increase in pressure across a lead shock wave. Now, this is something which is known as over pressure let us try to get an expression for the over pressure also we do it its quite simple. So, we have done this already in a in a, since in that we know the value of the shock pressure that means we say p by ρ naught into R s dot square.

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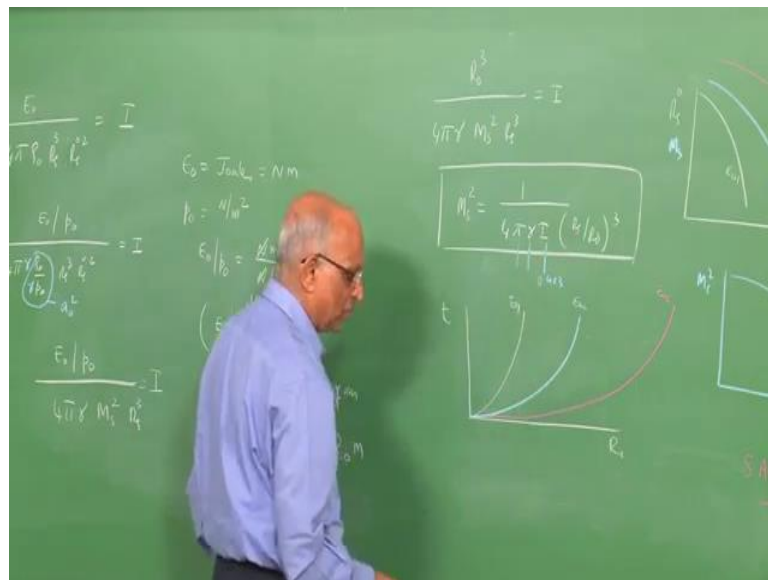
We say it is equal to 2 into gamma plus 1 for a, for the particular case of strong blast wave that means in this particular region. Well, I can simplify this and get it as p by row 0 divide by p_0 in the numerator divide by p_0 the denominator you R s dot square. Well,

let me also divide the numerator and denominator of this particular expression in the denominator by gamma again.

Now, I have gamma p 0 by rho 0 is equal to M s square and, therefore I can write the value of p by rho 0 uses same colour chalk p by rho 0 divided by gamma into M s square is equal to 2 over gamma plus 1. So, rather I get the value of p by rho 0 is equal to I get 2 into gamma plus 1 into gamma into M s square and, now if you were to look back at the equation what we derived or p divided by rho 0 in the third and fourth classes.

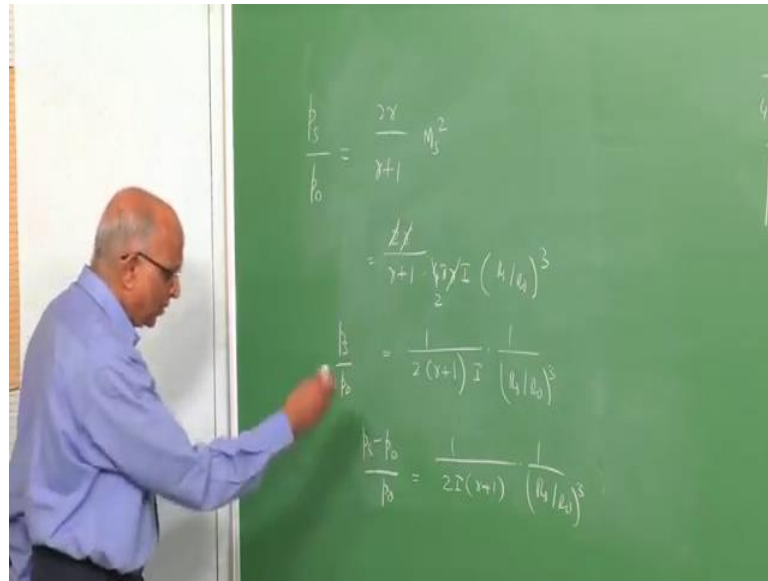
So, we have derived the equations p by rho 0 is equal to 2 gamma by gamma plus 1 m square minus gamma minus 1 by gamma plus 1, since this is weird we are talking in terms of large mach numbers. Well, gamma minus 1 by gamma plus 1 is negligible and this is the pressure ratio, therefore let us calculate the pressure behind the shock. So, to be able to distinguish between p and rho I can write this as p s behind the particular lead blast wave I am interested in the value of p s over here. Therefore, let us derive it, we all what we do is we substitute the value of M s square as we got by solving the energy equation either this.

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Let us put this M s square, as we got here we got M s square is equal to 1 over 4 phi gamma I into R s by R naught cube, so that we can determine the overpressure with particular distance, let us do that now.

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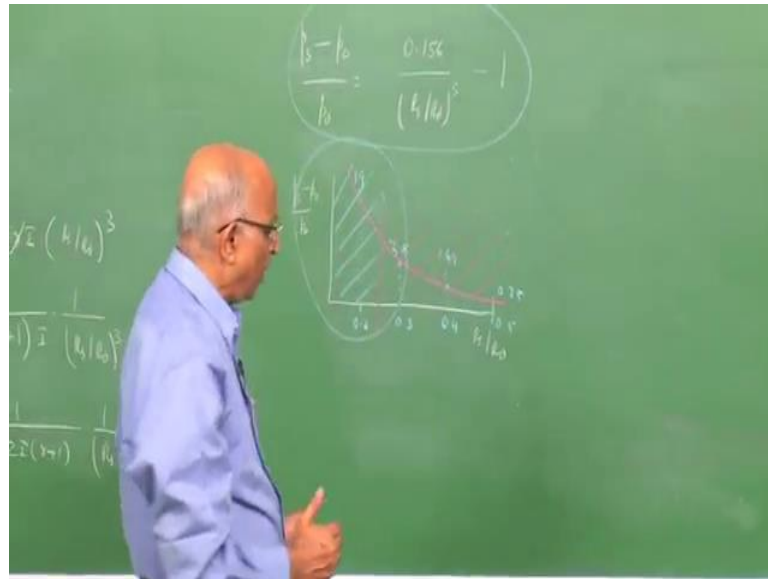


Therefore, write from the expression over there p_s by p_0 is equal to we get is equal to 2γ by $\gamma + 1$ into M_s^2 . But, M_s^2 is equal to 1 over $4\phi\gamma I$, therefore this I can write as equal to 2γ over $\gamma + 1$ into I get now $4\phi\gamma I$ $4\phi\gamma I$ into r by r_0 cube. So, rather in this I find γ and γ gets cancelled this cancels to giving $2I$ get the value as 1 over 2 into $\gamma + 1$, 2 into $\gamma + 1$ into I into 1 over r by r_0 cube.

Now, in other words I get the value of p_s by p_0 and what is the over pressure, over pressure at the shock front is equal to I have a jumping pressure minus the ambient pressure. Therefore, that dimensionless overpressure is equal to p_s minus p_0 divided by p_0 that means you have p_s by p_0 minus 1 . Therefore, the value comes out to be 1 over $2I$ into $\gamma + 1$ into 1 over r by r_0 cube, this is the value of the over pressure and mind you.

Now, we know the value of overpressure or dimensionless over pressure as a function of the stacks distance or the distance divided by the explosion length over here. So, let us take a look at this particular expression and see whether we can interpret this how the over pressure behaves with distance, we will substitute the values and what is it we get, let us, let us get the values.

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We get $p_1 - p_0$ divided by p_0 , now have I is equal to 0.423 their gamma plus 1 is 2.4 I substitute the value it gives me 0.156 divided by M cubed over here. So, this is the value of $p_1 - p_0$ over here I subtract 1, therefore I should have subtracted 1 over here I get this is the value. Now, if I plot this expression that means I plot the over pressure $p_1 - p_0$ divided by p_0 as a function of M .

So, what is it I get lets again do this similar to what I have done over, therefore the mach number I get at a value of M is equal to 0.2 the value of the overpressure. So, that is the dimensionless overpressure gives comes out to be 19 at the value of 0.3 M is equal to 0.3. So, the value comes out to be 3.8 at the value of 0.4 the value comes out to be 1.44 and let us take one last value 0.5 at which the value comes out to be something likes 0.25.

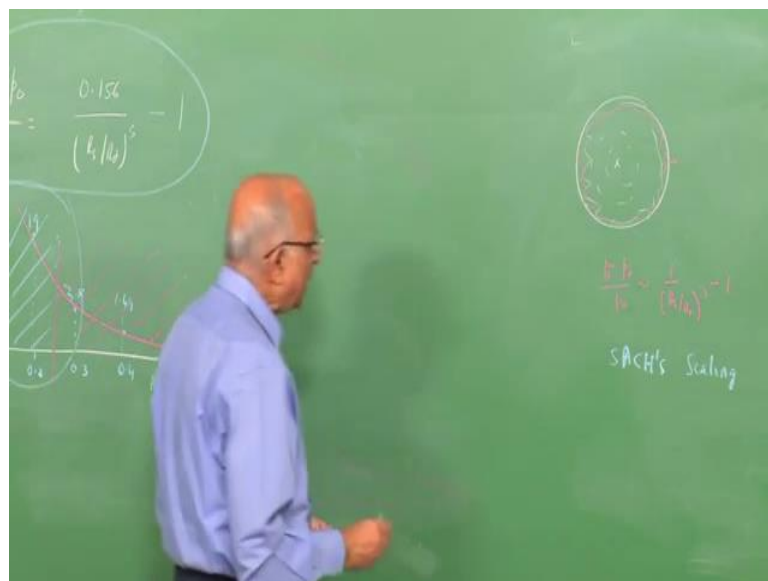
So, in other words if I join the values what I get is well the curve looks something like this and what is it we find well at 0.2 we found out that the mach number was 4.1. Well, strong blast assumption is valid 0.3 the Mach number was 2.2 for which is the over pressure you know.

So, in other words you know when the Mach number has decayed to these types of values well I cannot really expect the over pressures to be correctly predicted because we found. Well, the strong shock wave assumption is not valid I cannot write the density

ratio $\frac{\gamma + 1}{\gamma - 1}$ or $\frac{\gamma - 1}{\gamma + 1}$ is equal to the shock pressure divided by $\rho_0 R^2$ and all that. Therefore may be in this region in the region of these strong shock waves that is in the near field to the explosion I would expect this expression to be really valid.

Whereas, in the far field this expression may not be totally valid, in other words I have been able to get, but mind you know in a particular region I can predict my over pressures. Therefore, using the energy equation I am able to get the overpressure values well this they have quite a bit. Now, what are the let us quickly summarize what will it will we have understood for the blast wave using the mass balance and energy balance what did we tell ourselves. Well, from mass balance what did we get, we found the following namely when we have strong blast wave that is in the area near to the source of the explosion what is it we got.

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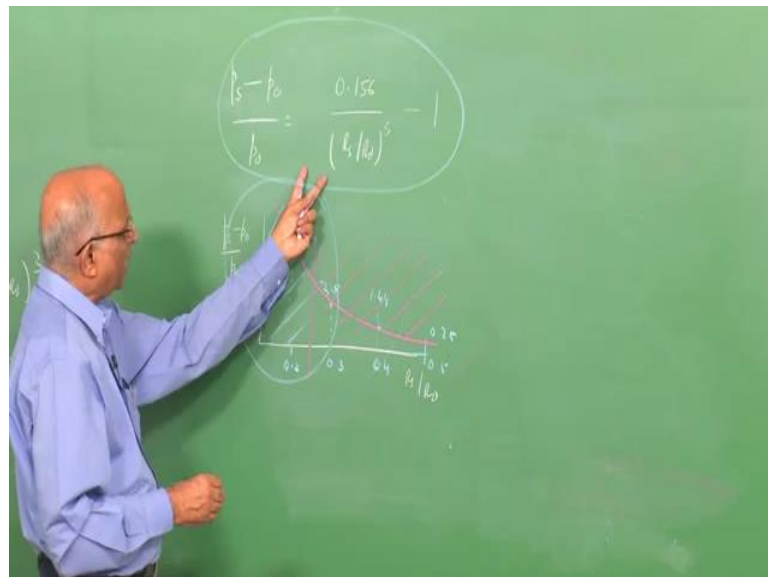


We found that may be I have an explosion over here I form a blast wave over here near to this well most of the blast, the blast wave. So, that is the blast wave as it moves it sweeps collects all the material and locates all the material in the zone of the lead shock wave. So, this is what I have lot of maths here travels with a high velocity and this is what creates my compression or the damage using the energy balance. So, what did we get we have the overpressure shock pressure while as a initial pressure divided by e

naught is a function we get of one over R^s by r naught cube 1 over r naught cube over here minus 1.

Therefore I am able to predict for a given distance what the type of pressure I have over here is, similarly it is possible for me to predict the velocity. But, let us discuss what we have achieved so far in terms of some scaling that means Sach's scaling in which I express the distance in terms of r naught has really been useful. Now, I am able to get the overpressure from a blast frame and overpressure is important because that is the one which creates damage for me because the high pressure compresses. So, damage is a building knocks down people and that, therefore we use Sach scaling over here can I think of anything further.

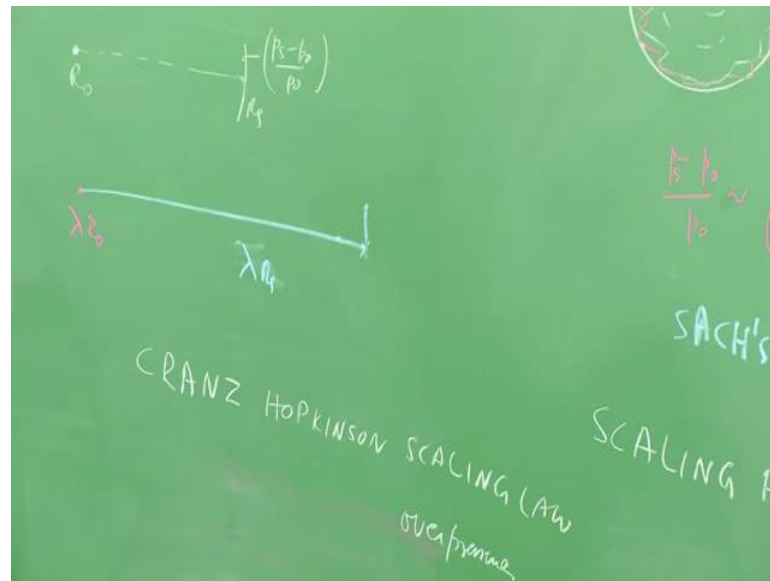
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If look at this particular expression what is it I get can I talk in terms of other forms of scaling can I say how does a blast waves came for over pressures. So, in other words let us ask our questions scaling for over pressure can I can I really solve further for this, what do you mean by scaling for over pressure.

So, supposing I have an explosion in which let us say that the explosion length is r_0 that means I deposit some energy e_0 . Now, I get the explosion length as r_0 because energy release in a medium p_0 is able to define it I am able to get may be at some distance r is a r away. So, I am able to now predict what is my overpressure namely p_s minus p_0 by p_0 minus 1 this is the value of over pressure dimensional over pressure.

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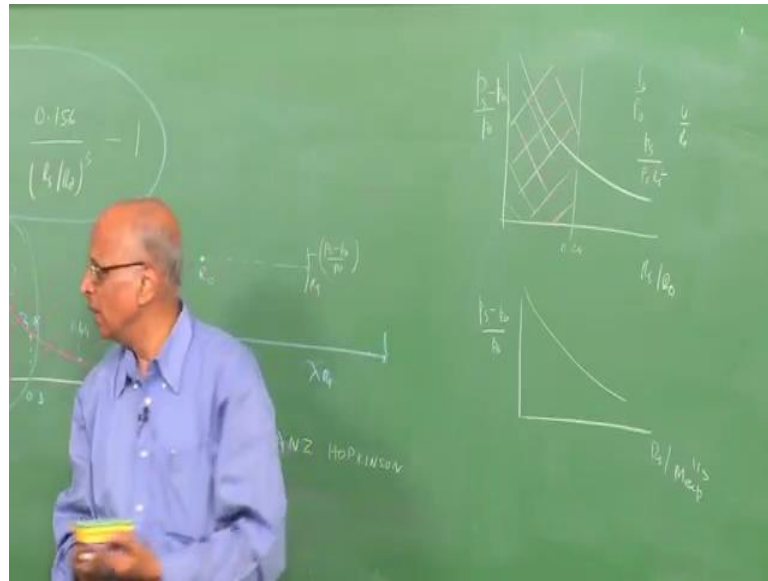


Now, instead of depositing energy by p_0 which is r_0 cube supposing the energy deposited is such that I now have an energy deposited to λ times λ could be multiplication factor. So, that means I deposited a value equal of explosion length e equivalent explosion length to be λr_0 the same over pressure. So, as per this expression will come out to be at a distance of λR_s away will give me the same value why is it because λR_s by λr_0 comes out to be identical. But, even though the energy released is higher well the scale of over pressure over here and the scale of over pressure are same.

So, this type of scaling laws where in which I change my energy level in terms of r_0 to λr_0 is known as Cranz Hopkinson scaling law for over pressures. So, what it states is for if an observer is situated at a distance λR_s away from an explosion whose explosion length λr_0 . So, he will feel the same overpressure as an observer who is stationed at the distance R_s away from an explosion whose explosion length is r_0 as simple as that this is Cranz Hopkinson scaling law.

But, it is used left and right in the explosion industry because we would like to find out what is the, what is the energy released from an explosion how it how it affects the pressure at some distance away. So, Cranz Hopkinson's scaling is widely used let straight to slightly different form we draw the last figure which I draw, now is the figure of over pressure.

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So, I tell myself, well I have p_s minus p_0 divided by p_0 which is the dimensionless overpressure as a function of R_s by r_0 we got this particular curve. So, we told our curve is valid only in the near region of the blast in which the blast wave is small and, now once I know the energy released from the explosion. So, I know the ambient pressure I can calculate r_0 , I want to calculate the overpressure at a given distance, if the distance falls within this let us say around 0.25.

So, I can predict the overpressure and we are able to do some problems, but you know if we look at certain books they do not use the Sach's law. So, in terms of explosion length there are the plot instead of writing r_0 they plot this scale as equal to energy release to the power 1 by 3 because r_0 is equal to e_0 by p_0 to the power 1 by 3 p_0 . So, for most blast in air its around 1 atmosphere pressure that is 10 to the power 5 Pascal and, therefore they express it in this form. So, they get the value of p_s minus p_0 by p_0 and therefore they give a curve like this, but instead of looking at energy.

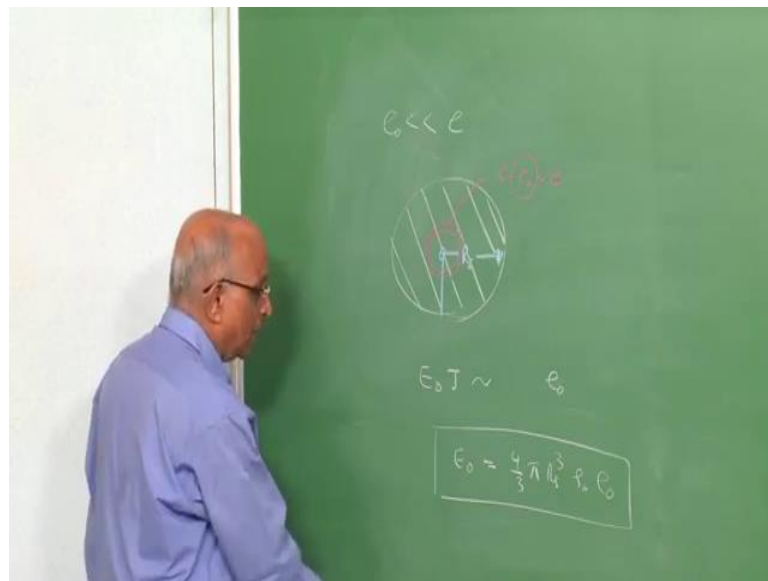
Since, we are looking at energy release from an explosion and this energy release from a explosion is directly proportional to the mass of explosive used very often. Now, why instead of this we even using energy over here they put mass of the explosive use to the power 1 by 3 and this is how many books like Baker's book. So, like in terms of R_s by mass of the explosive or mass of the particular explosive used we will take a look at this

a little later. Now, this is how figures are drawn well this is Cranz Hopkinson's scaling laws we are able to get the overpressures.

But, something which we must keep in mind see I keep qualifying each time we can predict in the near field of the explosive where in the blast wave is high. So, why because we showed earlier that the value of ρv by ρv_0 at the shock front p by p_0 R by R_0 square. But, the value of U divided by R by R_0 are all above the same in this particular region because the jump conditions did not really depend on the mach number square.

Whereas, in this region it is a function of Mach number square, therefore the integral which we use here in the expression as equal to 0.423 may really not be valid. Therefore, it is only in this region which we can use let us try to get some more information of that and for that let us look at the assumptions what we made. So, with that may be will be will be a little wiser, what is the assumption which we made while deriving this overpressure relation.

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Well, we assumed that the value of the initial internal energy of the medium is very much less than the internal energy of the medium which gets enhanced due to the blast wave. So, rather you will recall the recall that we had a spherical blast wave we talk in terms of a small segment or a small annular area spherical shell over here in which we said it is equal to e minus e_0 is equal to e . So, that means we neglected the value of e_0

that means what is it we have neglected we have neglected the internal energy of the medium.

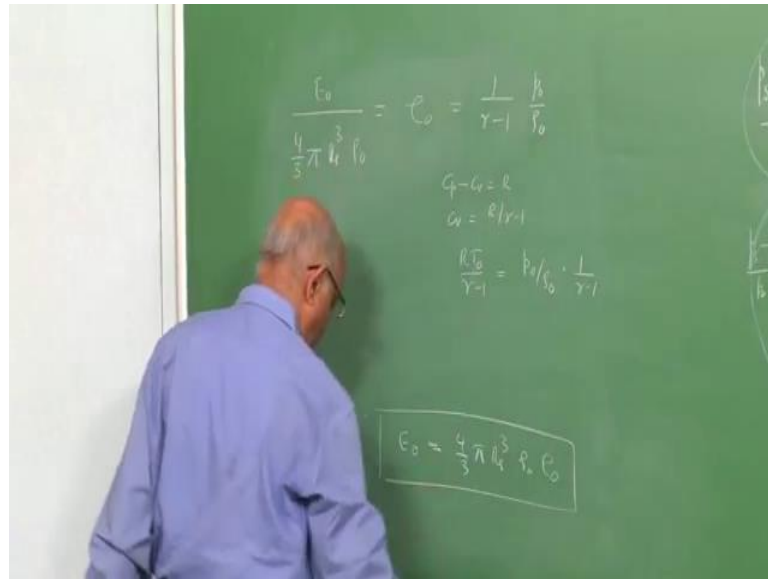
Here, can we find out under what conditions for what values of R_s by r naught does the internal energy of the medium become significant. So, let us say in this particular figure if I find that R_s by r naught for this for R_s by r naught greater than this e_0 becomes significant.

Well, I can immediately say in this region the internal energy has initial internal energy of the medium has to be considered. Therefore, my predictions are only valid in this particular band or in this particular band of R_s or r naught, therefore let us do the problem. Therefore, we tell ourselves well the shock is over here the source is here this is the shock which is R_s distance away and what is it we are telling ourselves.

Well, the energy release of the by the source we say is again e_0 joules and if the initial internal energy of the medium has to contribute. But, what is it we are saying e_0 joules must be of the same order as the internal energy e_0 of the medium, but what is the internal energy of the medium is ρ unit mass. Therefore, we tell ourselves when e_0 is equal to $4 \text{ upon } 3$ that is the volume occupied by the particular volume within the lead shock wave $4 \text{ upon } 3 \phi$ into R_s cube into the density.

So, that is the mass which is available here is equal to into e_0 that means the internal energy of the medium here is of the same order as energy release. Well, I should be able to get this particular point and beyond this what is happening is the initial internal energy affects my shock or affects my over pressure. But, it also affects my mach number of the shock and, therefore I can look at this particular expression and get a feel for what is the value of R_s by r naught. So, from this expression which will decide whether the region in which my predictions are quite reasonable, let us do this to be able to do this I just simplify this expression.

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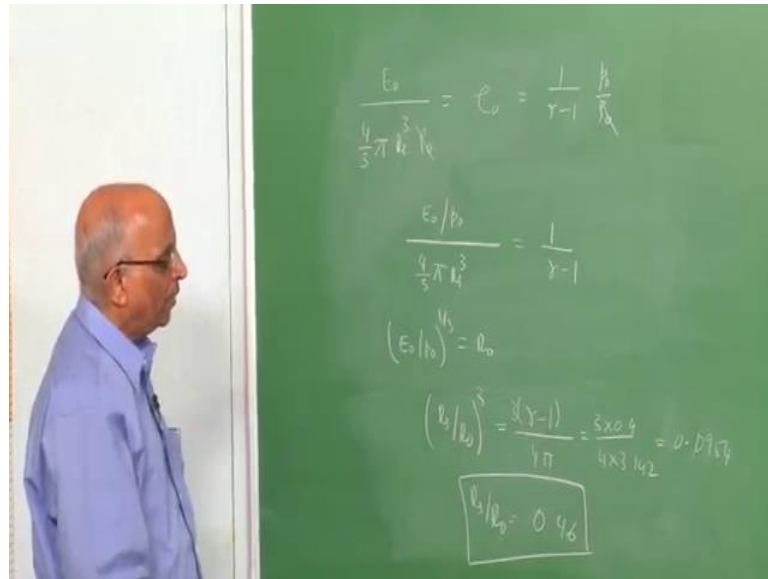


So, I get the value of E_0 divided by $\frac{4}{3}\pi R^3 \rho_0$ is equal to e_0 and what is e_0 internal energy by unit mass which is equal to $C_v t$. So, that is specific heat at constant volume into temperature because we know that de by de of temperature is equal to C_v , $C_v t$ is the value and C_v . Now, we have seen earlier can be written as again we do that C_p minus C_v is equal to specific gas constant C_v is equal to, therefore r divided by γ minus 1.

Therefore, I get the value of $C_v t$ as equal to $r t$ by γ minus 1 or this is equal to p_0 and the ambient temperature is t_0 . So, this is equal to p_0 by r_0 and, therefore this part $C_v t$ I can replace by the value of p_0 by r_0 is $r t_0$ into 1 over γ minus 1. Now, I carry this forward here and, therefore $C_v t$ can be replaced by or e_0 can be replaced by the expression 1 over γ minus 1 into p_0 by r_0 .

So, if I have to solve this particular expression over here what is it I get, I get e_0 I bring p_0 over here in the numerator divided by what is it I get. Well, r_0 , r_0 gets cancelled over here I get $\frac{4}{3}\pi R^3 \rho_0$ is all what is left over here is equal to 1 over γ minus 1 portion. So, the terms e_0 by p_0 is what we call as cube of the explosion length e_0 by p_0 to the power $1/3$ energy release in a medium $1/3$ is equal to r naught and, therefore what is it I get, so I simplify this.

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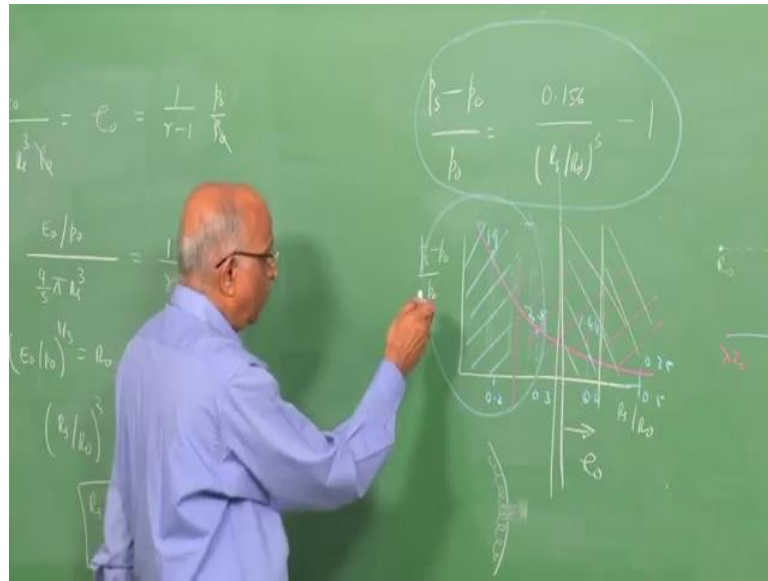


I get the value of R_s by r naught cube bring it on the right hand side over here must be equal to I get the value of gamma minus 1 divided by 3 comes on top. So, 3 into gamma minus 1 divided by 4 pi 3 into gamma minus 1 divided by 4 pi is equal to this particular value and what is the value. Now, I am able to find out the value of R_s by r naught at which the value is such that if R_s by r naught is greater than this value. So, this value let me get the precise number for you the value of R_s by r naught is equal to put the value three into 0.4 divided by 4 into 3.142 which is equal to 0.095.

Now, rather the value of R_s by r naught taking the cube root comes out to be 0.46 and, therefore what is it we tell ourselves if the value of R_s by r naught is greater than this particular value. Well, my predictions are all wrong because the initial internal energy begins to play a role and predictions will be much lower than this. But, in, but we also found when it is 0.4, the mach number of the shock has already decreased to a value around 2 or something.

So, it is still in the weak blast region the predictions what we have done so far are, therefore valid only for values around. Now, let us say less than around 0.25 or 0.3 this is where I conclude today and be able to put things in perspective what is it we have done we have looked at the energy conserved by the lead shock wave. So, we have been able to get an expression for p_s that is the over pressure behind the over pressure of the blast wave.

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So, in addition to this we talk in terms of Cranz Hopkins scaling law we talked in terms of Sach's scaling law which is able to give us this expression. So, we also did in the last class the mass balance which told that whenever I have a strong blast region, well the mass gets concentrated at the front. So, this is mass concentration is something like a hammer and something like a concentration which moves my material at high velocity and tells the dimension.

Therefore, in next class what we look at is we have, we are looking at only the strong blast region we would like to take a look at the weak blast region such that we can we can have some expressions for this. But, in weak blast region it is somewhat difficult as we tell ourselves the initial conditions are dependent on Mach number.

Therefore, we look at the weak region and get the overall that means in both the strong blast region and the far field region in which the blast wave has decayed. So, we try to get the overpressure and in addition to this we also take a look at the impulses and with that we would be done with the blast wave.

Thank you then.